



# SUSY scenarios for muon $g-2$ anomaly: LHC Run 2 and future

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ELTE Eötvös Loránd University

<http://pppheno.elte.hu/>

(2023 Feb. – Natl. Sun Yat-sen U., Taiwan)

8 Jul. 2022

ICHEP2022 @ Bologna

Based on works with

Manimala Chakraborti, Motoi Endo, Koichi Hamaguchi, Jong Soo Kim, Teppei Kitahara, Rafał Masełek, Kazuki Sakurai, Keisuke Yanagi, Tsutomu T. Yanagida, and Norimi Yokozaki, [1704.05287](#), [2001.11025](#), [2104.03217](#), [2104.03223](#), [2202.12928](#), and works in progress.



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- hint for better understanding of **SM**?  
... "lattice QCD vs data-driven calculation"
- hint for **new physics** beyond the SM?  
... **SUSY?** → this talk

SUSY **is/was** a nice candidate for the model beyond the SM because of several reasons.

## ■ Motivations for SUSY

- leads to superstring theory, ... beyond this talk
  - ~~solves naturalness problem,~~ ... disfavored by LHC (non-discovery of top-squark)
  - helps gauge-coupling unification,
  - contains **dark matter** (DM) candidates,
  - solves the **muon  $g-2$**  anomaly.
- } → **current status / prospects?**

[ Minimal Supersymmetric Standard Model ]

❖ This talk focuses on MSSM with  **$R$ -parity**.

( Extended MSSM scenarios (gravitino,  $R$ -parity violation)  
→ Chakraborti, Si, Kim, Masełek, Sakurai [2202.12928] )

➤ **The **LSP** becomes stable: Good dark matter candidate!**

[ Lightest SUSY Particle ]

In SUSY, DM and  $g-2$  are tightly related: Neutralinos appear in both.

## DM

- 4 candidates:

Bino  $\tilde{B}$ , Wino  $\tilde{W}^0$ , Higgsinos  $\tilde{H}_u^0, \tilde{H}_d^0$   
 (mixed to form neutralinos  $\tilde{\chi}_{1,2,3,4}^0$ )

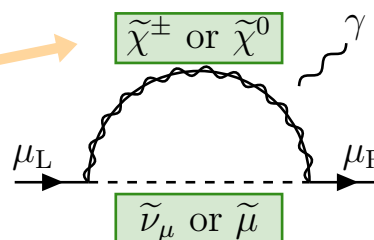
- DM density  $\Omega h^2$  is (in "simplest" setup) fixed by annihilation cross section:

$\tilde{W}$ -LSP  $\rightarrow m_{\text{LSP}} \sim \mathbf{2.7 \text{ TeV}}$ ,  
 $\tilde{H}$ -LSP  $\rightarrow m_{\text{LSP}} \sim \mathbf{1.1 \text{ TeV}}$ ,  
 $\tilde{B}$ -LSP  $\rightarrow$  extra mechanism to reduce DM,

to have  $(\Omega h^2)_{\text{LSP}} = (\Omega h^2)_{\text{DM}}^{\text{obs}}$ .

## Muon $g-2$

- Extra contribution



SUSY particles

$\tilde{\chi}^0$ : neutralino

$\tilde{\chi}^\pm$ : chargino

$\tilde{\mu}$ : smuon

$\tilde{\nu}_\mu$ : mu-sneutrino

$$a_\mu^{\text{MSSM}} \approx \frac{m_\mu^2 \cdot (\text{coupling})^2}{(\text{SUSY-particle mass})^2} \stackrel{!}{=} 2 \times 10^{-9}$$

$\rightarrow$  relevant SUSY-particles should  $\lesssim \mathbf{1 \text{ TeV}}$ .

Lopez, Nanopoulos, Wang [[ph/9308336](#)]

Chattopadhyay, Nath [[ph/9507386](#)]

Moroi [[ph/9512396](#)]

(cf. Cho et al. [[1104.1769](#)])

thermally-produced, freeze-out DM  
 with the standard thermal history of Universe.

The **LSP** becomes stable: Good dark matter candidate!

[ Lightest SUSY Particle ]

**It is not straightforward to achieve both.**

If  $g-2$  anomaly = MSSM contribution,  
LSP mass  $\lesssim O(100)$  GeV. Then...

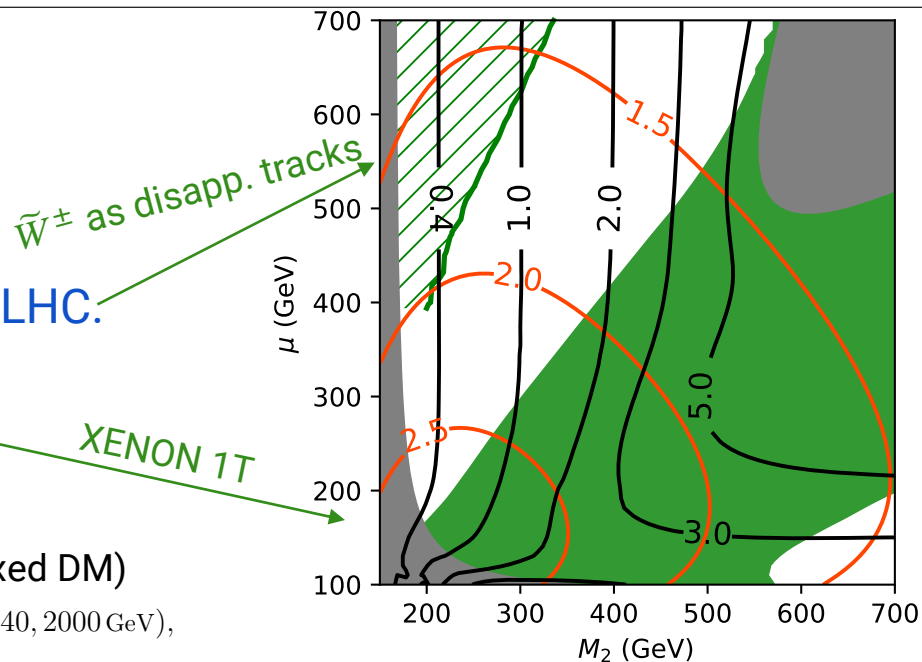
- $\tilde{W}$ -LSP  $\rightarrow$  explains only  $\sim 1\%$  of DM  
+ constr. from wino searches @ LHC.
- $\tilde{H}$ -LSP  $\rightarrow$  explains only  $\sim 1\%$  of DM  
+ constr. from direct detections.

