

# MSSM 4G<sup>📶</sup> scenario

Sho IWAMOTO (岩本 祥)

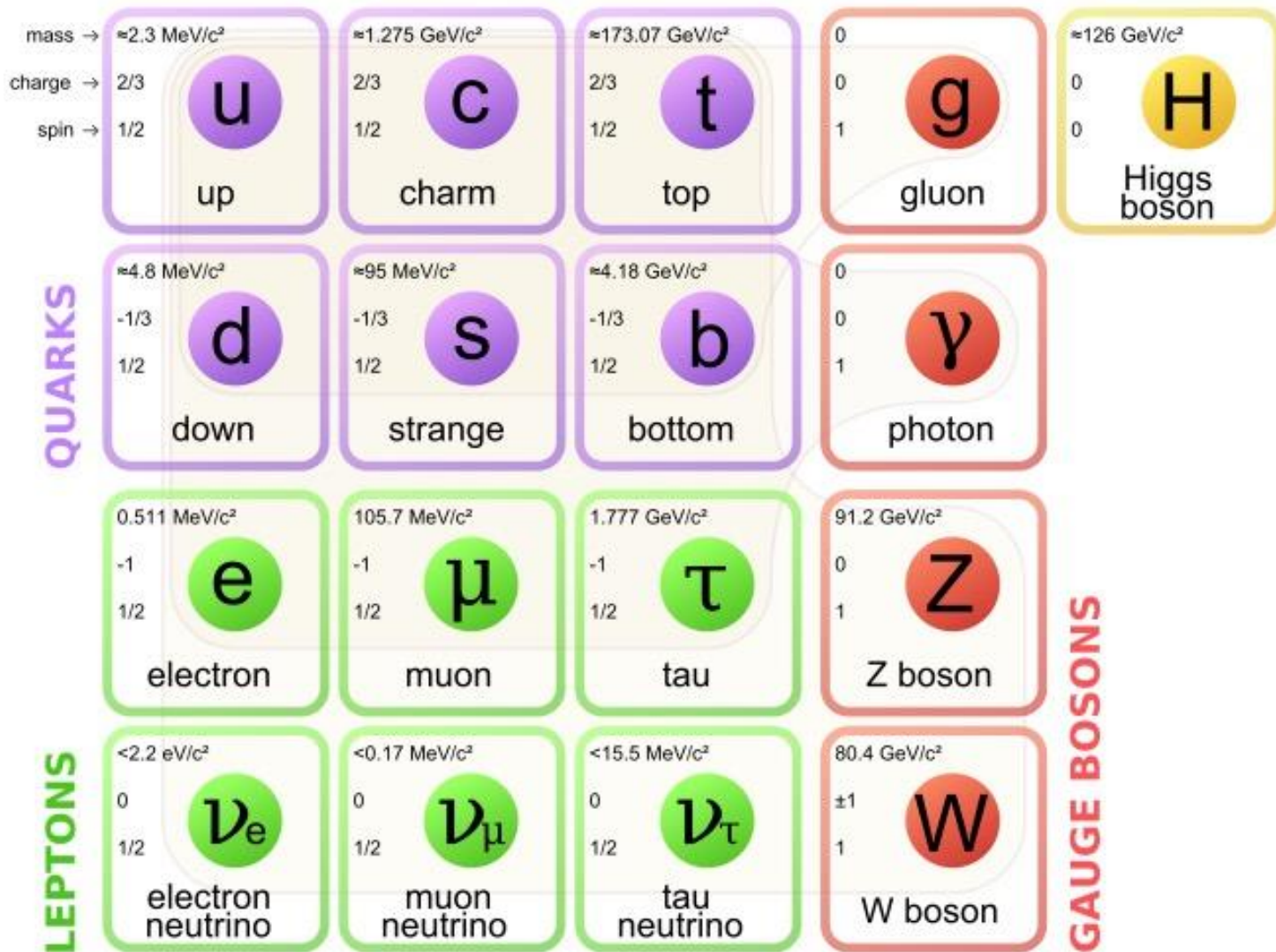
7 Nov. 2016

HEP phenomenology joint Cavendish–DAMTP seminar @ U. Cambridge

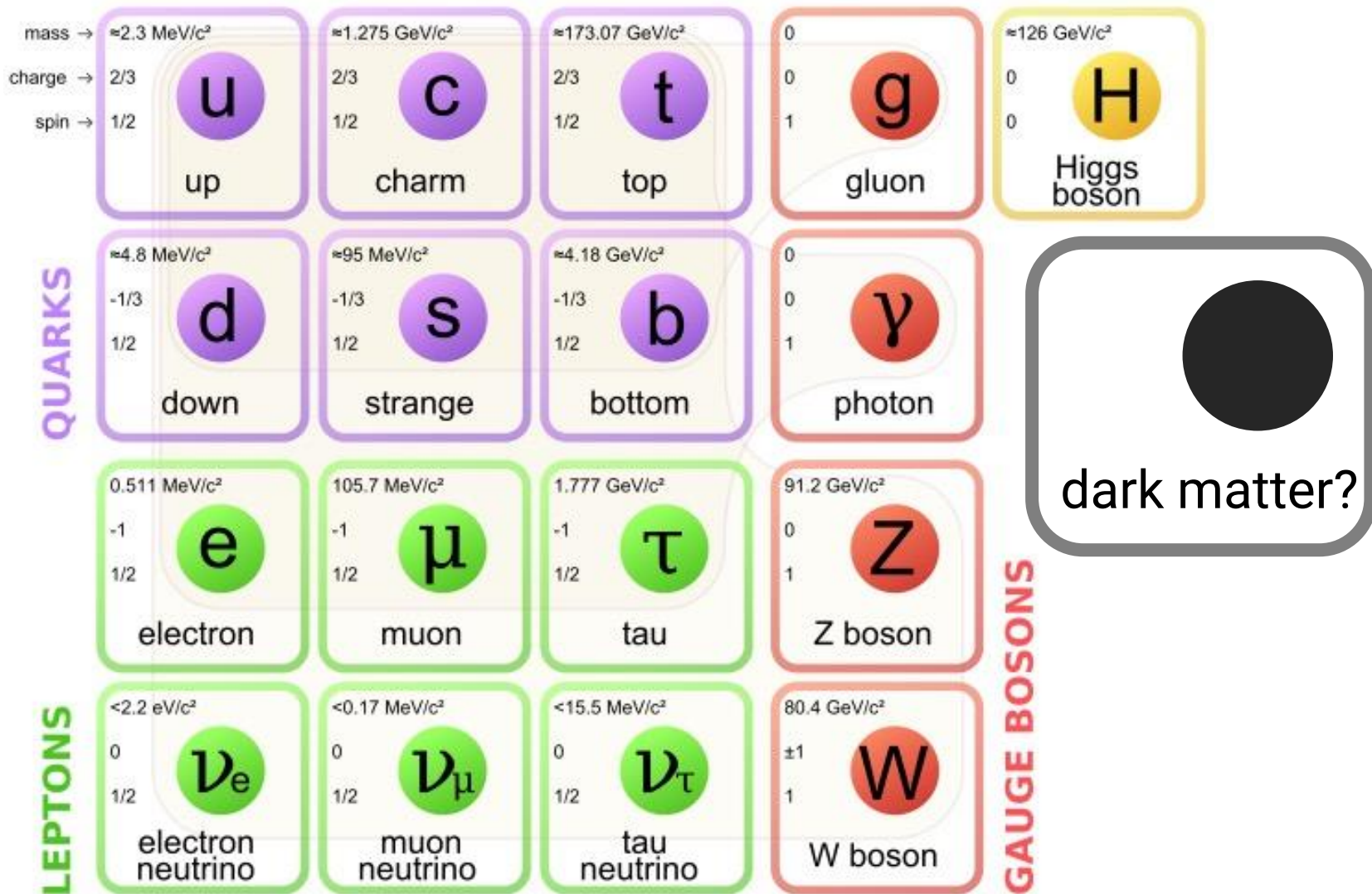
Based on [[1608.00283](#)] in collaboration with  
**M. Abdullah, J. L. Feng, and B. Lillard** (UC Irvine)

# The Standard Model of Particle Physics

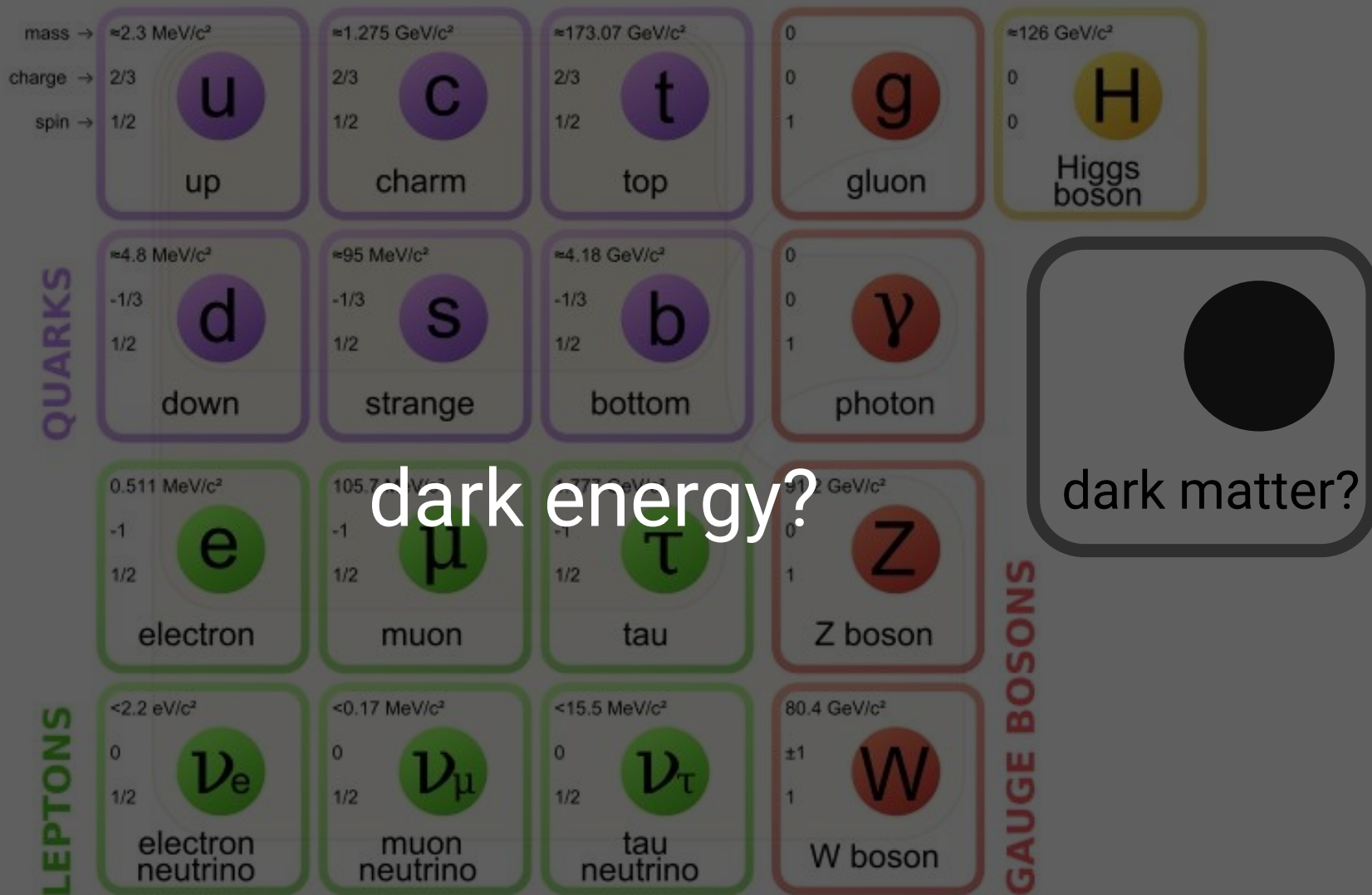
Universe =



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### Hints of “New Physics”

- Dark matter
- Dark energy
- Neutrino mass
- Gauge coupling unification
- Higgs mass (“naturalness”)
- Muon “ $g - 2$ ”
- ...

## New Physics Candidates

- 
- 
- 
- 

etc...

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- SUSY [supersymmetry]
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- etc...

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- SUSY [supersymmetry]



Please fill this list  
with your models  
/ models you like



etc...

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## New Physics Candidates

- SUSY [supersymmetry]
- Gauge-Higgs unification
- Hidden strong  $SU(N)$
- etc...

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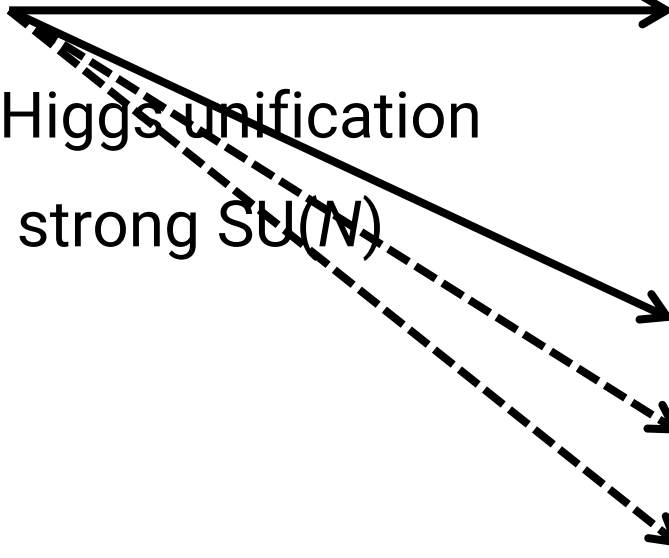
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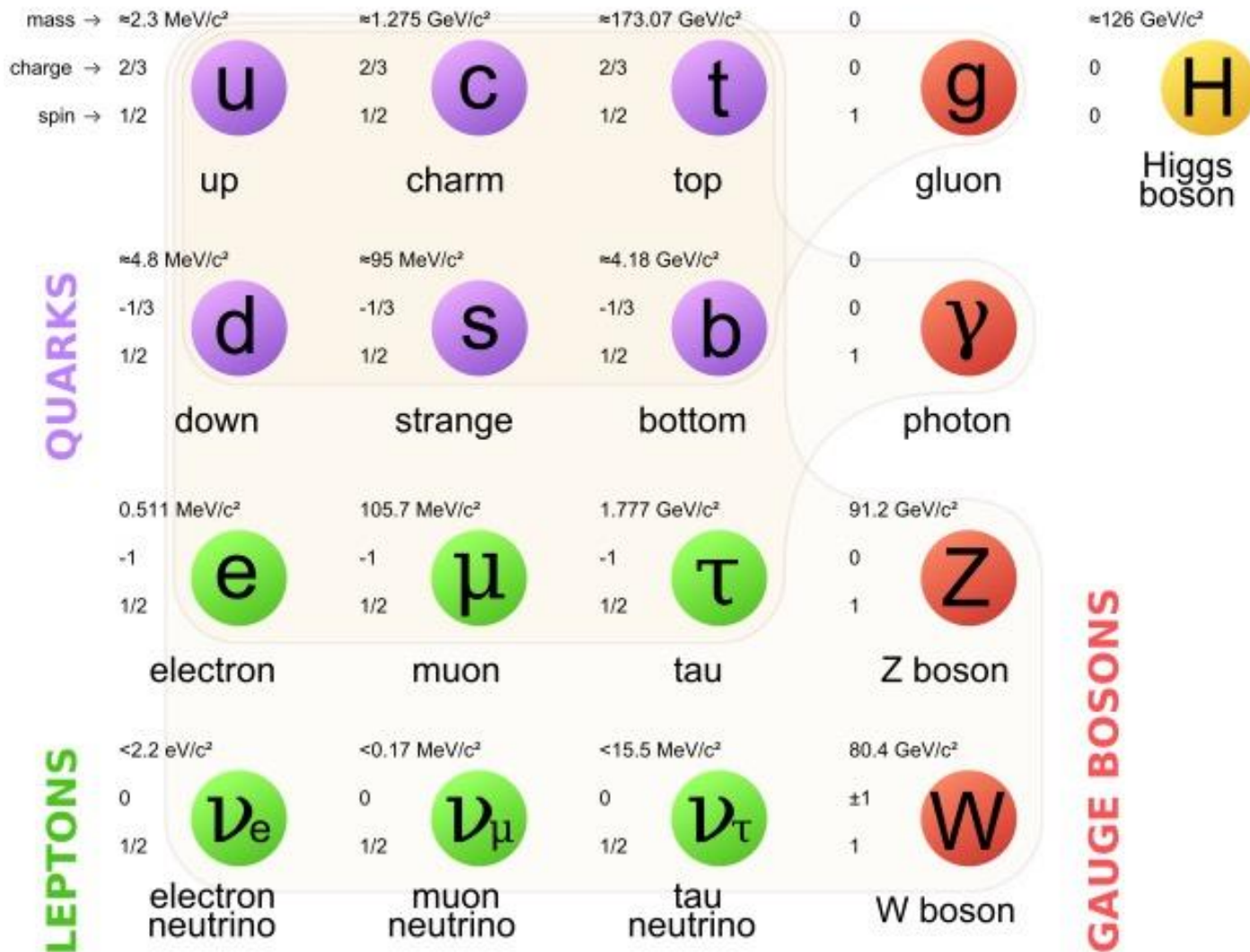
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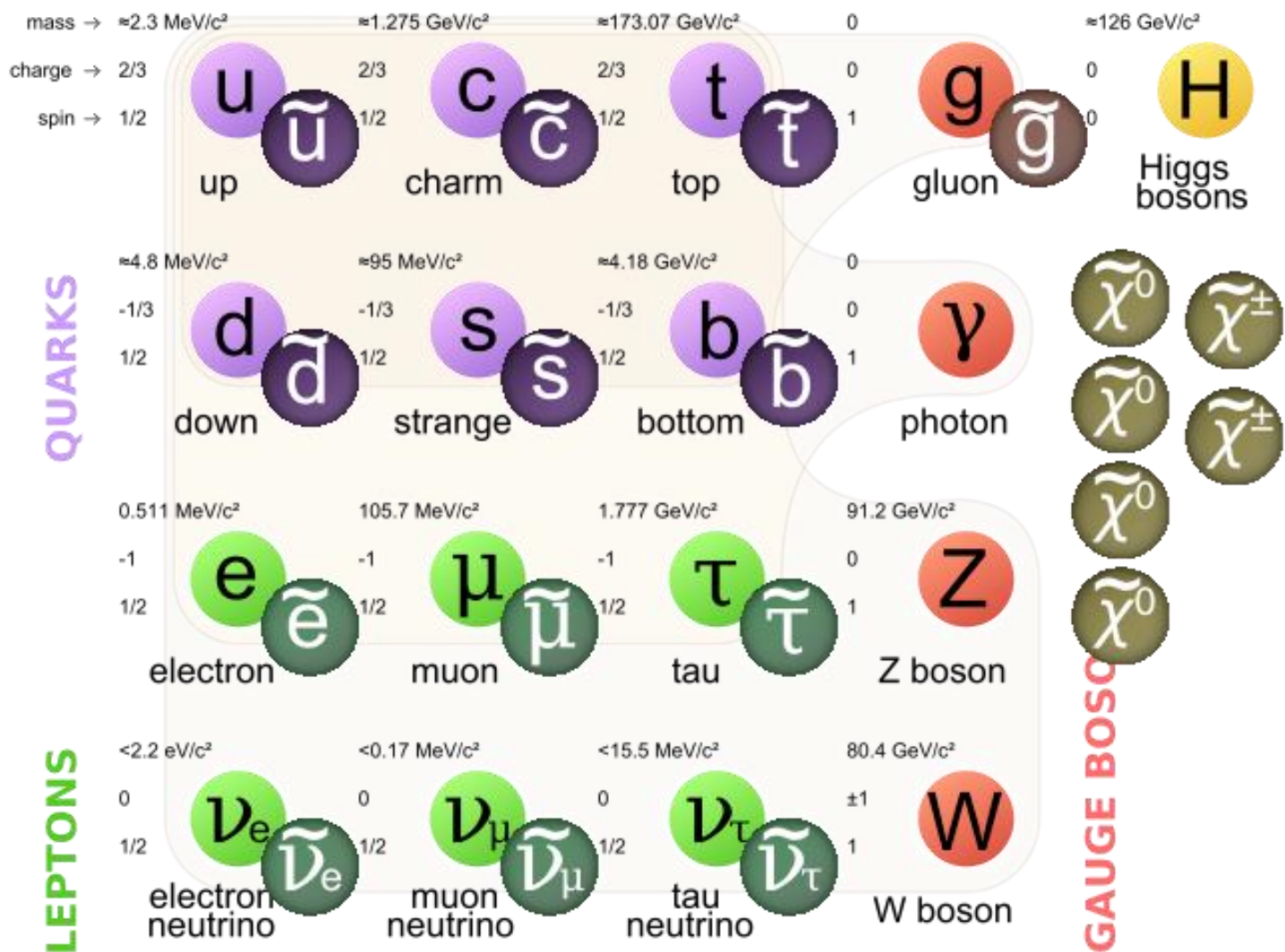