Example: "SUGRA" framework of SUSY-breaking  
(Wino / Higgsino / Wino-Higgsino mixed DM)

$$(m_0, M_1, M_3) = (0, 3800, 2500) \text{ GeV}, \quad (\tan \beta, m_A) = (40, 2000 \text{ GeV}),$$

$$(A_u, A_d, A_e) = (-1000, 0, 0) \text{ GeV}.$$

**Price: Avoid constraints && (extra DM || non-simple cosmology)**



— :  $\Omega_{\text{LSP}}/\Omega_{\text{DM}}$  [%]  
 — :  $\alpha_{\mu}^{\text{MSSM}} \times 10^9$   
 Green: exclusions

$\tilde{B}$ -LSP  $\rightarrow$  needs extra mechanism to reduce bino-DM.

➤ ~~Bino-Higgsino mixing~~  $\leftarrow$  disfavored by DM direct detections.

➤ Coannihilation

+ constraints from LHC searches.

} latter half of this talk

**Price: Avoid LHC && (DM reduction mechanism || non-simple cosmology)**

\* Wino disappearing track searches: ATLAS [2201.02472], CMS [2004.05153]

[  $2\ell + \cancel{p}_T$  from  $pp \rightarrow \tilde{\nu}\tilde{\nu}^* \rightarrow \tilde{W}^+\tilde{W}^-$  may also provide constraints.]

\* direct det. by XENON1T [1805.12562]; not included are PandaX-4T [2107.13438] and LZ (2022).

## SUSY now: DM and muon $g-2$

### 1. DM $\Leftrightarrow g-2$ : tightly connected in MSSM

- $\tilde{W}$ -LSP &  $g-2$  = partial DM + LHC constraints
- $\tilde{H}$ -LSP &  $g-2$  = partial DM + direct det. constraints
- $\tilde{B}$ -LSP &  $g-2$  = too much DM + LHC constraints

extra DM?  
non-simple cosmology?

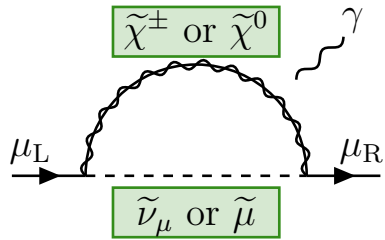
coannihilation?  
non-simple cosmology?

### 2. MSSM provides 4 scenarios (solutions) to the $g-2$ anomaly.

1. WHL:
2. BLR:
3. BHL, BHR:

### 3. Conclusion

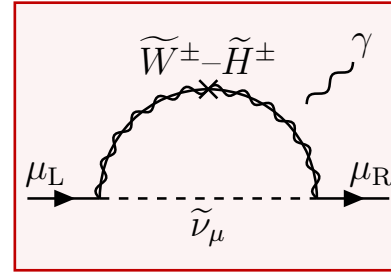
# MSSM has four dominant contributions to the muon $g-2$ .



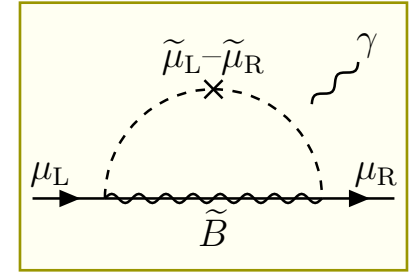
SUSY particles  
 $\tilde{\chi}^0$ : neutralino  
 $\tilde{\chi}^\pm$ : chargino  
 $\tilde{\mu}$ : smuon  
 $\tilde{\nu}_\mu$ : mu-sneutrino

mass insertion approx.

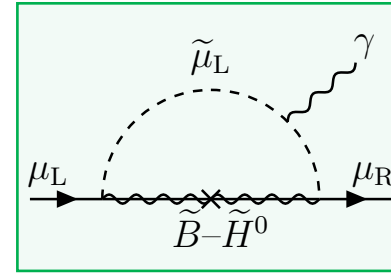
**WHL**



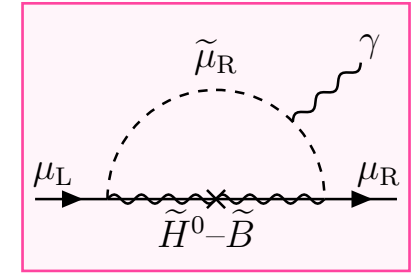
**BLR**



**BHL**

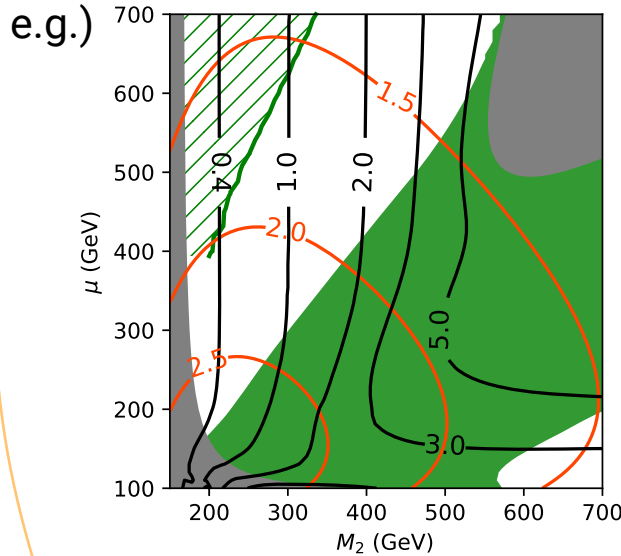


**BHR**



(cf. Cho et al. [1104.1769])

**Three\*** light particles = sufficient for  $g-2$ .



Left-handed slepton

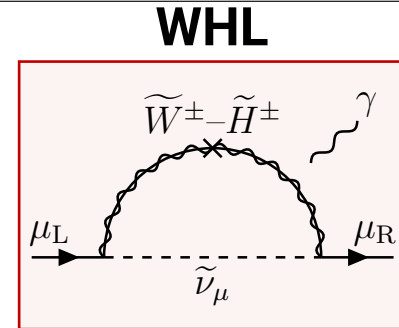
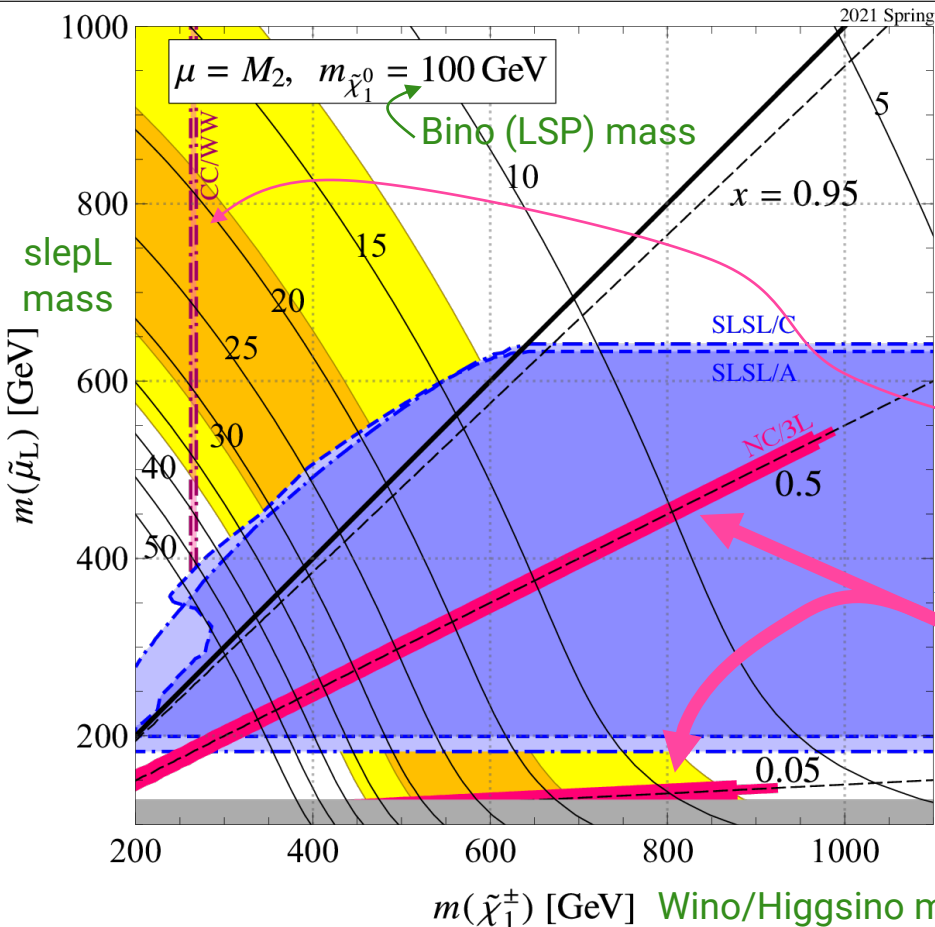
=  $\tilde{W}, \tilde{H}, \tilde{\nu} \sim \mathcal{O}(100) \text{ GeV}$  : "WHL scenario"

**→ What if Bino is also light?  
 (i.e., Bino-LSP with WHL?)**

\*In terms of gauge multiplets. Flavor universality is often assumed.

Hence  $\tilde{W}^\pm, \tilde{W}^0, \tilde{H}^\pm, \tilde{H}_{1,2}^0, \tilde{e}_L, \tilde{\mu}_L, \tilde{\tau}_L$ , and  $\tilde{\nu}_e, \tilde{\nu}_\mu, \tilde{\nu}_\tau$  are light here.

$$a_\mu^{\text{WHL}} = \frac{\alpha_2}{4\pi} \frac{m_\mu^2}{M_2 \mu} \tan \beta \cdot f_C \left( \frac{M_2^2}{m_{\tilde{\nu}_\mu}^2}, \frac{\mu^2}{m_{\tilde{\nu}_\mu}^2} \right) - \frac{\alpha_2}{8\pi} \frac{m_\mu^2}{M_2 \mu} \tan \beta \cdot f_N \left( \frac{M_2^2}{m_{\tilde{\mu}_L}^2}, \frac{\mu^2}{m_{\tilde{\mu}_L}^2} \right)$$

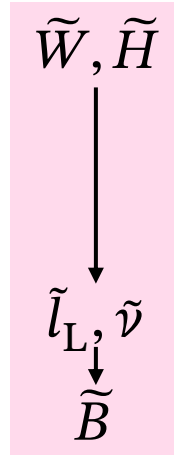


LHC constraints

- $\tilde{\mu}_L > \tilde{W}^\pm, \tilde{H}^\pm$ 
  - $\tilde{W}^+ \tilde{W}^- \rightarrow W^+ W^- \cancel{p}_T$  (CC/WW)
  - $\tilde{W}^0 \tilde{W}^+ \rightarrow ZW + \cancel{p}_T, HW + \cancel{p}_T$  (NC/HW, NC/ZW)
- $\tilde{\mu}_L < \tilde{W}^\pm, \tilde{H}^\pm$ 
  - $\tilde{\mu}_L \tilde{\mu}_L^* \rightarrow 2\mu + \cancel{p}_T$  (SLSL)
  - $\tilde{W}^0 \tilde{W}^+ \rightarrow (\mu \tilde{\mu}_L)(\mu \tilde{\nu}) \rightarrow 3\mu + \cancel{p}_T$  (NC/3L)

Bino-stau coannihilation works if  $m(\tilde{B}) \simeq m(\tilde{\tau})$  ... excluded by NC/3L.