■ SM =



## ■ MSSM =

[Minimal Supersymmetric Standard Model]



## New Physics Candidates

■ SUSY

## Hints of “New Physics”

■ Dark matter

■ Dark energy

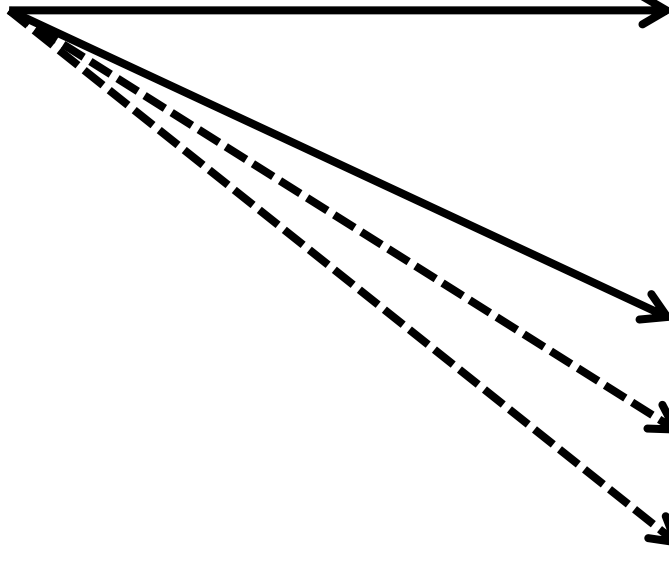
■ Neutrino mass

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## New Physics Candidates

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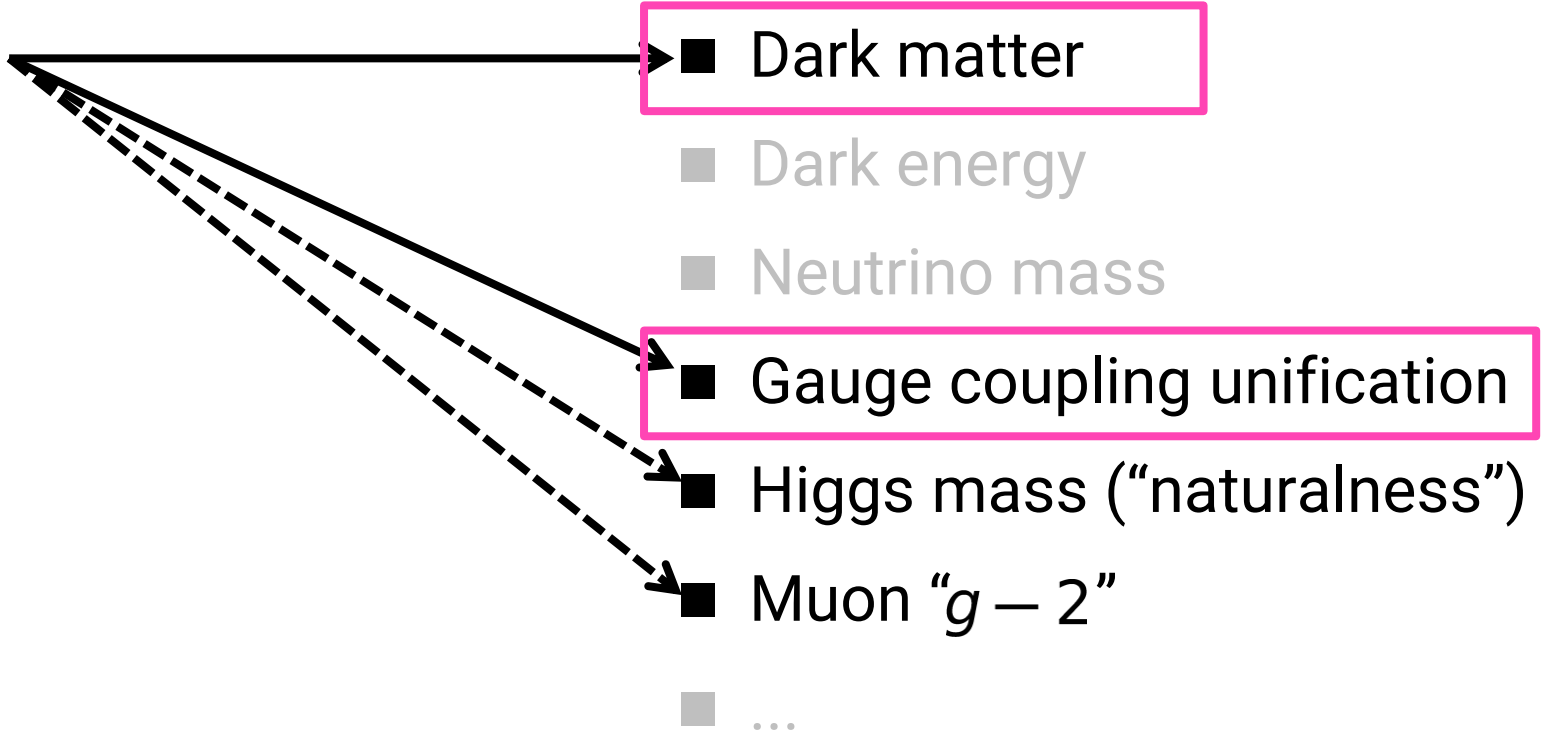
■ Neutrino mass

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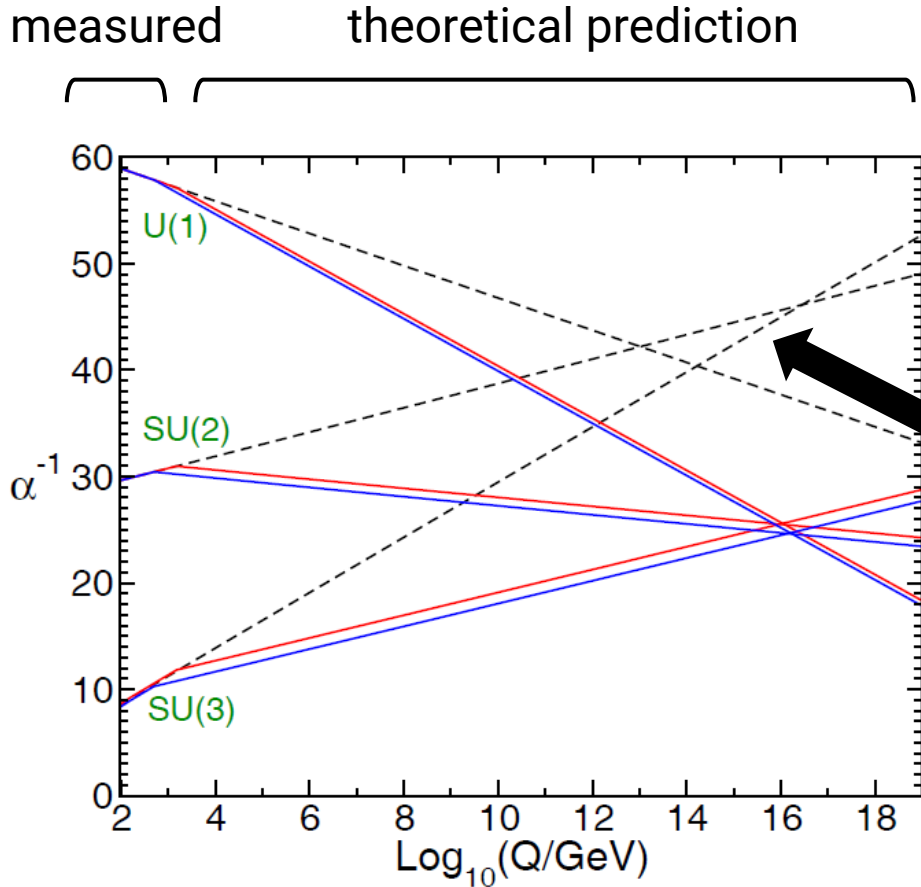
■ Muon “ $g - 2$ ”

■ ...



# Gauge coupling unification

- SM  $\ni$  3 forces : U(1), SU(2), SU(3) [Why three?]



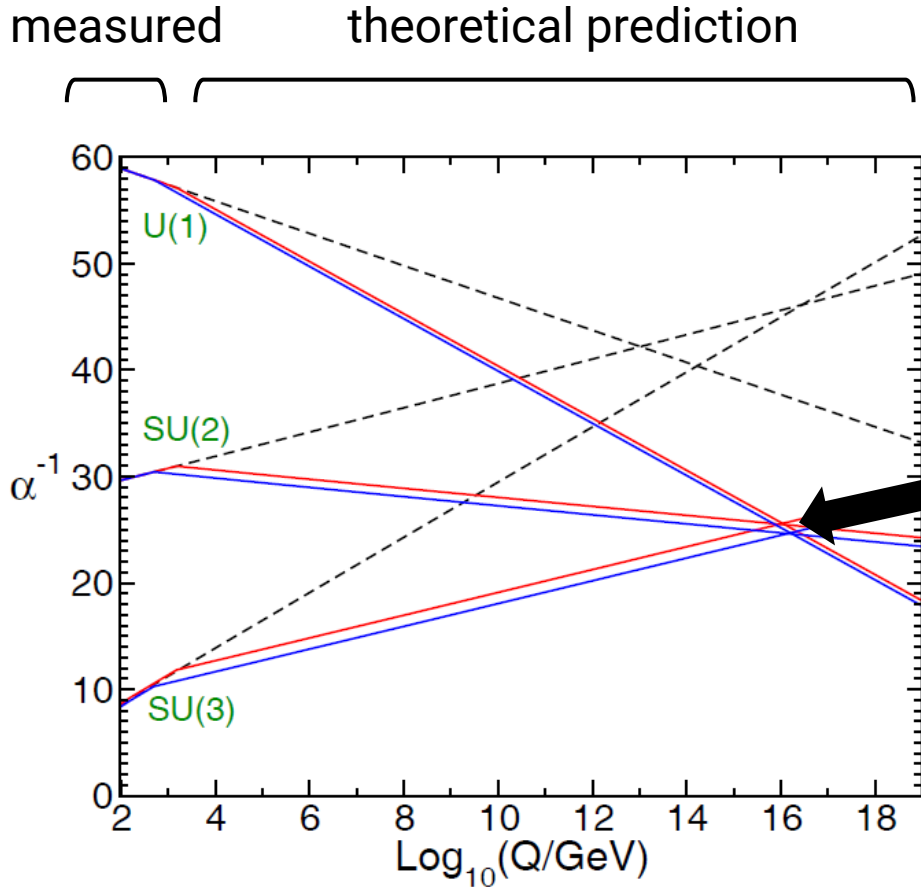
## Gauge coupling unification

	mass $\rightarrow$ $\approx 2.3 \text{ MeV}/c^2$	$\approx 1.275 \text{ GeV}/c^2$	$\approx 173.07 \text{ GeV}/c^2$	0	$\approx 126 \text{ GeV}/c^2$
charge $\rightarrow$ 2/3	u	c	t	g	H
spin $\rightarrow$ 1/2	up	charm	top	gluon	Higgs boson
	$\approx 4.8 \text{ MeV}/c^2$	$\approx 95 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$	0	0
charge $\rightarrow$ -1/3	d	s	b	$\gamma$	
spin $\rightarrow$ 1/2	down	strange	bottom	photon	
	$0.511 \text{ MeV}/c^2$	$105.7 \text{ MeV}/c^2$	$1.777 \text{ GeV}/c^2$	$91.2 \text{ GeV}/c^2$	
charge $\rightarrow$ -1	e	$\mu$	$\tau$	Z	
spin $\rightarrow$ 1/2	electron	muon	tau	Z boson	
	$< 2.2 \text{ eV}/c^2$	$< 0.17 \text{ MeV}/c^2$	$< 15.5 \text{ MeV}/c^2$	$80.4 \text{ GeV}/c^2$	
charge $\rightarrow$ 0	$\nu_e$	$\nu_\mu$	$\nu_\tau$	W	
spin $\rightarrow$ 1/2	electron neutrino	muon neutrino	tau neutrino	W boson	

Figure from S. P. Martin, *A Supersymmetry Primer*, [hep-ph/9709356](http://hep-ph/9709356)

# Gauge coupling unification

- SM  $\ni$  3 forces : U(1), SU(2), SU(3) [Why three?]



## Gauge coupling unification

Particle	mass $\rightarrow$	charge $\rightarrow$	spin
<b>QUARKS</b>			
up ( $u$ )	$\approx 2.3 \text{ MeV}/c^2$	$2/3$	$1/2$
charm ( $c$ )	$\approx 1.275 \text{ GeV}/c^2$	$2/3$	$1/2$
top ( $t$ )	$\approx 173.07 \text{ GeV}/c^2$	$2/3$	$1/2$
down ( $d$ )	$\approx 4.8 \text{ MeV}/c^2$	$-1/3$	$1/2$
strange ( $s$ )	$\approx 95 \text{ MeV}/c^2$	$-1/3$	$1/2$
bottom ( $b$ )	$\approx 4.18 \text{ GeV}/c^2$	$-1/3$	$1/2$
gluon ( $g$ )	0	0	1
photon ( $\gamma$ )	0	0	1
Z boson	91.2 $\text{ GeV}/c^2$	0	1
W boson	80.4 $\text{ GeV}/c^2$	$\pm 1$	1
Higgs bosons ( $H$ )	$\approx 126 \text{ GeV}/c^2$	0	0
<b>LEPTONS</b>			
electron ( $e$ )	$0.511 \text{ MeV}/c^2$	$-1$	$1/2$
muon ( $\mu$ )	$105.7 \text{ MeV}/c^2$	$-1$	$1/2$
tau ( $\tau$ )	$1.777 \text{ GeV}/c^2$	$-1$	$1/2$
electron neutrino ( $\nu_e$ )	$< 2.2 \text{ eV}/c^2$	0	$1/2$
muon neutrino ( $\nu_\mu$ )	$< 0.17 \text{ MeV}/c^2$	0	$1/2$
tau neutrino ( $\nu_\tau$ )	$< 15.5 \text{ MeV}/c^2$	0	$1/2$
<b>GAUGE BOSONS</b>			
Neutralinos ( $\tilde{\chi}^0$ )			0
Charginos ( $\tilde{\chi}^\pm$ )			$\pm 1$

Figure from S. P. Martin, *A Supersymmetry Primer*, [hep-ph/9709356](http://hep-ph/9709356)

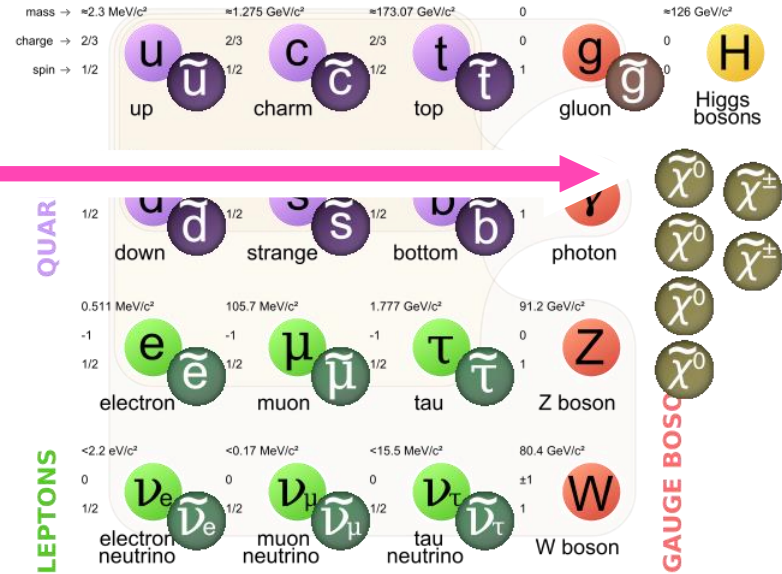


■ MSSM  $\ni$  Dark matter candidate



■ Dark matter?