N.B. Exclusions at the "obviously 95%-CL excluded" criterion.  
Slepton universality is assumed.



Masses set at low energy,  
 $\mu = M_2, \tan\beta = 40, \tilde{\chi}_1^0 = 100 \text{ GeV}, A_{u,d,e} = 0,$   
right-handed sleptons, squarks, gluinos, extra Higgses  $\gg 1 \text{ TeV}.$

SLSL: ATLAS [1908.08215], CMS [2012.08600].  
CC/WW: ATLAS [1909.09226].  
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Results to be analyzed: [2106.01676], [2108.07586].



## SUSY now: DM and muon $g-2$

### 1. DM $\Leftrightarrow g-2$ : tightly connected in MSSM

- $\tilde{W}$ -LSP &  $g-2$  = partial DM + LHC constraints
- $\tilde{H}$ -LSP &  $g-2$  = partial DM + direct det. constraints
- $\tilde{B}$ -LSP &  $g-2$  = too much DM + LHC constraints

extra DM?  
non-simple cosmology?

coannihilation?  
non-simple cosmology?

### 2. MSSM provides 4 scenarios for $g-2$ .

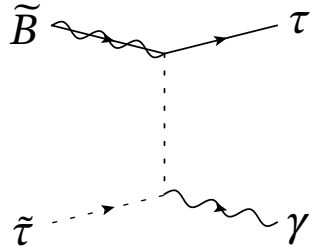
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2. BLR: Coannihil.  $\tilde{B}$ -DM
3. BHL/R:

### 3. Conclusion

**BLR scenario works well with coannihilation bino DM.**

$(\tilde{e}_L, \tilde{\nu}_e), (\tilde{\mu}_L, \tilde{\nu}_\mu), (\tilde{\tau}_L, \tilde{\nu}_\tau), \tilde{e}_R, \tilde{\mu}_R, \tilde{\tau}_R$ , and  $\tilde{B}$  are light.

Bino-stau coannihilation ← LSP (DM)



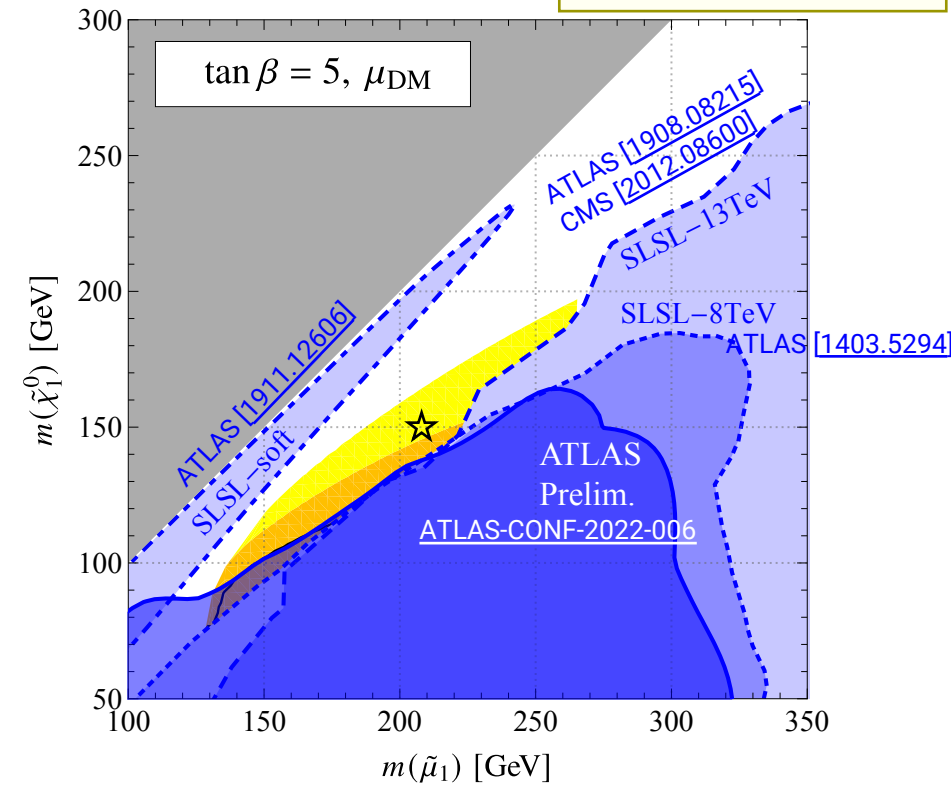
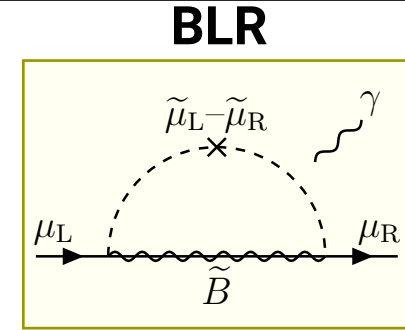
works if  $m(\tilde{B}) \simeq m(\tilde{\tau})$   
(degenerate/compressed spectra).

... Elusive@LHC. (→ ILC searches)

(or, see Beresford, Liu [1811.06465])

A benchmark point ☆ :

$\tilde{\tau}_2$ : 242 GeV	$\mu$ : 1922 GeV
$\tilde{\mu}_2, \tilde{e}_2$ : 207 GeV	$\tan \beta$ : 5
$\tilde{\mu}_1, \tilde{e}_1$ : 202 GeV	$a_\mu^{\text{SUSY}}$ : $1.7 \times 10^{-9}$
$\tilde{\nu}_{e,\mu,\tau}$ : 190 GeV	$(\Omega h^2)_{\text{bino}}$ : 0.12
$\tilde{\tau}_1$ : 159 GeV	
$\tilde{B}$ : 150 GeV	



$(\Omega h^2)_{\text{bino LSP}} = (\Omega h^2)_{\text{DM}}^{\text{obs}}$   
on the whole plane (by tuned  $\mu$ -parameter).

**Reminder:** Prices for bino DM

= Avoid LHC && (DM reduction mechanism || non-simple cosmology)

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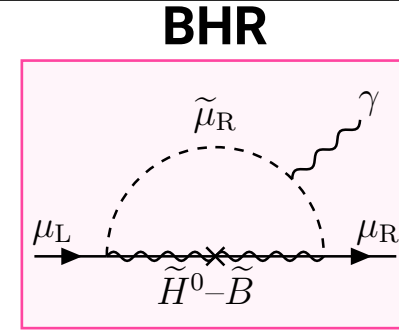
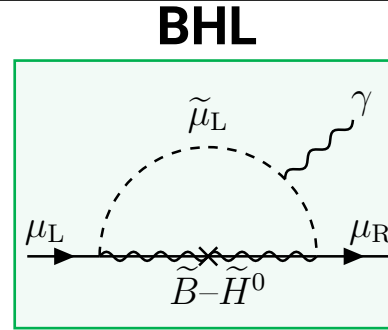
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2. BLR: Coannihil.  $\tilde{B}$ -DM = compressed ... still alive.
3. BHL/R:

→ ee colliders.  
 $ee \rightarrow \tilde{\ell}\tilde{\ell}$

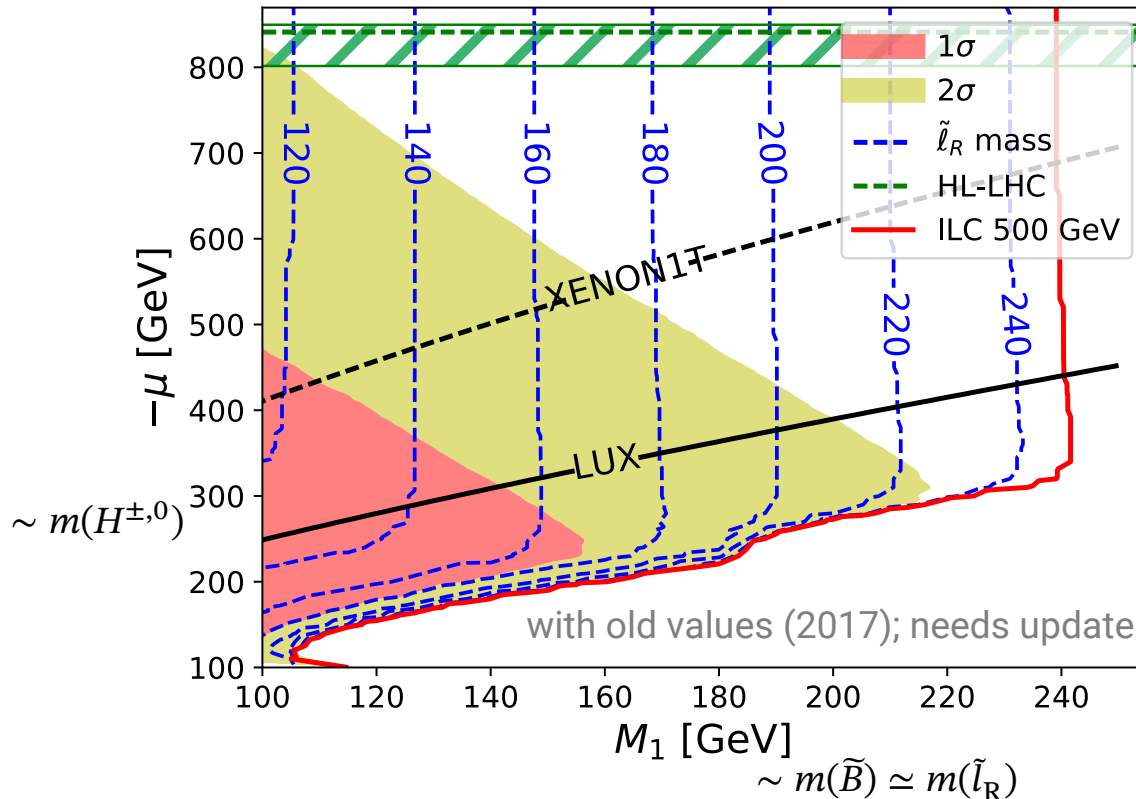
### 3. Conclusion

$\tilde{B}, \tilde{H}$ , and  $(\tilde{l}_L \text{ or } \tilde{l}_R)$  are light. ←

- ❖  $\tilde{H}$ -DM
  - ❖ mixed DM
  - ❖  $\tilde{B}$ -DM → Needs reduction ... Bino-stau coannihilation [ $m(\tilde{B}) \simeq m(\tilde{\tau})$ ]?
- partial DM or direct detection



➤ BHR plane with coannihilation DM



$$\tilde{B}, \tilde{l}_R < \tilde{H}$$

100–200 GeV      200–800 GeV

**Whole region will be explored by**

- DM direct detection,
- HL-LHC  
( $pp \rightarrow \tilde{H}^+ \tilde{H}^0 \rightarrow 2\tau + \cancel{p}_T$ ),
- ILC slepton searches.

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Coannihil.  $\tilde{B}$ -DM ... still alive. → direct det., HL-LHC, ee colliders.

$2\tau + \cancel{p}_T$      $ee \rightarrow \tilde{\ell}\tilde{\ell}$

### 3. Conclusion

Bad news to me: Non-discovery of non-colored SUSY particles @ LHC Run 2.