- stable (at least  $10^{10}$  yr)
- charge neutral
- density  $\Omega h^2 = 0.12$
- not detected by astrophysics / direct search / LHC



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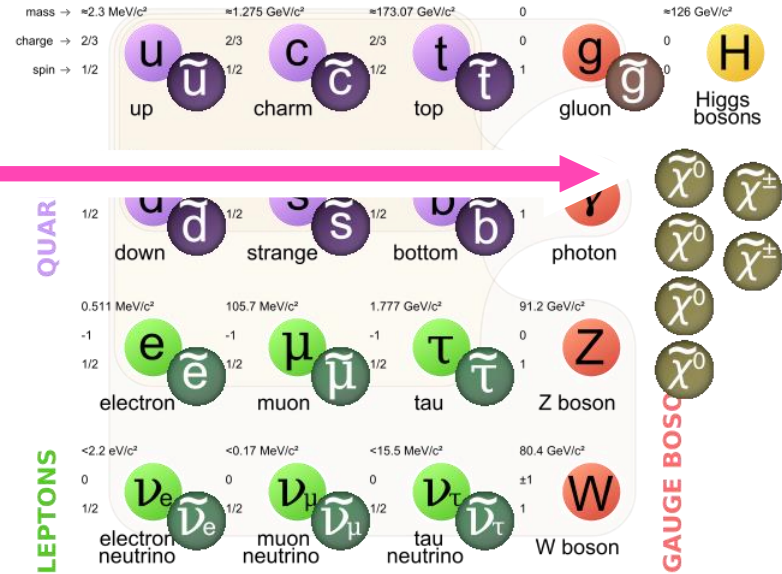
*if we introduce R-parity*

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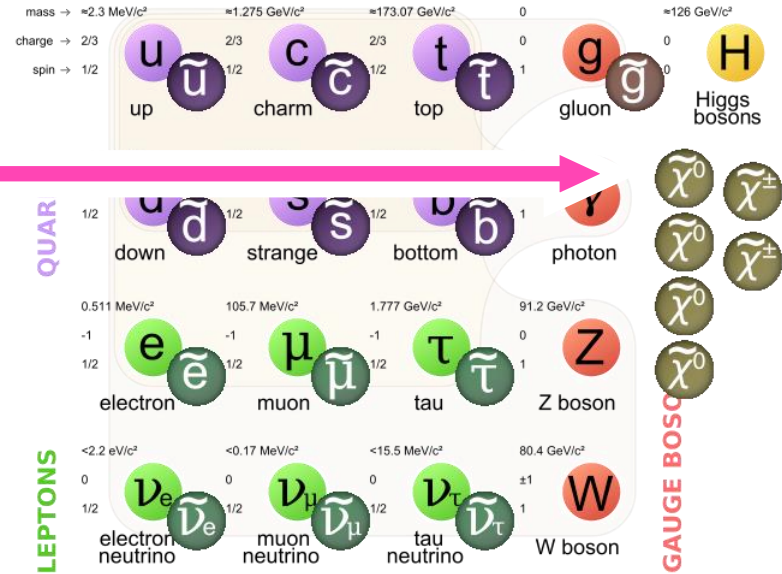
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$$\tilde{\chi}^0 = \tilde{B} \oplus \tilde{W}^0 \oplus \tilde{H}_d^0 \oplus \tilde{H}_u^0$$

- $\tilde{B}$ -like?

→ “overabundant” problem

- $\tilde{W}$ -like?

$$\Omega h^2 \gg 0.12$$

- $\tilde{H}$ -like?

$$\tilde{\chi}^0 = \tilde{B} \oplus \tilde{W}^0 \oplus \tilde{H}_d^0 \oplus \tilde{H}_u^0$$

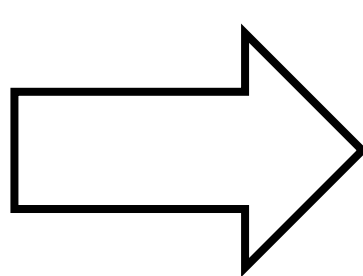
•  $\tilde{B}$ -like?

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**MSSM 4G<sup>📶</sup> model**

**Introduction:** why overabundant?

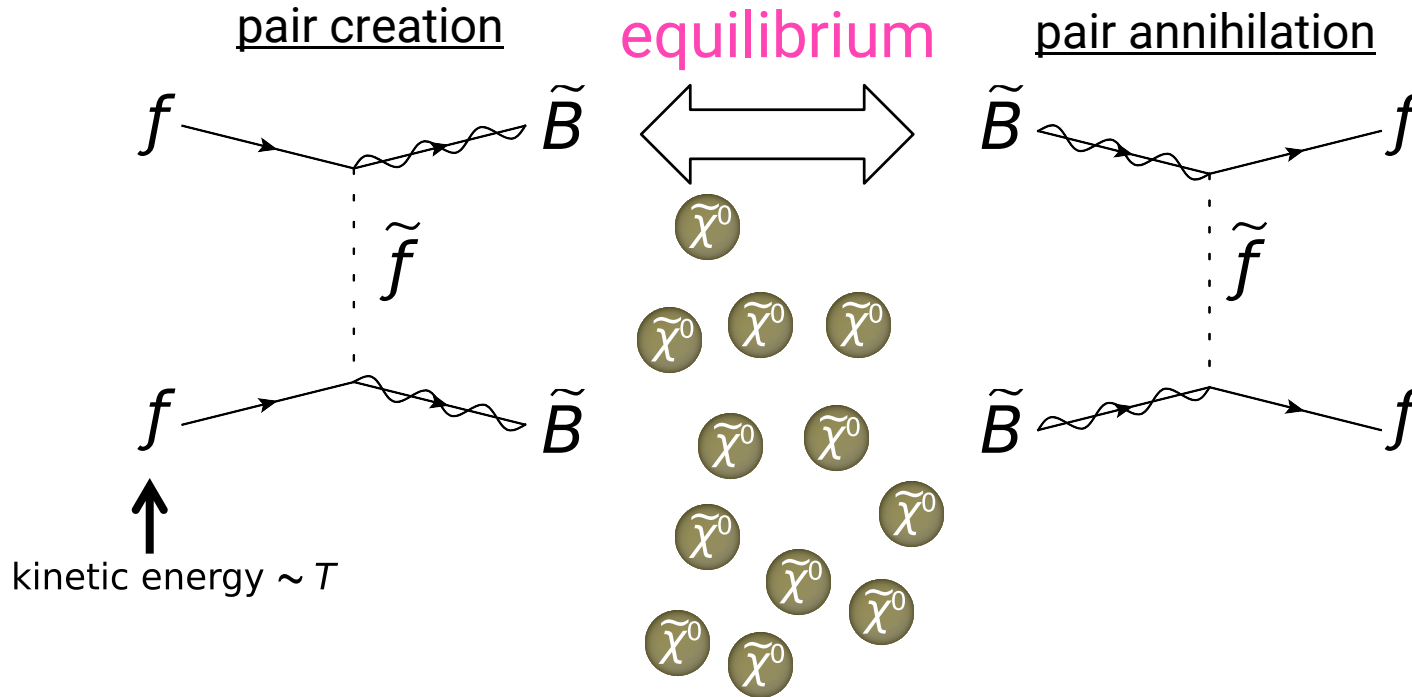
**Model:** **MSSM4G**  solves overabundance.

**Analysis:**

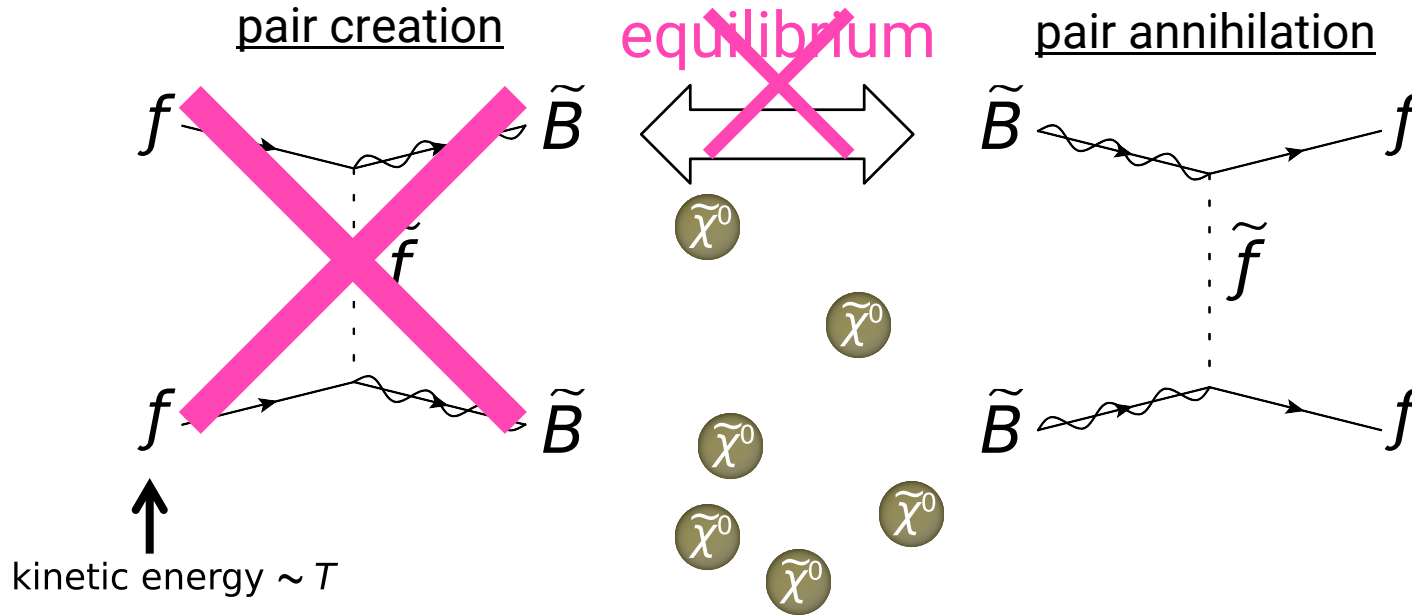
- cosmic rays (CTA, Fermi, MAGIC)
- colliders (LHC)
- direct detection (LUX)

**Summary** with discussion seeds

■ Early Universe with  $T > m_{\tilde{B}}$



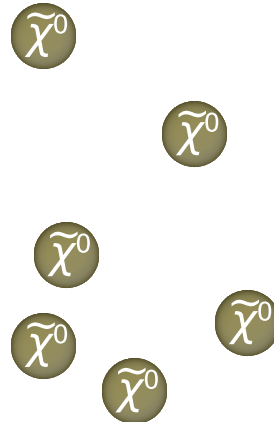
■ Early Universe with  $T \lesssim m_{\tilde{B}}$





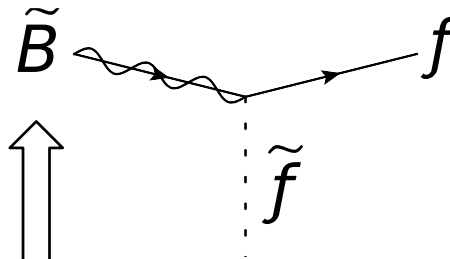
## ■ Early Universe with $T \lesssim m_{\tilde{B}}/20$

pair creation



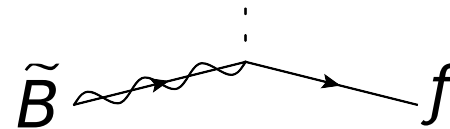
**“relic density”**

pair annihilation



far apart due to

- pair annihilation
- Universe's expansion



■ “observed” relic density  $\Omega h^2$

← “proper” crosssection  $\langle \sigma v \rangle$  of  $(DM)(DM) \rightarrow SM$

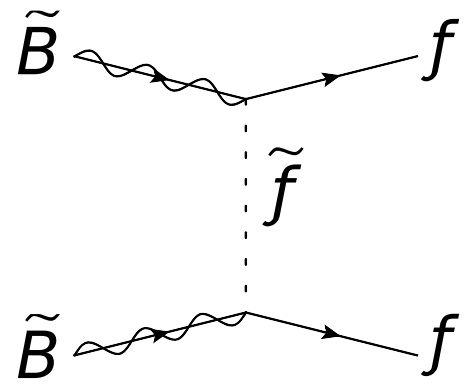
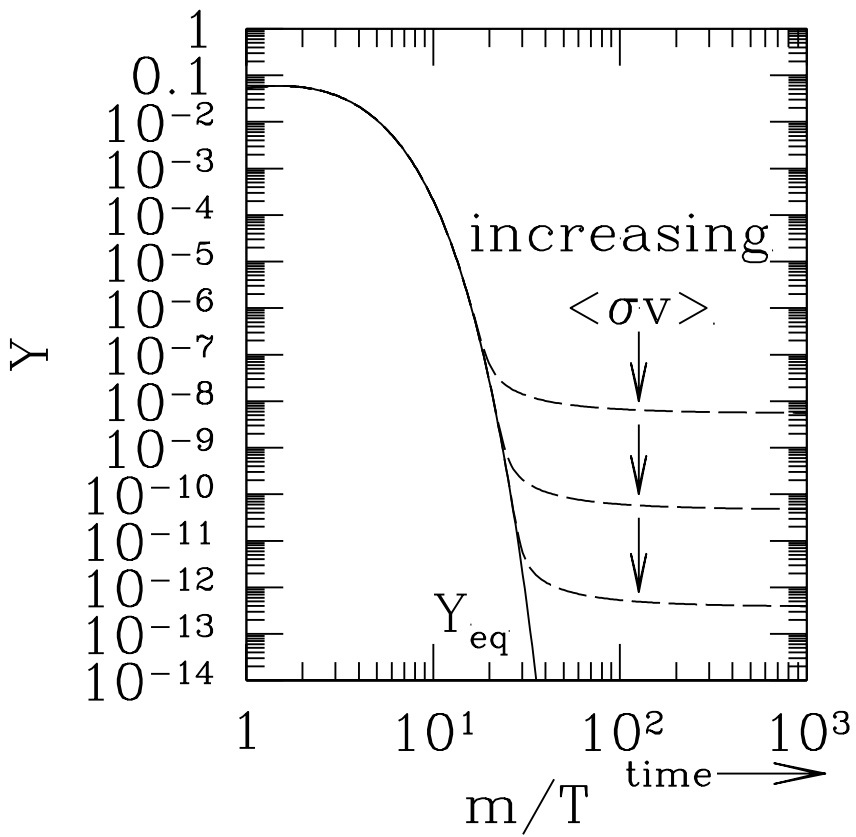


Figure from Gelmini and Gondolo, [1009.3690](https://arxiv.org/abs/1009.3690)

- “observed” relic density  $\Omega h^2$

← “proper” crosssection  $\langle \sigma v \rangle$  of  $(\text{DM})(\text{DM}) \rightarrow \text{SM}$

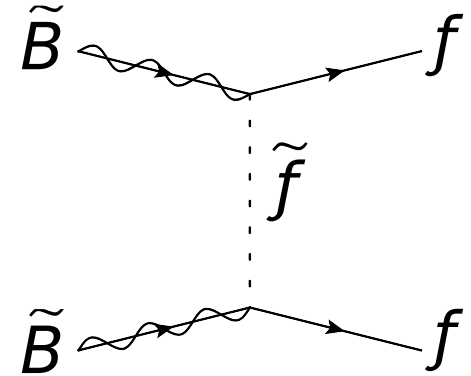
- pure  $\tilde{B}$ -DM (i.e., LSP  $\tilde{\chi}^0$  is  $\tilde{B}$ -like)

➤  $\langle \sigma v \rangle$  strongly depends on  $m_{\tilde{f}}$

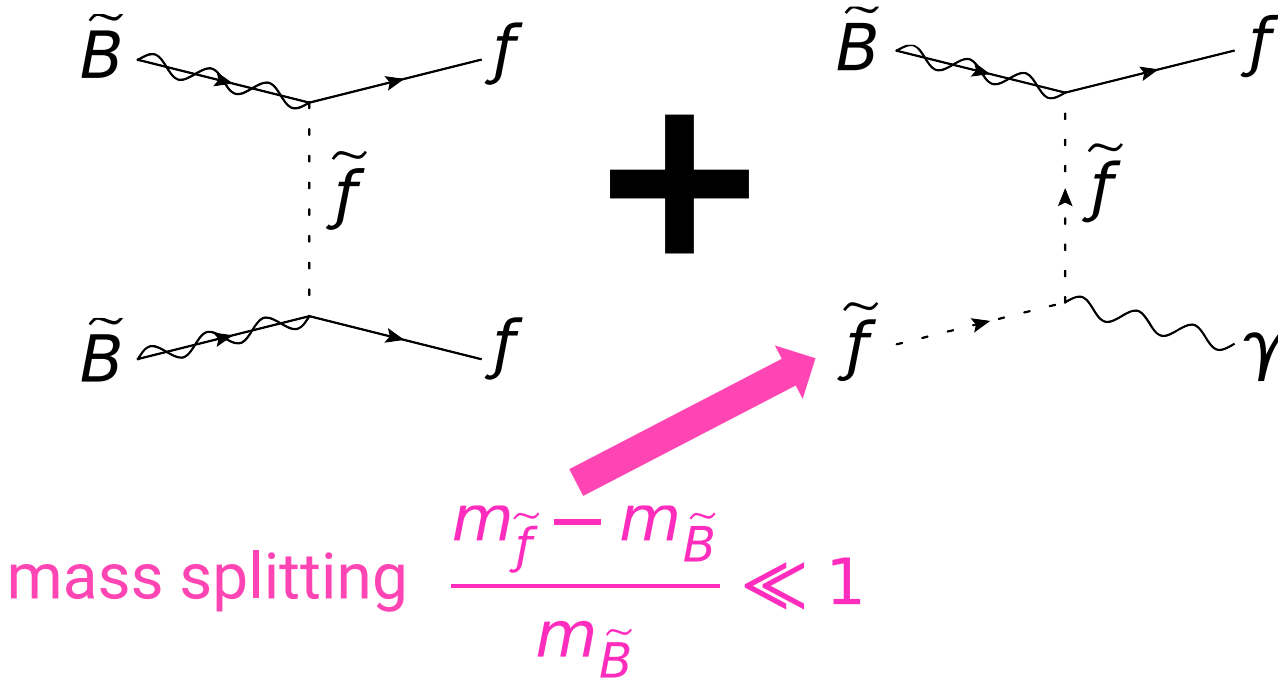
↳  $m_{\tilde{f}} \sim 100 \text{ GeV}$

$m_{\tilde{f}} \gg 100 \text{ GeV} \implies \langle \sigma v \rangle$  too small

$\implies$  “overabundant” problem



- An old solution to increase  $\langle \sigma v \rangle$ : “co-annihilation”



- An example in CMSSM with  $\tilde{\tau}$ -coannihilation

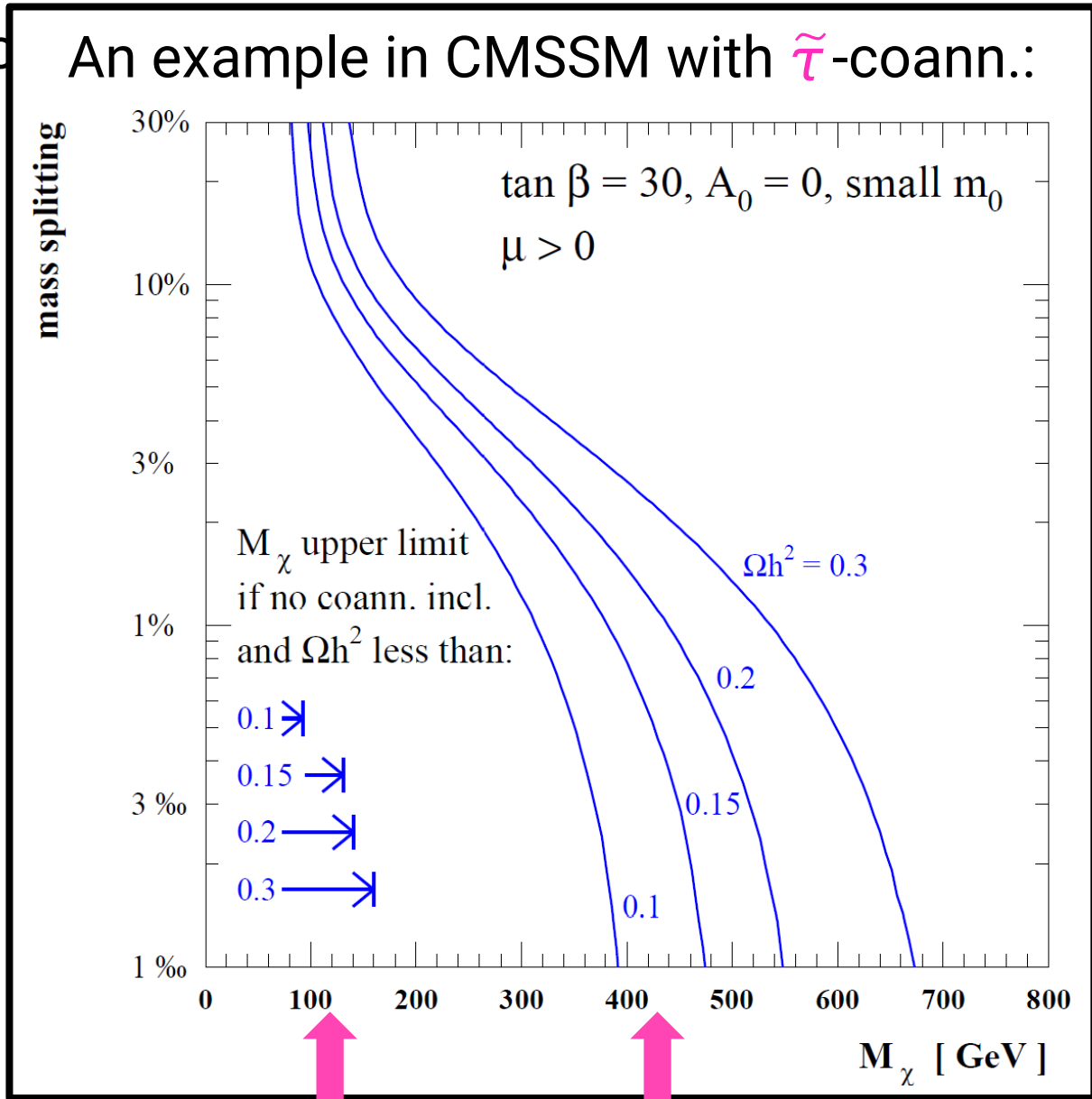


Figure from Edlö, Schelke, Ullio, Gondolo, [hep-ph/0301106](http://hep-ph/0301106)

Introduction: why overabundant?

Model: **MSSM4G**  solves overabundance.

Analysis:

- cosmic rays (CTA, Fermi, MAGIC)
- colliders (LHC)
- direct detection (LUX)

Summary with discussion seeds

■ MSSM = 3G generations

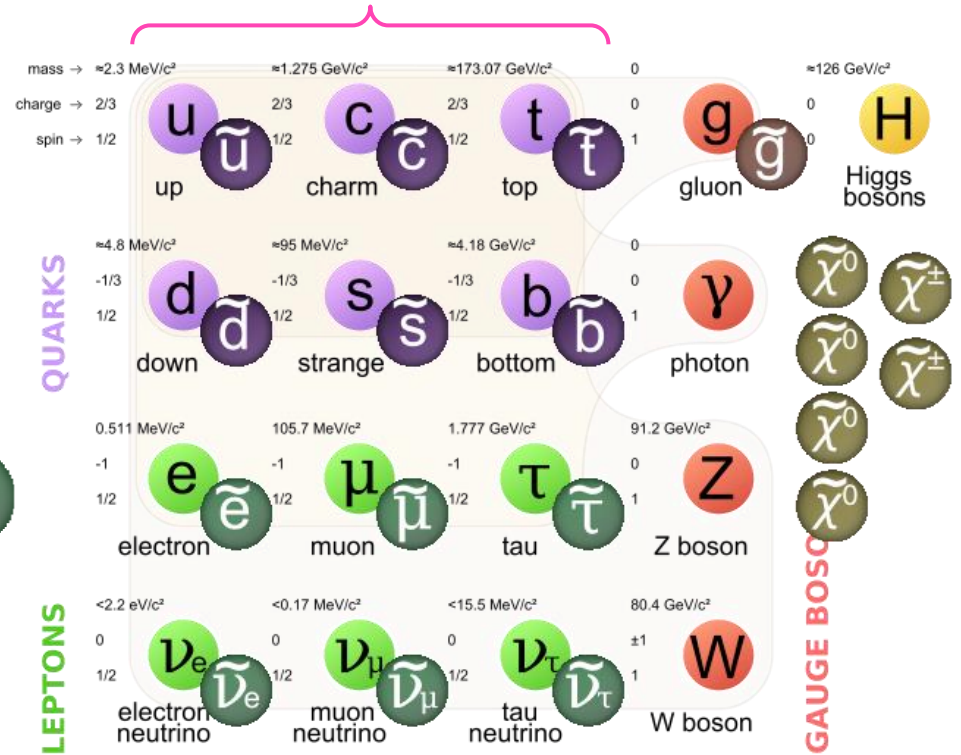


extra vector-like

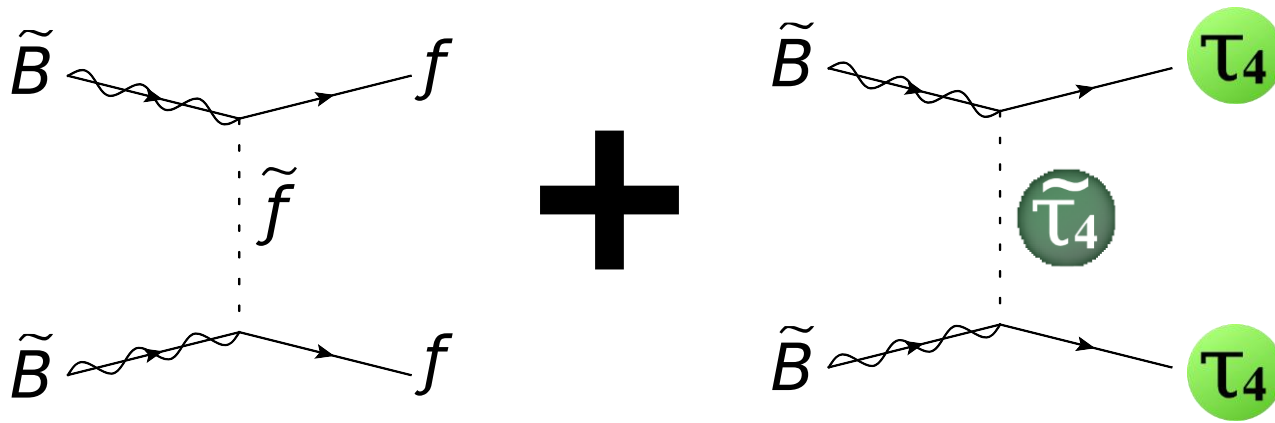
4<sup>th</sup>-Generation lepton



MSSM4G



- A new solution to increase  $\langle\sigma v\rangle$ : MSSM4G



**extra annihilation channel**

- larger  $\langle\sigma v\rangle$
- “proper”  $\Omega h^2$

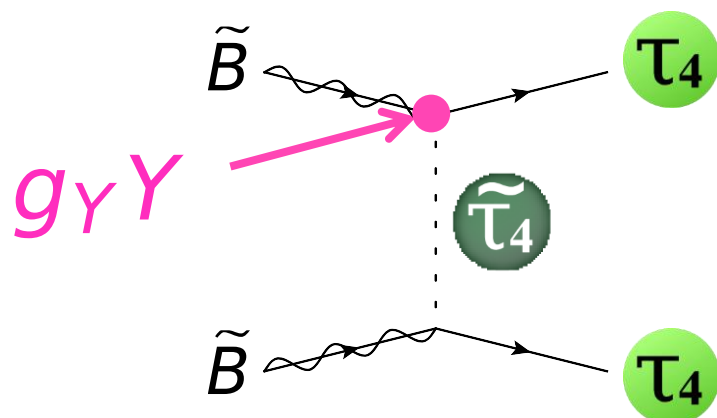
if  $\tilde{\tau}_4 \gtrsim \tilde{B} > \tau_4$



$$(Q_i, \bar{U}_i, \bar{D}_i, L_i, \bar{E}_i) + (H_u, H_d) \quad [\text{MSSM}]$$

$(i = 1 \dots 3)$

$$+ (E_4, \bar{E}_4) \quad [\text{MSSM4G}]$$



$$\Rightarrow \langle \sigma \nu \rangle \propto Y^4$$

	$SU(3)_{\text{color}}$	$SU(2)_{\text{weak}}$	$U(1)_Y$
$Q_i$	<b>3</b>	<b>2</b>	1/6
$\bar{U}_i$	<b><math>\bar{3}</math></b>	<b>1</b>	-2/3
$\bar{E}_i$	<b>1</b>	<b>1</b>	1
$\bar{D}_i$	<b><math>\bar{3}</math></b>	<b>1</b>	1/3
$L_i$	<b>1</b>	<b>2</b>	-1/2
$H_u$	<b>1</b>	<b>2</b>	1/2
$H_d$	<b>1</b>	<b>2</b>	-1/2
$\bar{E}_4$	<b>1</b>	<b>1</b>	1
$E_4$	<b>1</b>	<b>1</b>	-1

$$W = Y_u H_u Q \bar{U} + Y_d H_d Q \bar{D} + Y_e H_d L \bar{E}$$

$$+ M_{E_4} E_4 \bar{E}_4 + \epsilon_i H_d L_i \bar{E}_4$$

[vector-like mass]

[mixing with SM leptons]

■ MSSM +  $E\bar{E}$  → breaks coupling unification

■ QUE model : MSSM +  $Q\bar{Q}U\bar{U}E\bar{E}$

✓ gauge coupling unification

✓ SU(5) GUT

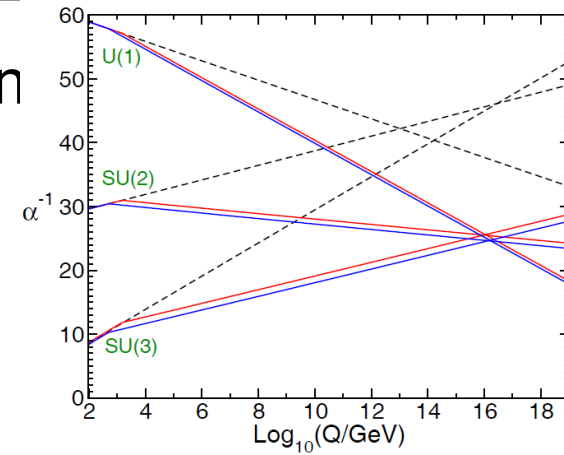
➤ extra  $H_u Q_4 \bar{U}_4$  interaction →  $m_h$  **UP**

■ QDEE model : MSSM +  $Q\bar{Q}D\bar{D}E\bar{E}E\bar{E}$

✓ gauge coupling unification

✗ SU(5) GUT

➤ extra  $H_d Q_4 \bar{D}_4$  coupling →  $m_h$  slightly **UP**



■ MSSM +  $E\bar{E}$  → breaks coupling unification

■ QUE model : MSSM +  $Q\bar{Q}U\bar{U}E\bar{E}$

⇒ MSSM +  $T_4, B_4, t_4, \tau_4,$

$\tilde{T}_{4L}, \tilde{T}_{4R}, \tilde{B}_{4L}, \tilde{B}_{4R}, \tilde{t}_{4L}, \tilde{t}_{4R}, \tilde{\tau}_{4L}, \tilde{\tau}_{4R}$

■ QDEE model : MSSM +  $Q\bar{Q}D\bar{D}E\bar{E}E\bar{E}$

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■ MSSM +  $E\bar{E}$  → breaks coupling

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assumed to be “decoupled” (very heavy)  
and we will ignore them.

■ QDEE model : MSSM +  $Q\bar{Q}D\bar{D}E\bar{E}E\bar{E}$

⇒ MSSM +  ~~$T_4, B_4, b_4, \tau_4, \tau_5,$~~

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### Other working assumptions

- $M_1 \ll \mu \ll M_2$   
→ LSP  $\tilde{\chi}_1^0$  is  $\tilde{B}$ -like
- All the other SUSY particles & extra Higgses are decoupled.

■ MSSM +  $E\bar{E}$  → breaks coupling

■ QUE model : MSSM +  $Q\bar{Q}U\bar{U}E\bar{E}$

⇒ SM +  $\tilde{\chi}_1^0 (\approx \tilde{B})$ ,  $\tau_4$ ,  
 $\underbrace{\tilde{\tau}_{4L}, \tilde{\tau}_{4R}}_{\text{assumed to be equal-mass}}$

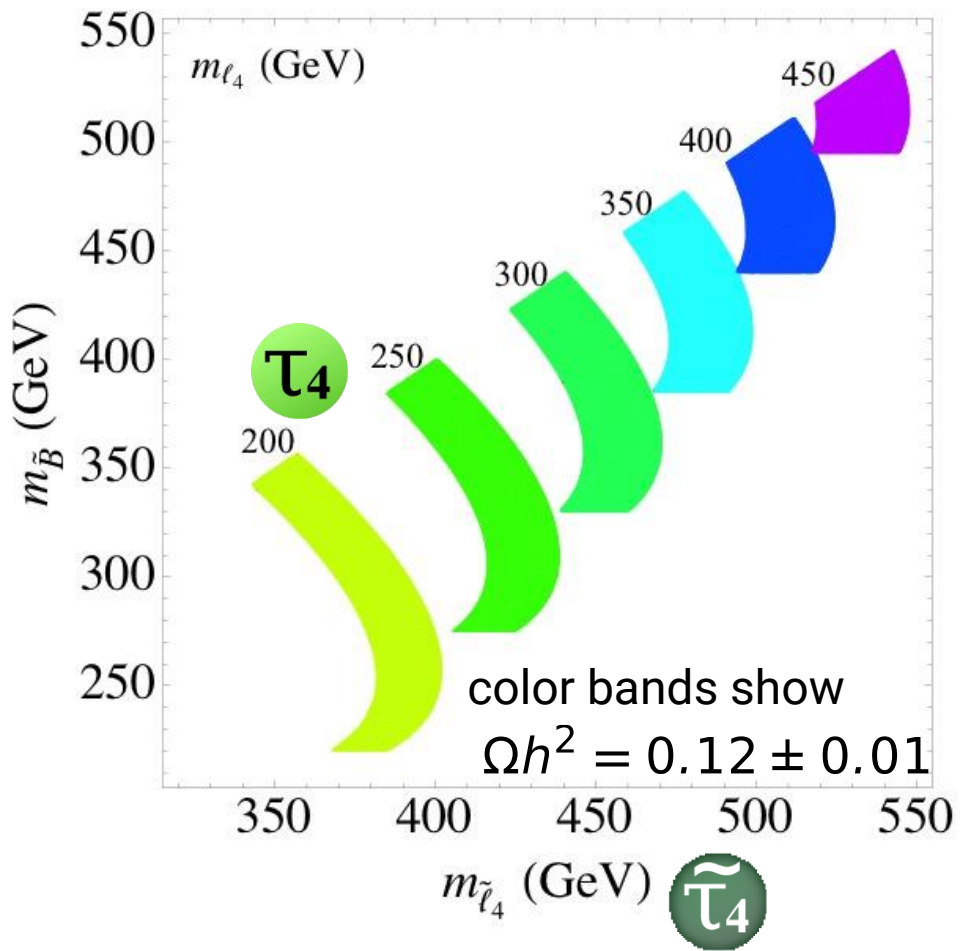
■ QDEE model : MSSM +  $Q\bar{Q}D\bar{D}E\bar{E}E\bar{E}$