## ■ DM $\Leftrightarrow g-2$ : tightly connected in MSSM

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# Conclusion

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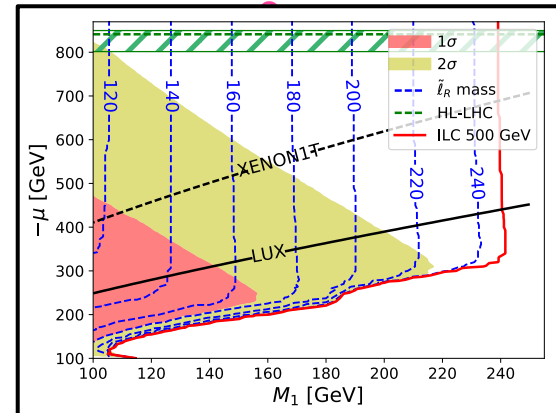
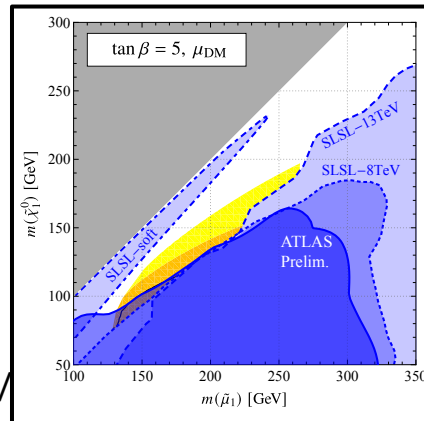
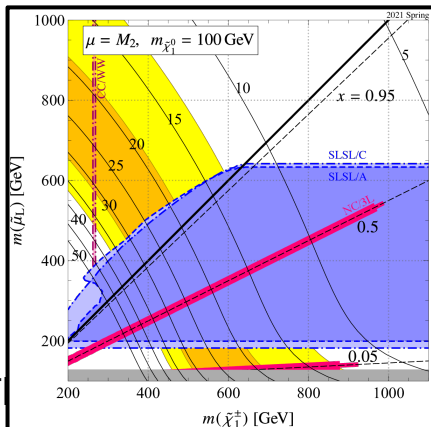
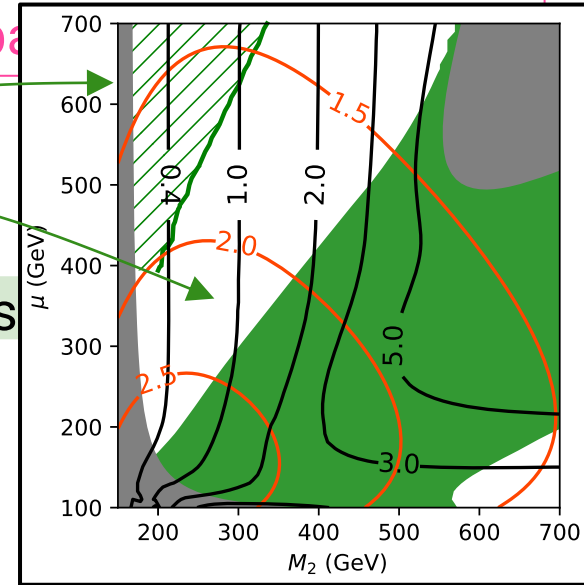
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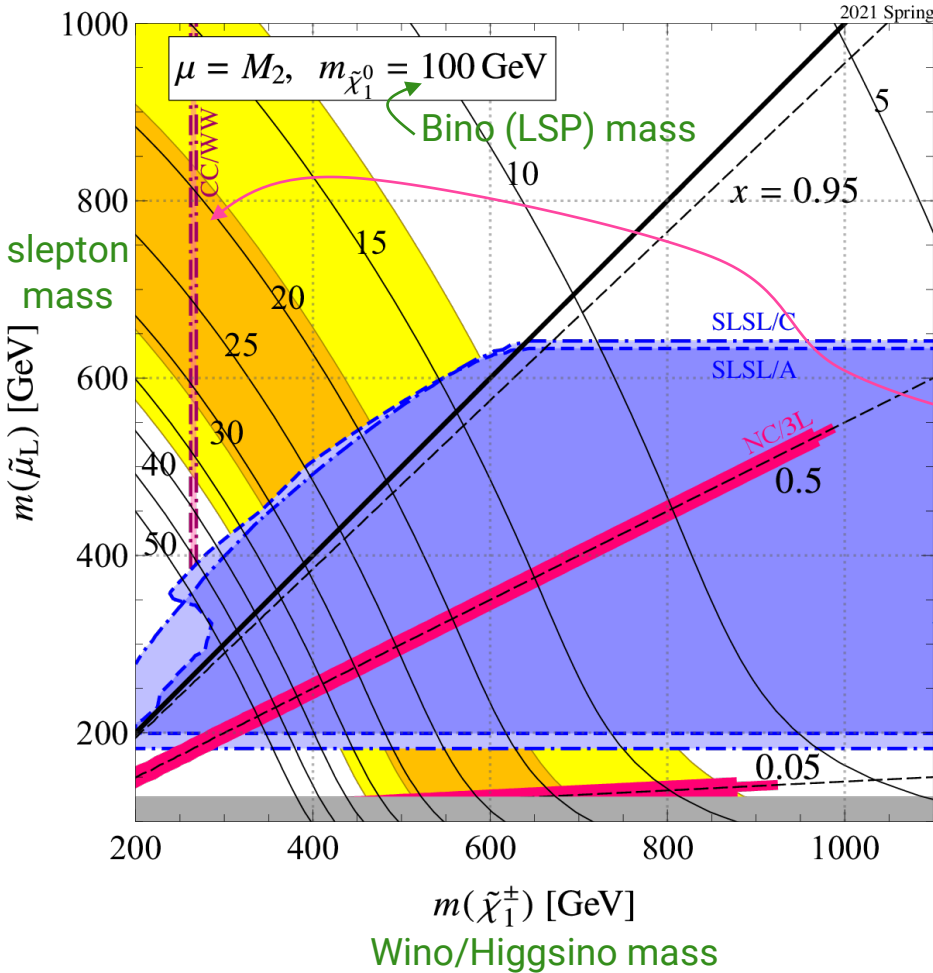
BHL/R:  $\tilde{B}$ - $\tilde{H}$  mixed DM ...  $\otimes$  direct det.