⇒ SM +  $\tilde{\chi}_1^0 (\approx \tilde{B})$ ,  $\underbrace{\tau_4, \tau_5}_{\text{assumed to be equal-mass}}$ ,  
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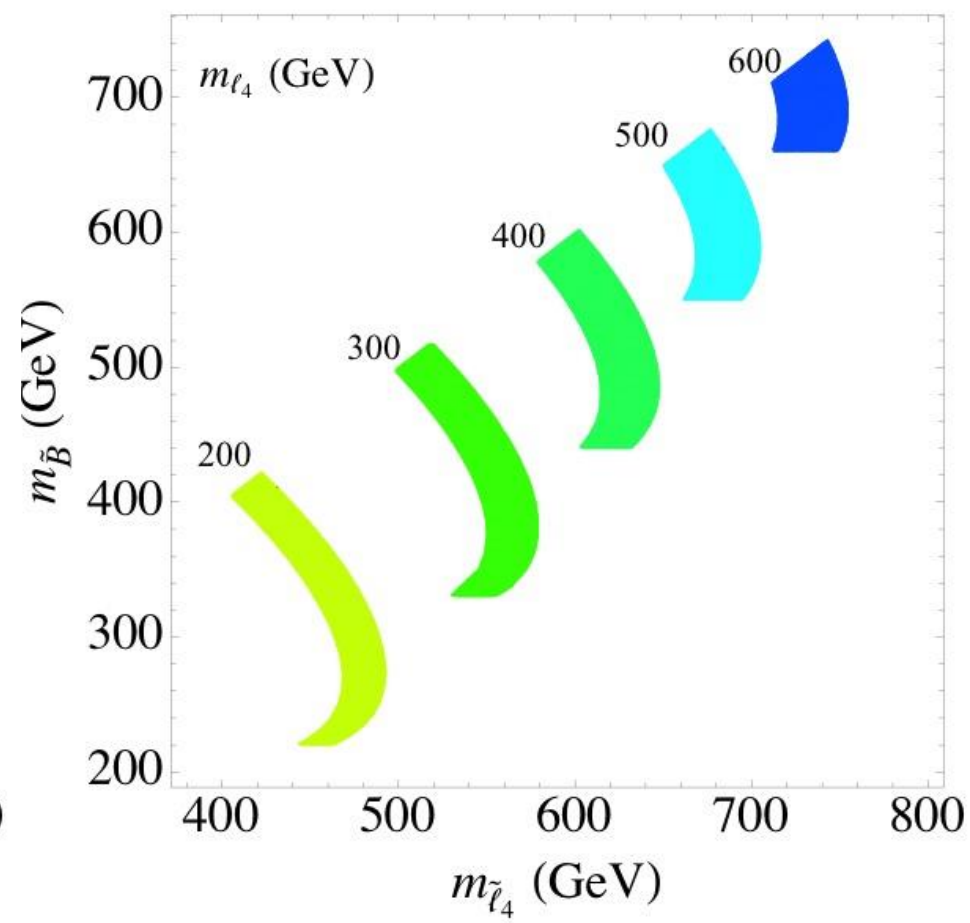
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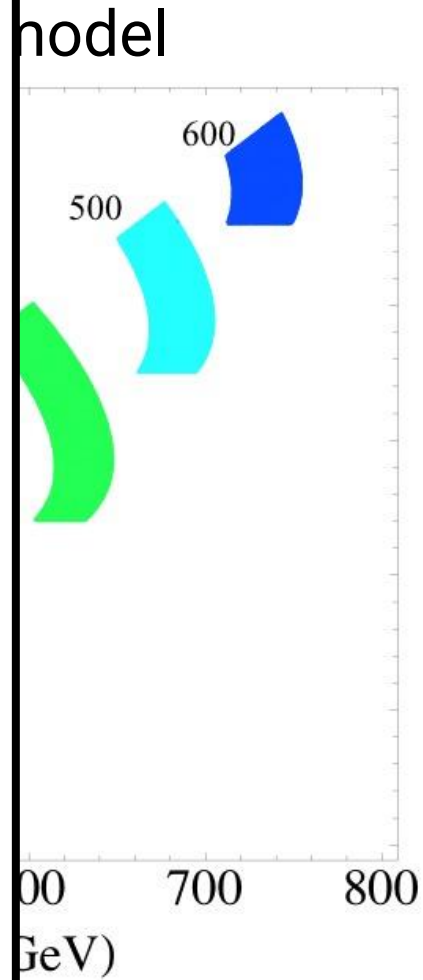
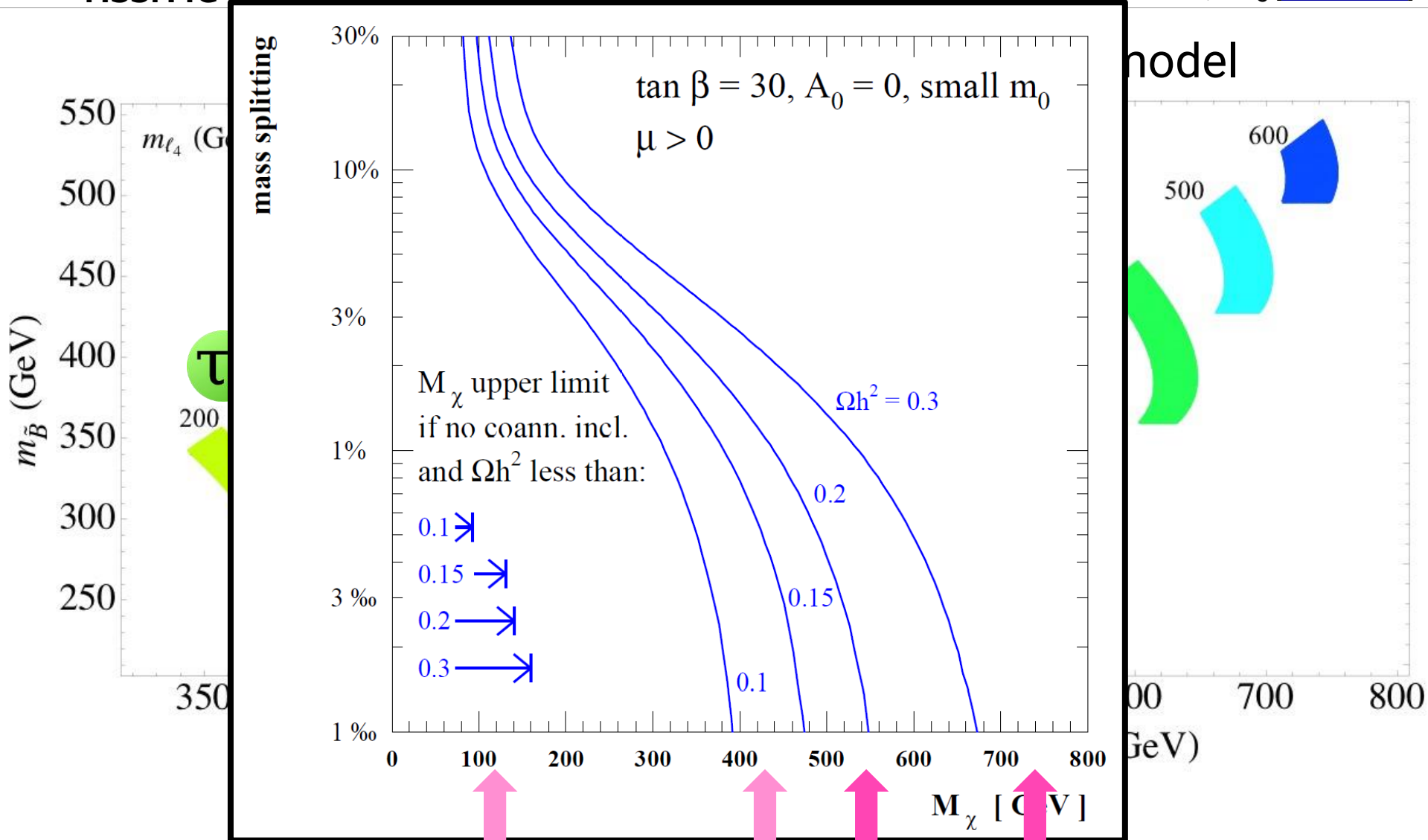
### QUE model



### QDEE model



$$\tilde{\tau}_4 \gtrsim \tilde{B} > \tau_4$$



Introduction: why overabundant?

Model: MSSM4G  solves overabundance.

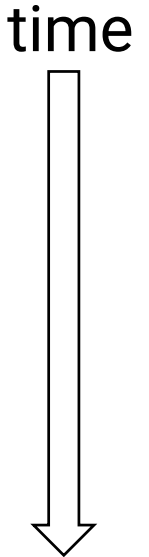
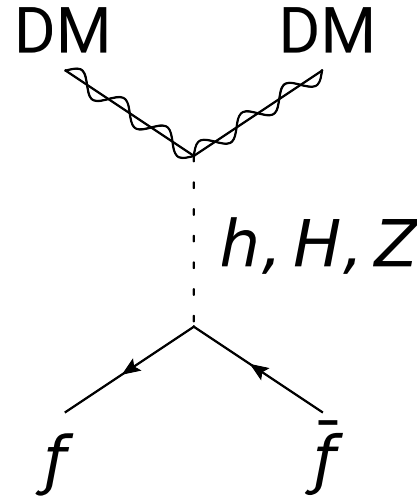
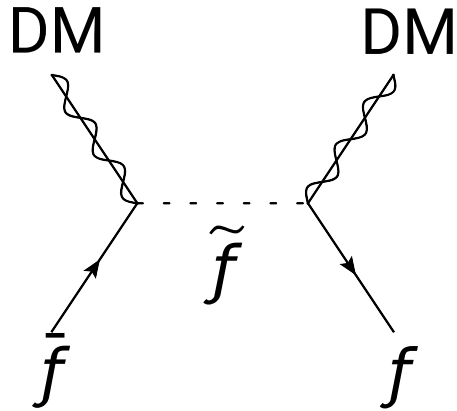
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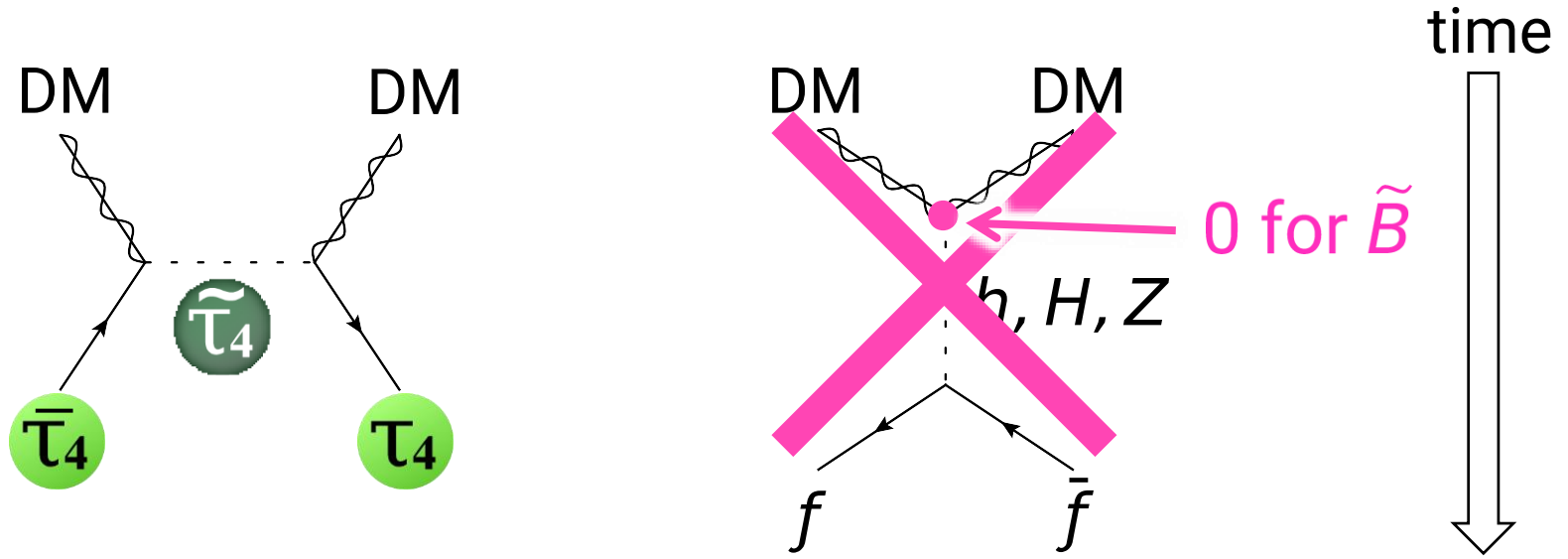
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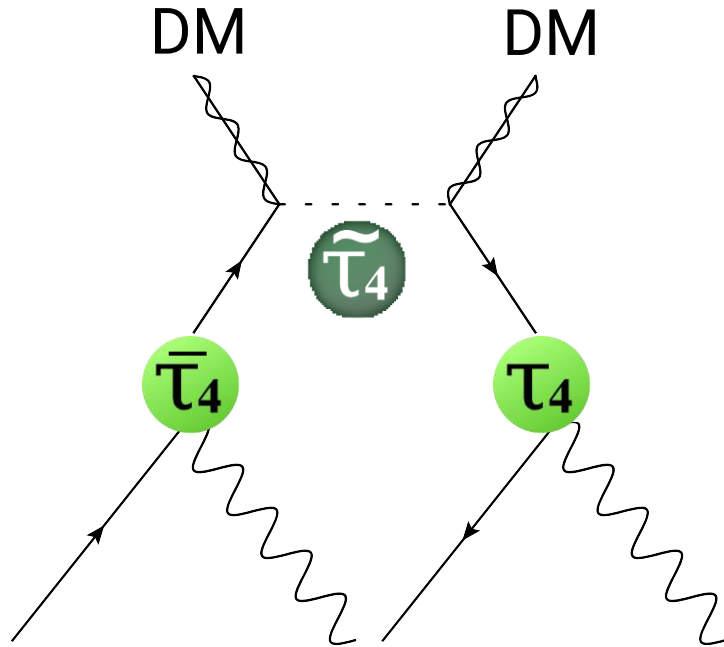
- DM indirect detection (= searches for DM annihilation)



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- DM indirect detection (= searches for  $DM DM \rightarrow \tau_4 \bar{\tau}_4$ )



$$\tau_4 \longrightarrow \begin{cases} W + \nu \\ Z + l \\ h + l \end{cases} \quad \left( \begin{array}{l} \nu = \nu_e, \nu_\mu, \nu_\tau \\ l = e, \mu, \tau \end{array} \right)$$

$$W\nu : Zl : hl \sim 2 : 1 : 1$$

$$W \ni Y_e H_d L \bar{E}$$

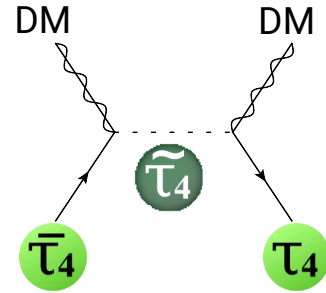
$$+ M_{E_4} E_4 \bar{E}_4 + \epsilon_i H_d L_i \bar{E}_4$$

[vector-like mass]      [mixing with SM leptons]

■ DM indirect detection

$$W \ni Y_e H_d L \bar{E} + M_{E_4} E_4 \bar{E}_4 + \epsilon_i H_d L_i \bar{E}_4$$

$$W\nu : Zl : hl \sim 2 : 1 : 1$$

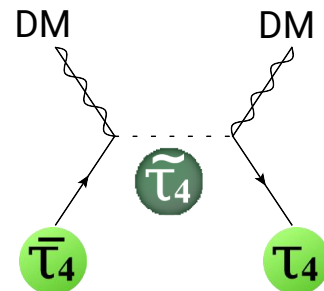


	DM DM →
$\tau_{4(5)}$ mixes with $e$	$W^+W^- \quad ZZ \quad hh \quad \nu\bar{\nu} \quad e^+e^-$
$\tau_{4(5)}$ mixes with $\mu$	$W^+W^- \quad ZZ \quad hh \quad \nu\bar{\nu} \quad \mu^+\mu^-$
$\tau_{4(5)}$ mixes with $\tau$	$W^+W^- \quad ZZ \quad hh \quad \nu\bar{\nu} \quad \tau^+\tau^-$

■ DM indirect detection

$$W \ni Y_e H_d L \bar{E} + M_{E_4} E_4 \bar{E}_4 + \epsilon_i H_d L_i \bar{E}_4$$

$$W\nu : Zl : Hl \sim 2 : 1 : 1$$



insensitive (IceCube)

DM DM →

$\tau_{4(5)}$  mixes with  $e$

$W^+W^- \quad ZZ \quad hh$

$\nu\bar{\nu}$

less sensitive / large BKG uncertainty

$e^+e^-$

$\tau_{4(5)}$  mixes with  $\mu$

$W^+W^- \quad ZZ \quad hh$

$\nu\bar{\nu}$

$\mu^+\mu^-$

$\tau_{4(5)}$  mixes with  $\tau$

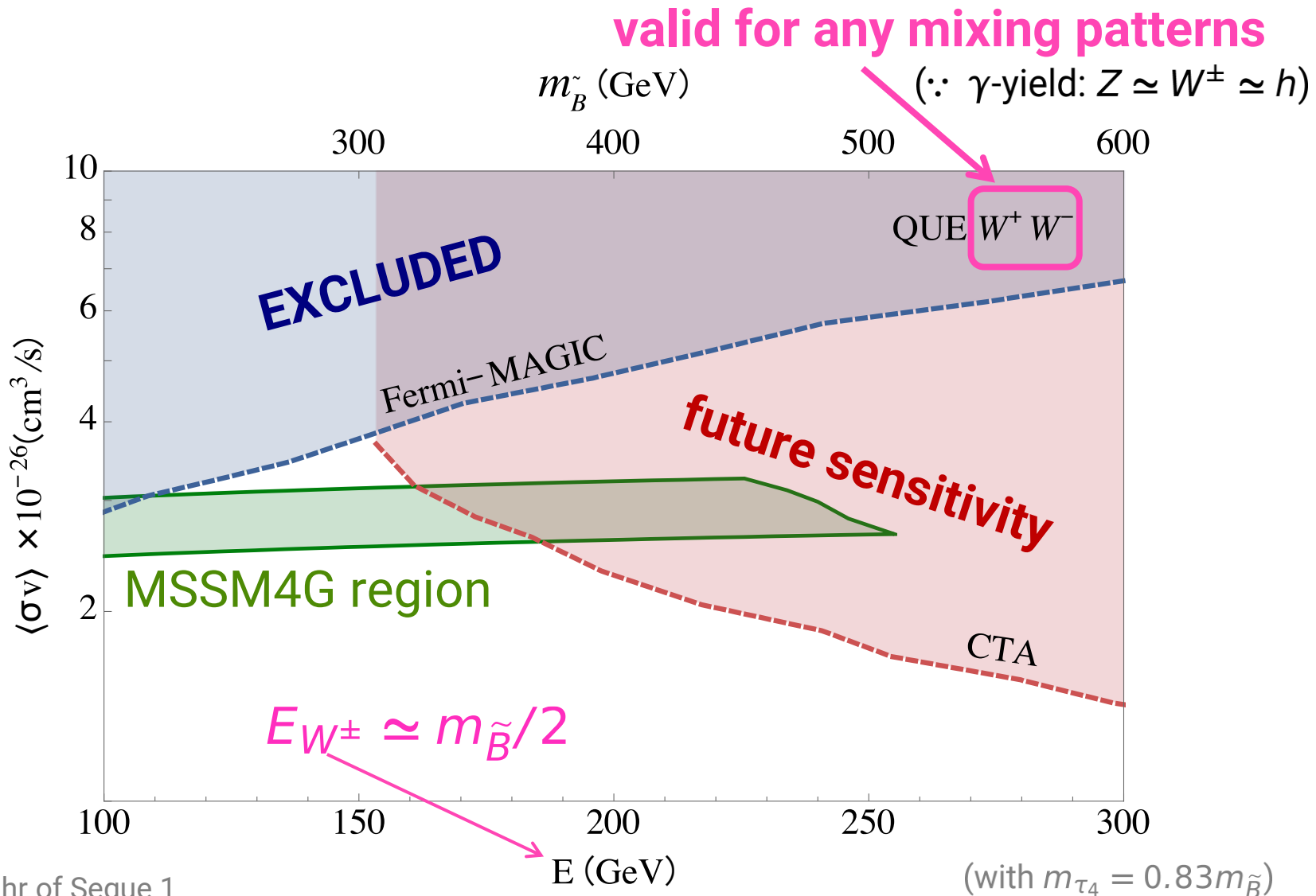
$W^+W^- \quad ZZ \quad hh$

$\nu\bar{\nu}$

$\tau^+\tau^-$

→ ... →  $\gamma$

→  $\pi^0$  →  $\gamma$



MAGIC: 158 hr of Segue 1

Fermi-LAT: 6 yr of 15 dSph (incl. Segue 1)

DM profile: NFW

Fermi-LAT dominates MAGIC in almost all  $E$ -range.

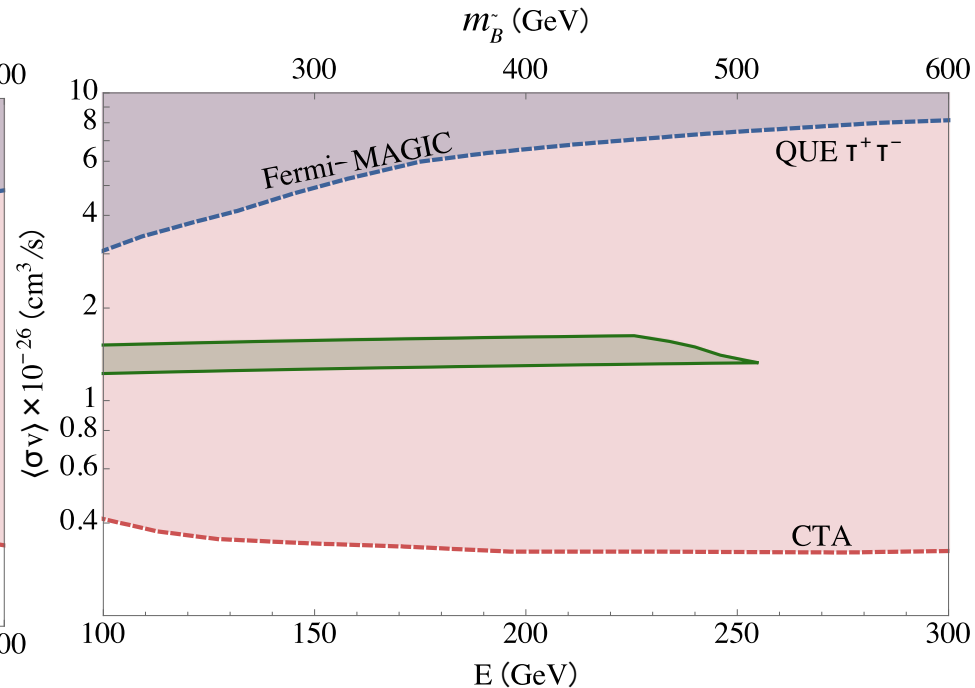
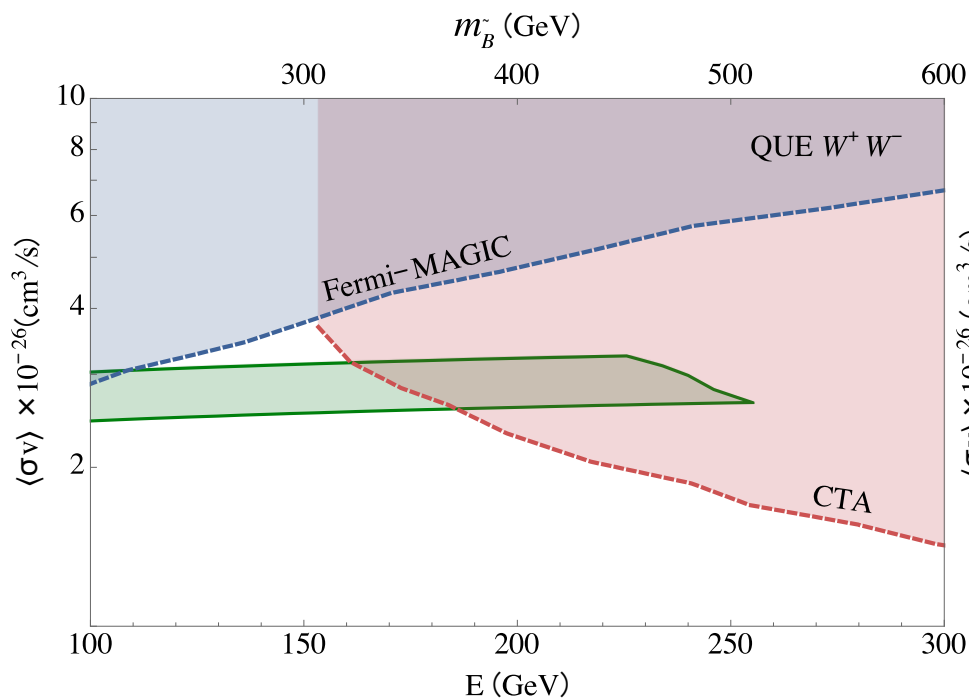
CTA prospect : 500hr of Milky Way

DM profile: Einasto

No syst. unc. (stat only)

WW (any mixing pattern)

$\tau\tau$  (only for  $\tau$ -mixing cases)



- ✓  $\tau$ -mixing fully covered
- ✓ e/ $\mu$ -mixing with  $m_{\tilde{B}} > 340-380$  GeV covered

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Fermi-LAT: 6 yr of 15 dSph (incl. Segue 1)

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Fermi-LAT dominates MAGIC in almost all  $E$ -range.

(with  $m_{\tau_4} = 0.83m_{\tilde{B}}$ )

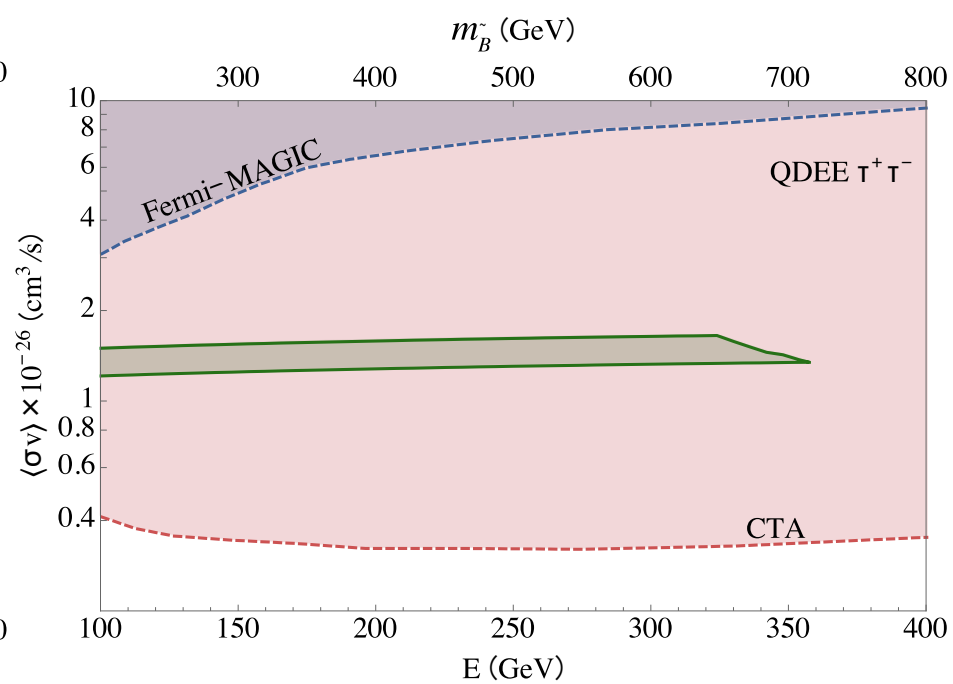
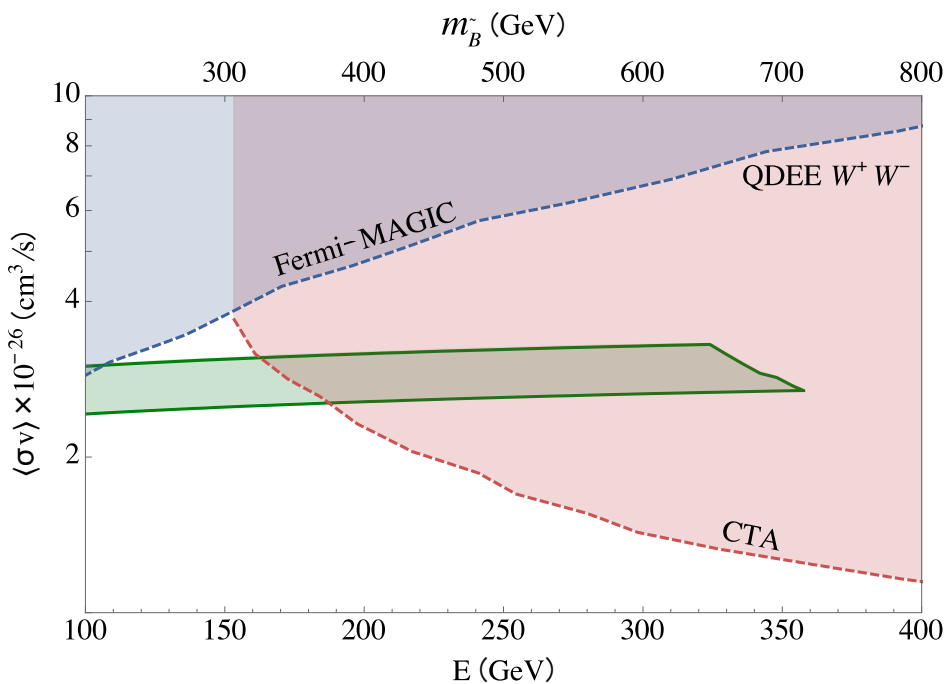
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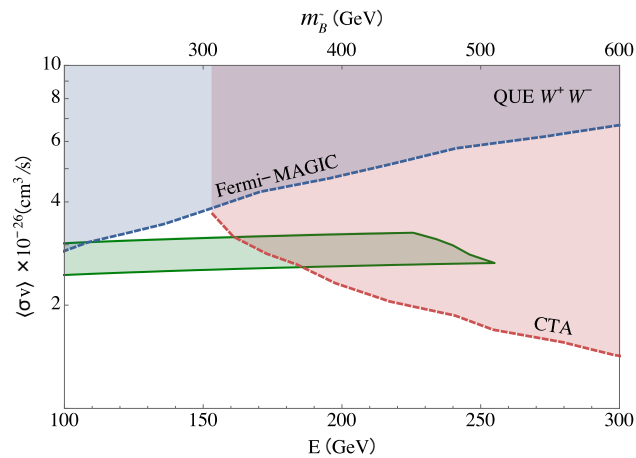
No syst. unc. (stat only)



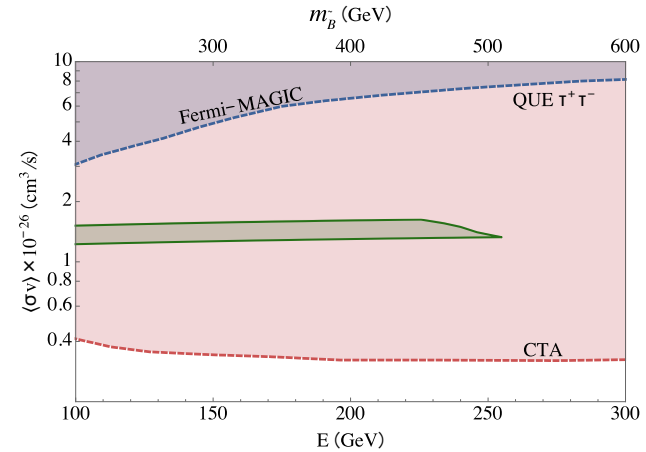
# Summary

	e-mixing	$\mu$ -mixing	$\tau$ -mixing
CTA 500hr	covers $m_{\tilde{B}} > 340-380$ GeV		<b>full coverage</b>
HL-LHC			

e/ $\mu$ -mixing, QUE



$\tau$ / $\mu$ -mixing, QUE



Introduction: why overabundant?

Model: **MSSM4G**  solves overabundance.

Analysis:

- cosmic rays (CTA, Fermi, MAGIC)
- colliders (LHC)
- direct detection (LUX)

Summary with discussion seeds

■ MSSM +  $E\bar{E}$  → breaks coupling unification

■ QUE model : MSSM +  $Q\bar{Q}U\bar{U}E\bar{E}$

⇒ SM +  $\tilde{\chi}_1^0 (\approx \tilde{B})$ ,  $\tau_4$ ,  
 $\underbrace{\tilde{\tau}_{4L}, \tilde{\tau}_{4R}}_{\text{assumed to be equal-mass}}$

■ QDEE model : MSSM +  $Q\bar{Q}D\bar{D}E\bar{E}E\bar{E}$

⇒ SM +  $\tilde{\chi}_1^0 (\approx \tilde{B})$ ,  $\underbrace{\tau_4, \tau_5}_{\text{assumed to be equal-mass}}$ ,  
 $\underbrace{\tilde{\tau}_{4L}, \tilde{\tau}_{4R}, \tilde{\tau}_{5L}, \tilde{\tau}_{5R}}_{\text{assumed to be equal-mass}}$

■ MSSM +  $E\bar{E}$  → breaks coupling unification

■ QUE model : MSSM +  $Q\bar{Q}U\bar{U}E\bar{E}$

⇒ SM +  $\tilde{\chi}_1^0 (\approx \tilde{B}), \tau_4,$   
 $\tau_{4L}, \tau_{4R}$   
 assumed to be equal-mass

**extra lepton search** (red arrow from  $\tau_4$ )

**slepton search** (blue arrow from  $\tau_{4L}, \tau_{4R}$ )

■ QDEE model : MSSM +  $Q\bar{Q}D\bar{D}E\bar{E}E\bar{E}$

⇒ SM +  $\tilde{\chi}_1^0 (\approx \tilde{B}), \tau_4, \tau_5,$   
 $\tau_{4L}, \tau_{4R}, \tau_{5L}, \tau_{5R}$   
 assumed to be equal-mass

**slepton search** (blue arrow from  $\tau_4, \tau_5$ )

■ MSSM +  $E\bar{E}$  → breaks coupling unification

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$\tilde{\tau}_{4L}, \tilde{\tau}_{4R}$

assumed to be equal-mass

+  $Q\bar{Q}D\bar{D}E\bar{E}E\bar{E}$

$\tau_4, \tau_5$ ,

$\tilde{\tau}_{4L}, \tilde{\tau}_{4R}, \tilde{\tau}_{5L}, \tilde{\tau}_{5R}$

assumed to be equal-mass

**slepton search**

$\tilde{\tau}_4 \not\rightarrow \tau_4 + \tilde{B}$   
 $\rightarrow (e, \mu, \tau) + \tilde{B}$   
 $\equiv 2(4) \times \tilde{l}_R$

**extra lepton search**

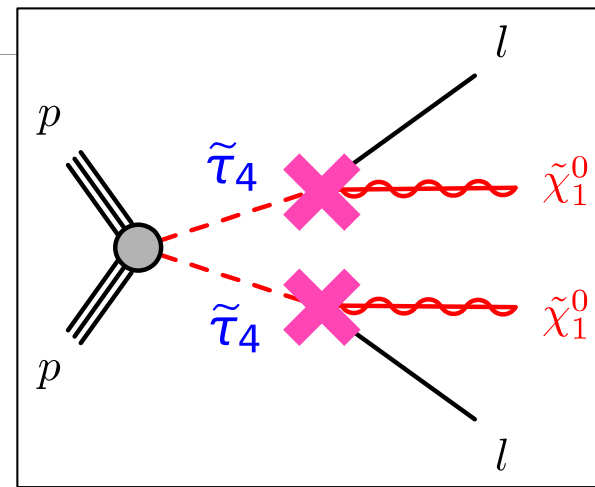
$\tau_4 \rightarrow W\nu, Zl, hl$   
 (as discussed before)

**standard searches for vectorlike leptons (but 2x in QDEE)**

# Collider prospects for extra slepton searches

$$pp \rightarrow \tilde{\tau}_{4(5)} \tilde{\tau}_{4(5)}^* \equiv pp \rightarrow \tilde{l}_R \tilde{l}_R^*$$

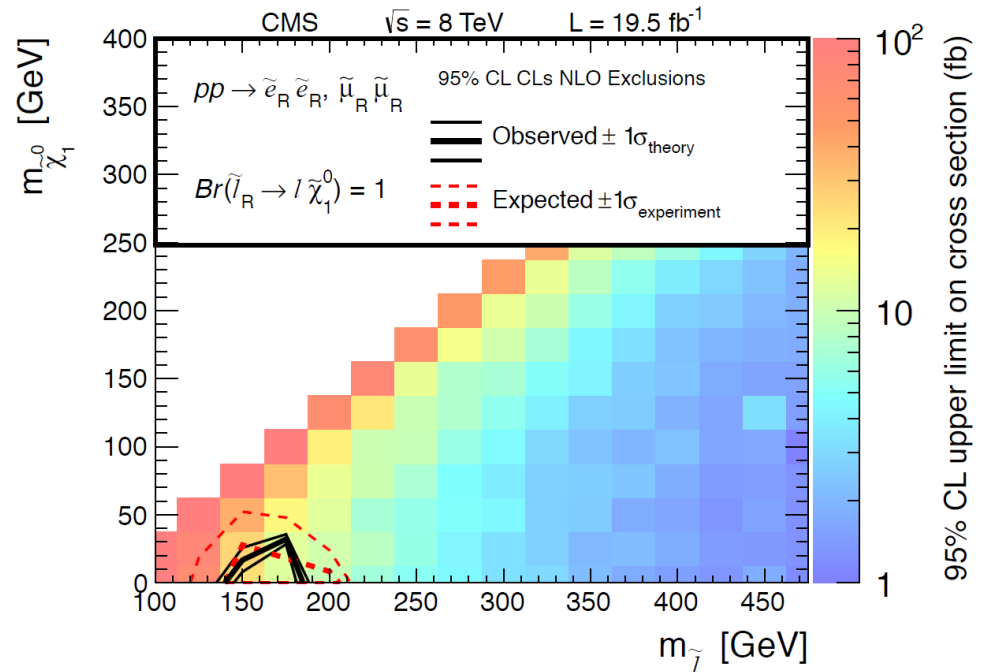
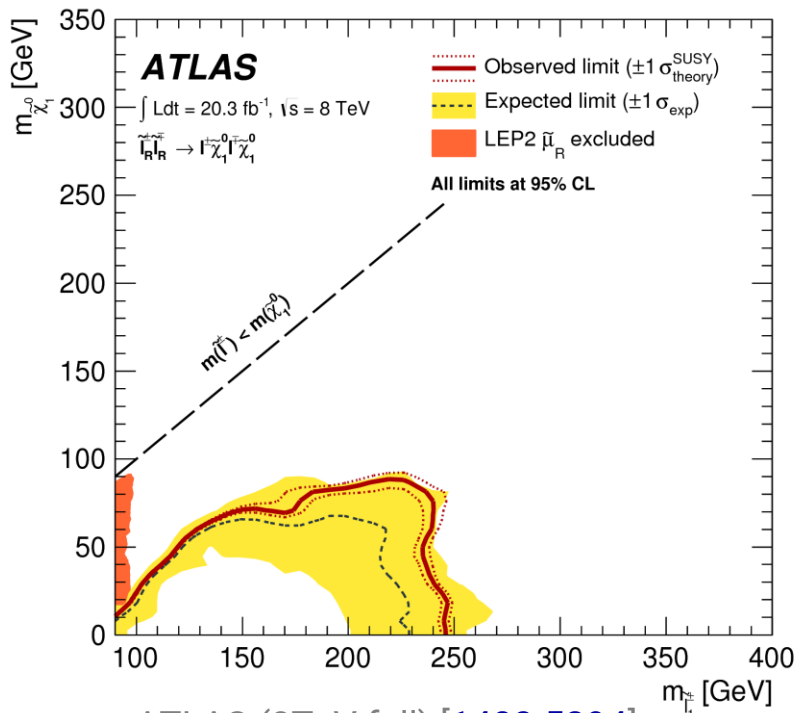
↑  
determined by mixing parameters



e/ $\mu$ -mixing  $\rightarrow$  slepton searches  $\times 2$  (4)  
( $\tilde{e}_R, \tilde{\mu}_R$ )