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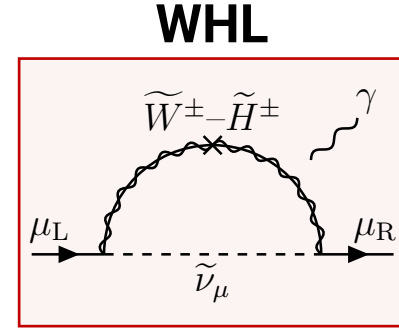


**One topic I omitted from  
the mainstream of the talk**





Various constraints @ LHC!



- $\tilde{\mu}_L > \tilde{W}^\pm, \tilde{H}^\pm$ 
  - $\tilde{W}^+ \tilde{W}^- \rightarrow W^+ W^- \cancel{p}_T$  (CC/WW)
  - $\tilde{W}^0 \tilde{W}^\pm \rightarrow ZW + \cancel{p}_T, HW + \cancel{p}_T$  (NC/HW, NC/ZW)
- $\tilde{\mu}_L < \tilde{W}^\pm, \tilde{H}^\pm$ 
  - $\tilde{\mu}_L \tilde{\mu}_L^* \rightarrow 2\mu + \cancel{p}_T$  (SLSL)
  - $\tilde{W}^0 \tilde{W}^\pm \rightarrow (\mu \tilde{\mu}_L)(\mu \tilde{\nu}) \rightarrow 3\mu + \cancel{p}_T$  (NC/3L)

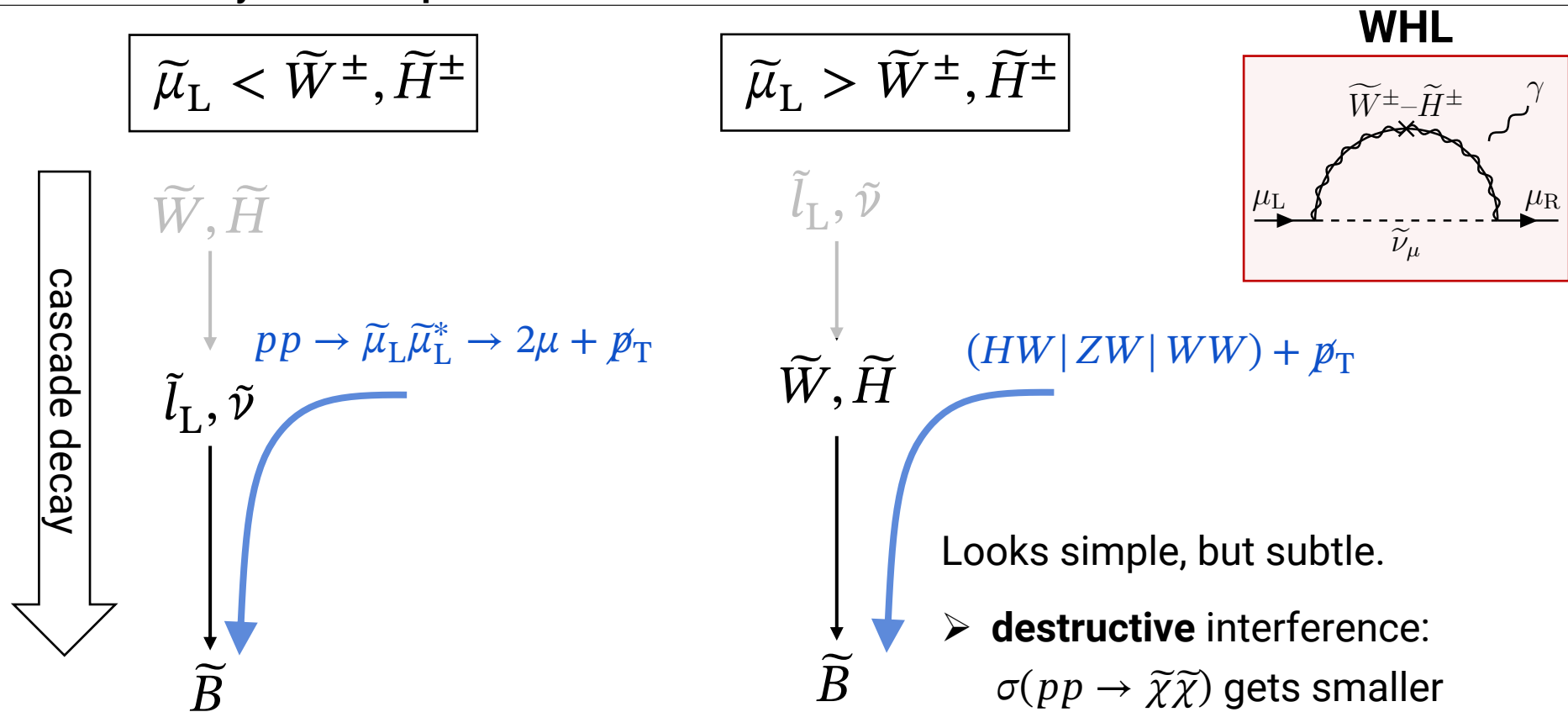
(a bit of details in the next slide)

Stringent for  $\mu_L < \tilde{W}^\pm, \tilde{H}^\pm$ .

N.B. Exclusions at the "obviously 95%-CL excluded" criterion.

Masses set at low energy,  
 $\mu = M_2, \tan \beta = 40, \tilde{\chi}_1^0 = 100 \text{ GeV}, A_{u,d,e} = 0,$   
 right-handed sleptons, squarks, gluinos, extra Higgses  $\gg 1 \text{ TeV}.$

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 Results to be analyzed: [2106.01676, 2108.07586].