14 TeV prospects studied in [1408.2841](#) (Eckel, Ramsey-Musolf, Shepherd, Su)

$\rightarrow$  re-interpreted

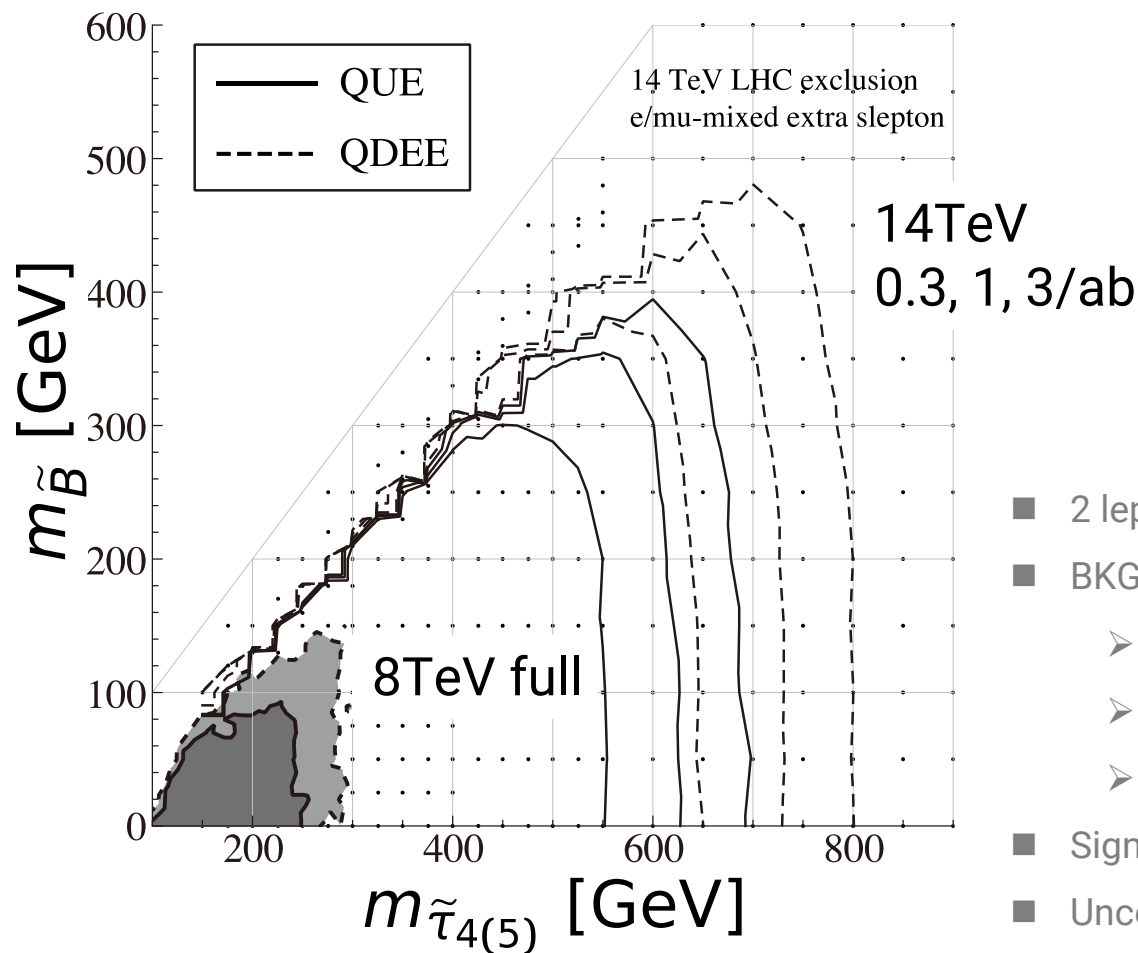
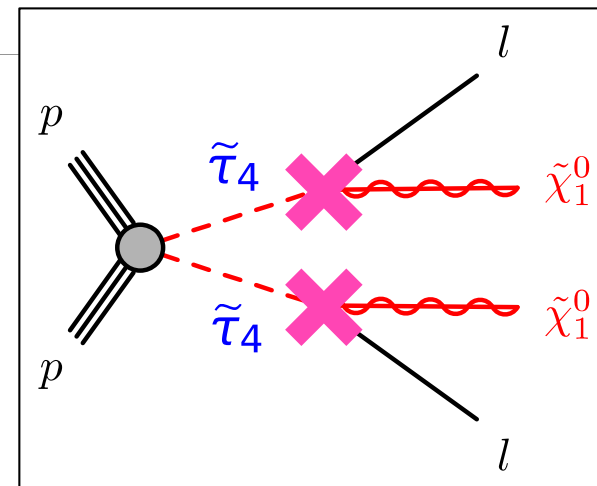


# Collider prospects for extra slepton searches

$$pp \rightarrow \tilde{\tau}_{4(5)} \tilde{\tau}_{4(5)}^* \equiv pp \rightarrow \tilde{l}_R \tilde{l}_R^*$$

↑  
determined by mixing parameters

e/ $\mu$ -mixing  $\rightarrow$  slepton searches  $\times 2$  (4)  
( $\tilde{e}_R, \tilde{\mu}_R$ )



- 2 lepton + MET + mT2 + jet-veto
- BKG taken from 1408.2841
  - MG5-Pythia-Delphes (also for signal)
  - rescaled by NLO  $K$ -factor
  - di-boson dominates
- Signal events at LO level
- Uncertainties = stat. + 5% syst.

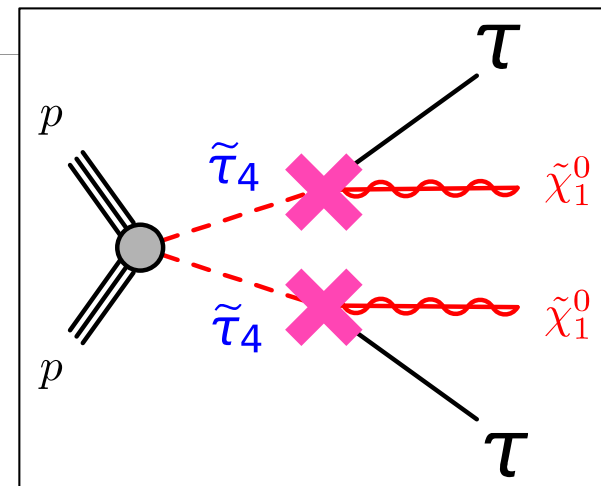
## Collider prospects for **extra slepton** searches

$$pp \rightarrow \tilde{\tau}_{4,(5)} \tilde{\tau}_{4,(5)}^* \equiv pp \rightarrow \tilde{l}_R \tilde{l}_R^*$$

↑  
determined by mixing parameters

$\tau$ -mixing  $\rightarrow$  stau searches  $\times 2$  (4)

**$\rightarrow$  No constraint expected.**

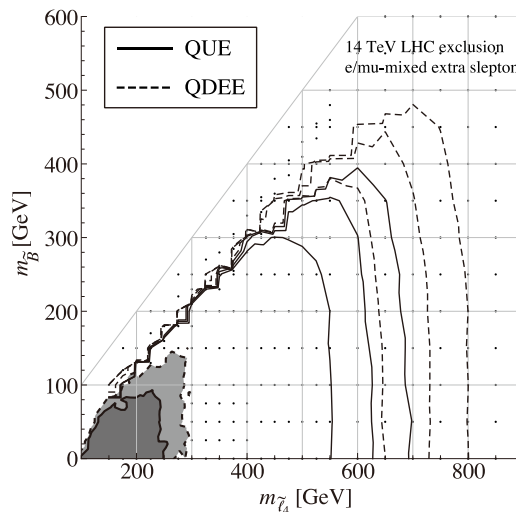
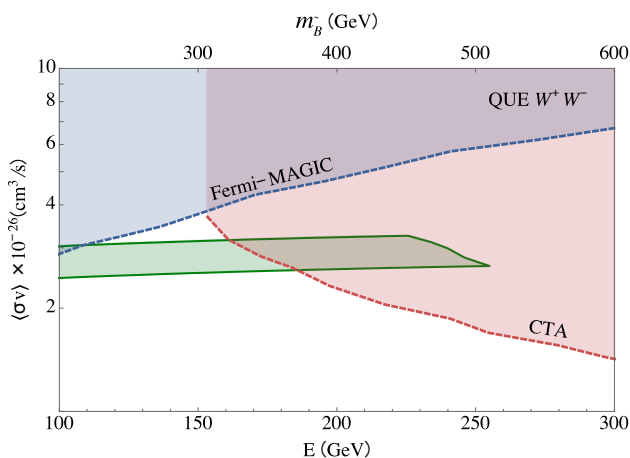


- LHC Run 1 provided no limit on MSSM stau mass.
- 14TeV, 3/ab LHC will not exclude MSSM4G parameter region.

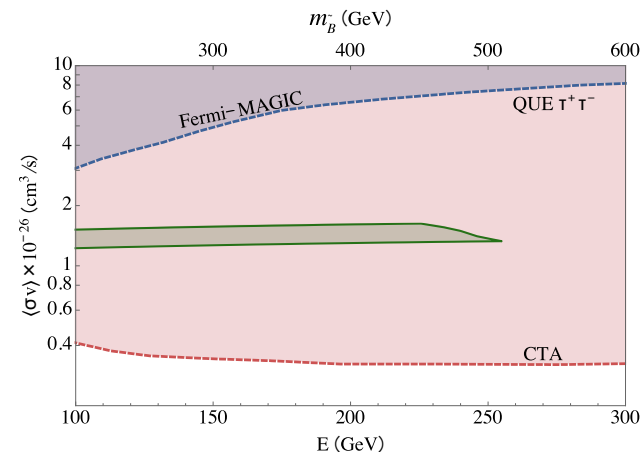


	e-mixing	$\mu$ -mixing	$\tau$ -mixing
CTA 500hr	covers $m_{\tilde{B}} > 340\text{--}380$ GeV		<b>full coverage</b>
HL-LHC (slepton)	covers $m_{\tilde{B}} < 400$ (480) GeV (but not “degenerate” region)		—
HL-LHC (lepton)			

e/ $\mu$ -mixing



$\tau/\mu$ -mixing, QUE



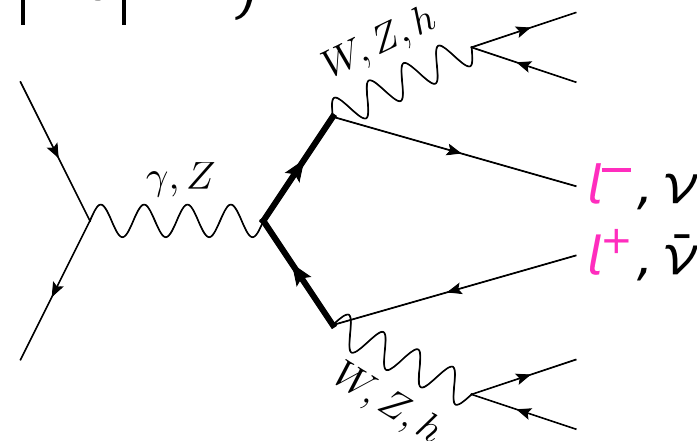
$$pp \rightarrow \tau_{4,(5)}^+ \tau_{4,(5)}^- \rightarrow (W\nu | hl | Zl)(W\nu | hl | hZ)$$

e/ $\mu$ -mixing case

“vectorlike lepton searches” by  
multi- $l^\pm$  signature ( $3-5l^\pm$ )

[Cf. ATLAS collaboration, [1506.01291](#)]

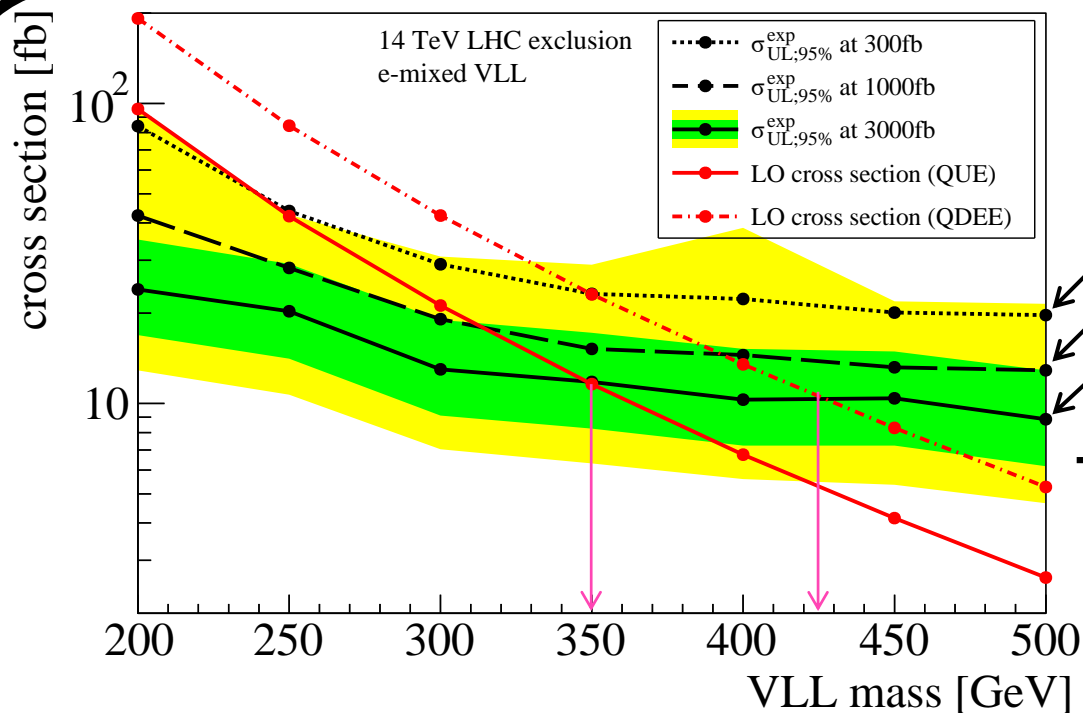
$$\left\{ \begin{array}{l} W\nu Zl \rightarrow 3l \text{ (1.3\%)} \\ W\nu hl \rightarrow 3l \text{ (0.6\%)} \\ hlZl \rightarrow 3l \text{ (0.8\%)} \\ hlhl \rightarrow 3l \text{ (0.8\%)} \end{array} \right. \quad \left\{ \begin{array}{l} W\nu Zl \rightarrow 4^+ l \text{ (0.4\%)} \\ hlZl \rightarrow 4^+ l \text{ (1.0\%)} \\ ZlZl \rightarrow 4^+ l \text{ (0.8\%)} \\ hlhl \rightarrow 4^+ l \text{ (0.2\%)} \end{array} \right.$$



→ Monte Carlo simulation

$$pp \rightarrow \tau_{4,(5)}^+ \tau_{4,(5)}^- \rightarrow (W\nu | hl | Zl)(W\nu | hl | hZ)$$

e/ $\mu$ -mixing case



- Snowmass BKG set is used.
  - MG5-Pythia-Delphes + NLO  $K$ -factor
  - di-boson +  $tt$  dominated
- SR dedicated for WZ / ZZ + leptons
  - 3L, 4L for WZ, and 4L, 5L for ZZ
  - tau-tag / b-tag not used (avoided)
- Signal by FR-MG5aMC-Pythia-Delphes (LO)
- Uncertainties = stat. + 20% syst.