Even though  $\sigma(pp \rightarrow \tilde{\mu}_L \tilde{\mu}_L^*) \ll \sigma(pp \rightarrow \tilde{W} \tilde{W})$ ,  
large luminosity in Run 2

→ **silver bullet** to kill models with  
 $\tilde{\mu}_L < \tilde{W}^\pm, \tilde{H}^\pm$

(but not coannihil. region  
→ next slide)

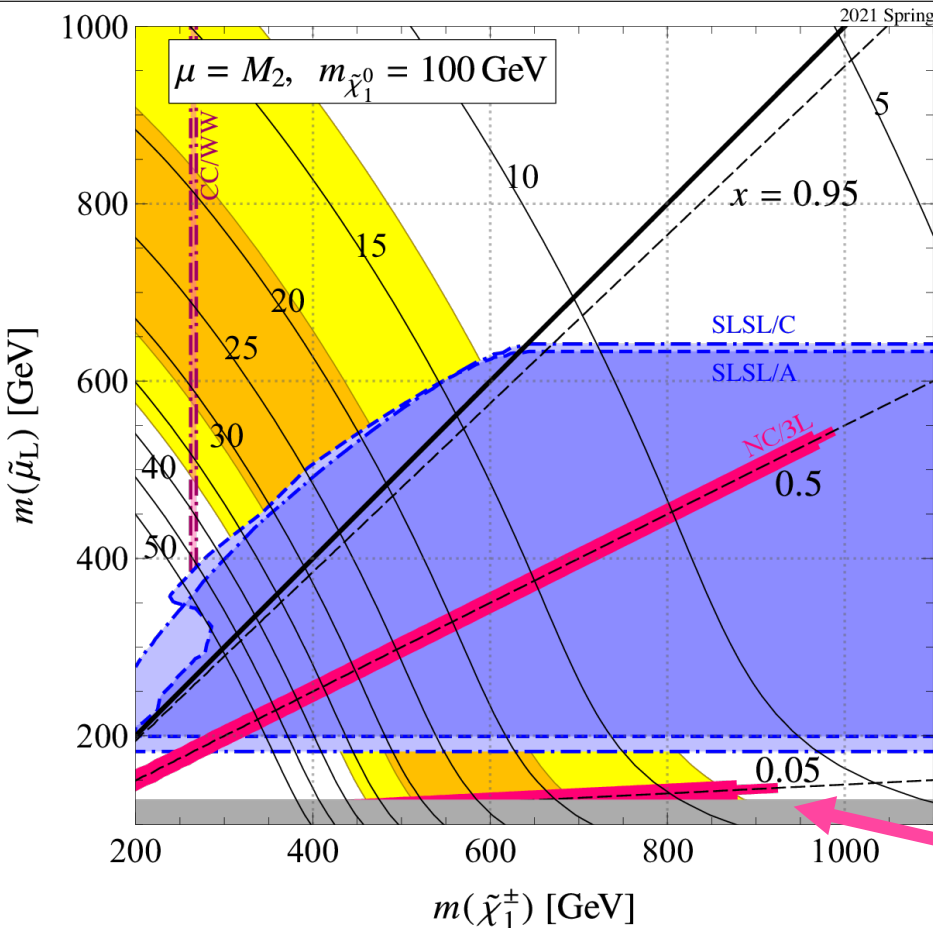
Looks simple, but subtle.

- **destructive** interference:  
 $\sigma(pp \rightarrow \tilde{\chi} \tilde{\chi})$  gets smaller  
if squarks are not decoupled.

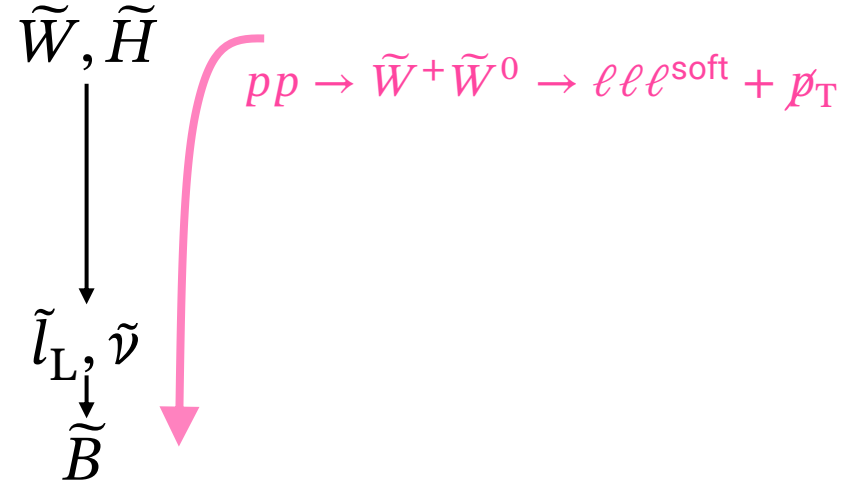
Liu, McGinnis, Wagner, Wang [2008.11847]

- multiple types of final states:  
needs to combine HW + ZW.  
(cf. ATLAS [2108.07586])

→ **yet to discuss/analyze.**



## WHL + coannihil. $\tilde{B}$ -DM



- $\tilde{\mu}_L < \tilde{W}^\pm, \tilde{H}^\pm$

$$\tilde{\mu}_L \tilde{\mu}_L^* \rightarrow 2\mu + \cancel{p}_T \quad (\text{SLSL})$$

$$\tilde{W}^0 \tilde{W}^+ \rightarrow (\mu \tilde{\mu}_L)(\mu \tilde{\nu}) \rightarrow 3\mu + \cancel{p}_T \quad (\text{NC/3L})$$

-----> Coannihilation region looks dead : **WHL & DM = difficult.**

Masses set at low energy,  
 $\mu = M_2$ ,  $\tan \beta = 40$ ,  $\tilde{\chi}_1^0 = 100 \text{ GeV}$ ,  $A_{u,d,e} = 0$ ,  
 right-handed sleptons, squarks, gluinos, extra Higgses  $\gg 1 \text{ TeV}$ .

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