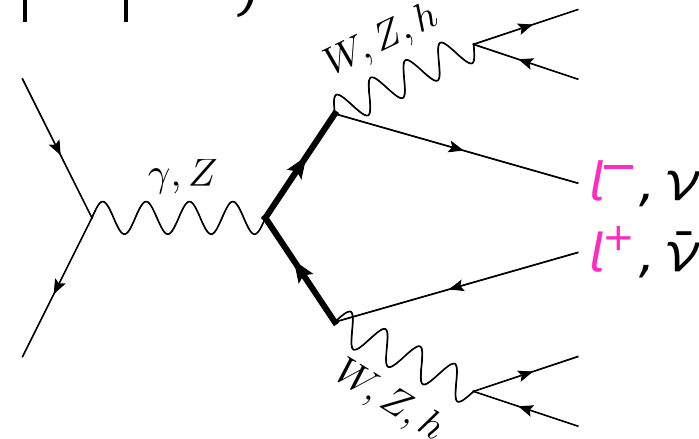
$$pp \rightarrow \tau_{4,(5)}^+ \tau_{4,(5)}^- \rightarrow (W\nu | hl | Zl)(W\nu | hl | hZ)$$

e/ $\mu$ -mixing case

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multi- $l^\pm$  signature ( $3-5l^\pm$ )

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→ 14TeV, 3/ab covers  
 $m_{\tau_4} < 350 \text{ (425) GeV}$   
QUE QDEE

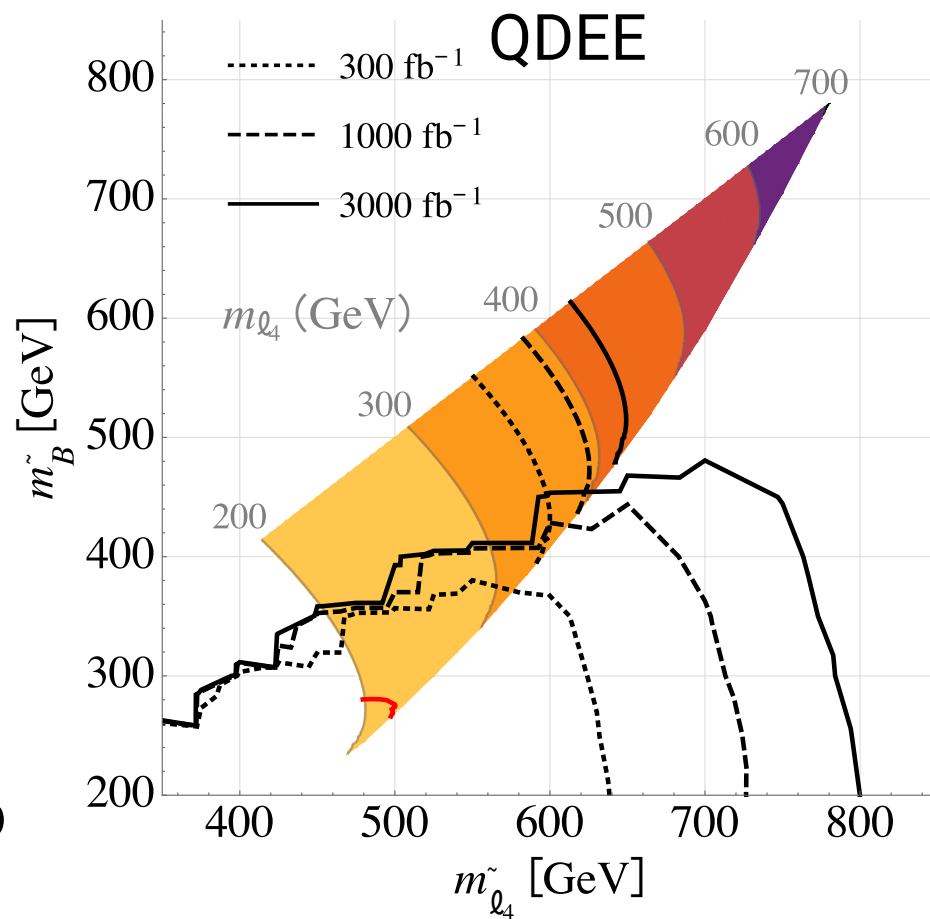
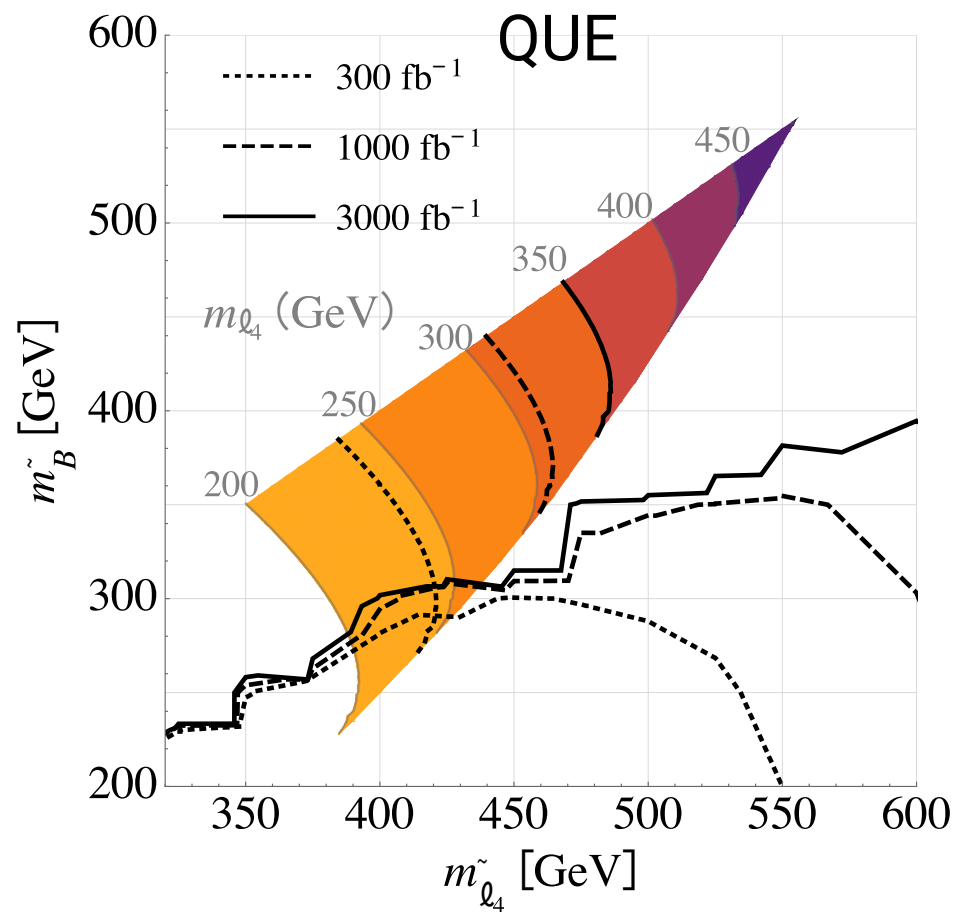
$\tau$ -mixing case

✓ [1510.03456](#) (Kumar and Matrin)

- SRs: 4(e, mu, had-tau)
- Signal and BKG by their MC (FR-MG5-Pythia-Delphes)
- no prospects for exclusion if BKG syst. unc. > 10%

→ 13 TeV, 3/ab covers  
 $m_{\tau_4} < 234 \text{ (264) GeV}$   
with “a very optimistic BKG estimation”

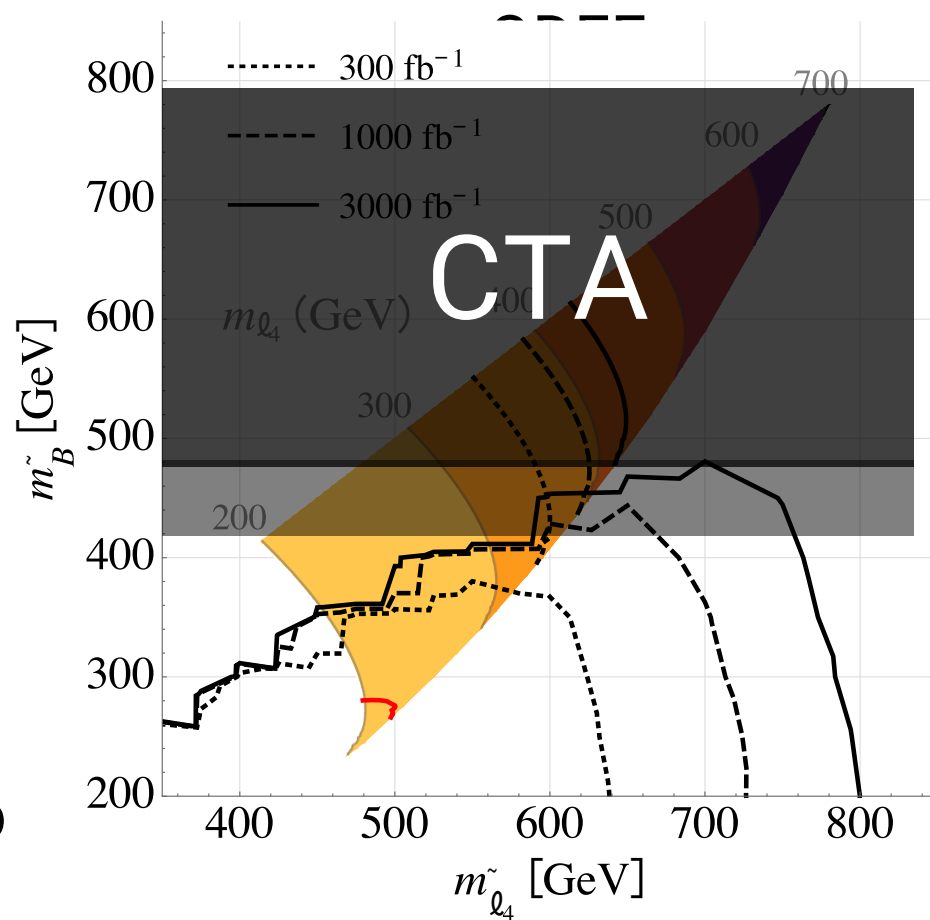
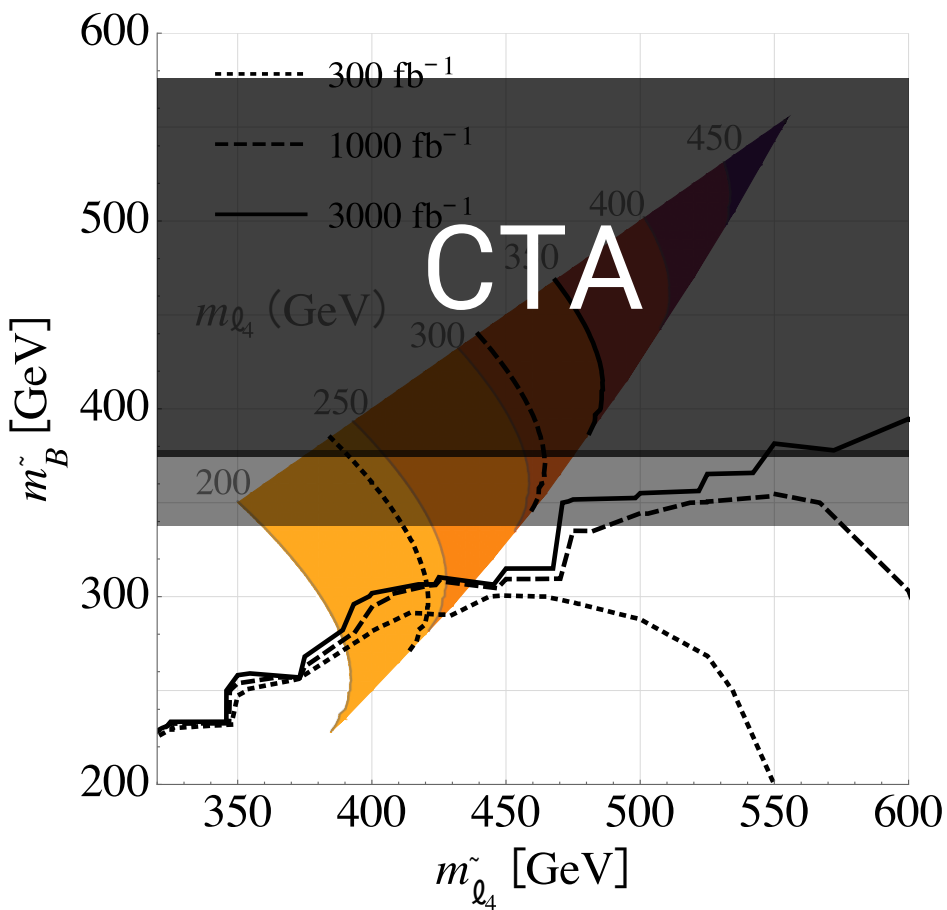
■ e/ $\mu$ -mixing cases



■  $\tau$ -mixing case

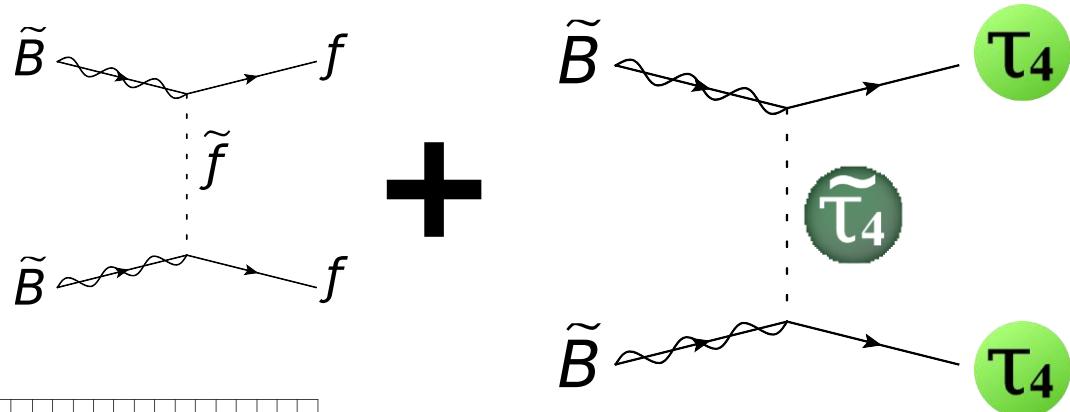
➤ LHC insensitive ... ( $\tau \cdot \omega \cdot \tau$ )

■ e/ $\mu$ -mixing cases



■  $\tau$ -mixing case

➤ LHC insensitive, but CTA covers full region



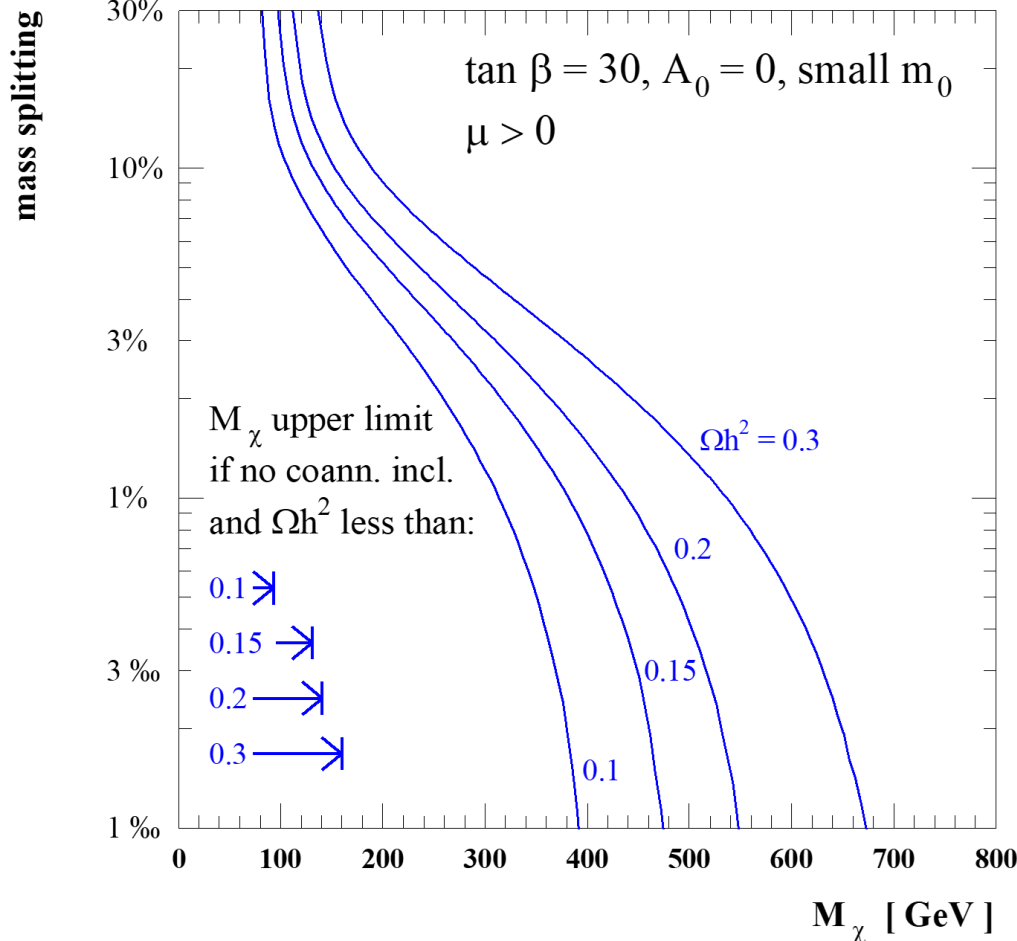
**extra annihilation channel**

→ larger  $\Omega h^2$   
 → “proper”  $\langle \sigma v \rangle$

if  $\tilde{\tau} \gtrsim \tilde{B} > \tau$

$\langle \sigma v \rangle \propto Y^4 \implies \text{MSSM} + E\bar{E}$

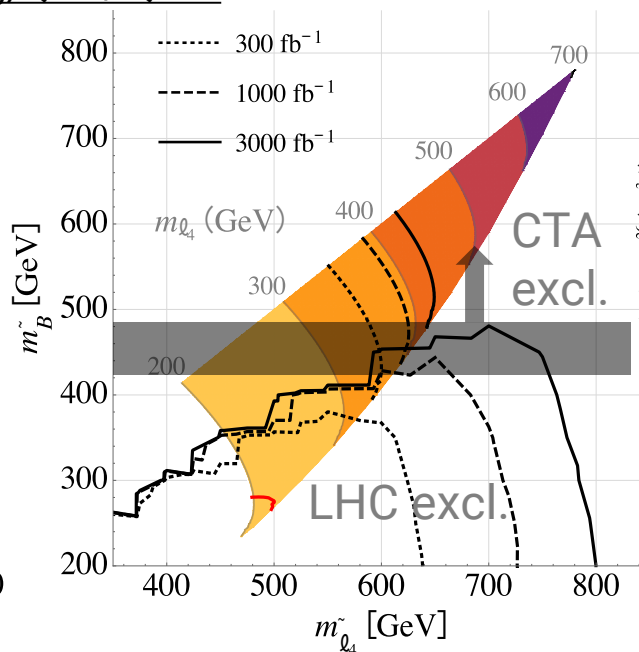
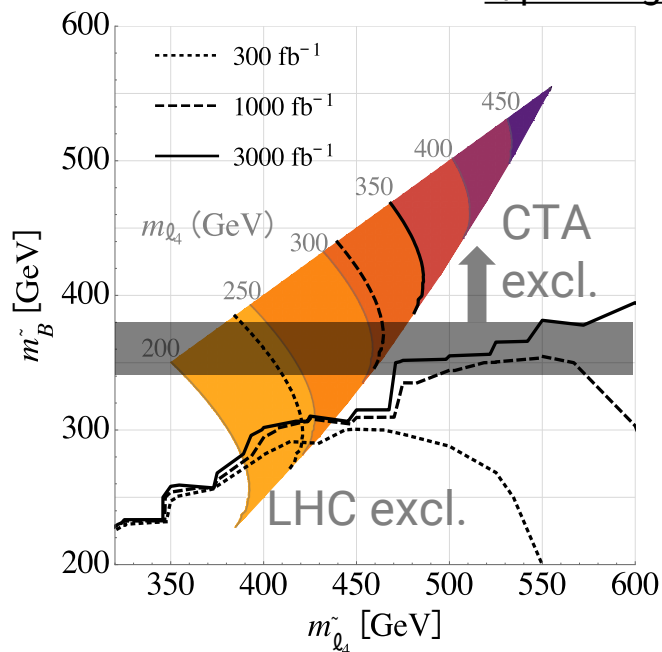
$$Y_u H_u Q \bar{U} + Y_d H_d Q \bar{D} + Y_e H_d L \bar{E} + M_{E_4} E_4 \bar{E}_4 + \epsilon_i H_d L_i \bar{E}_4$$



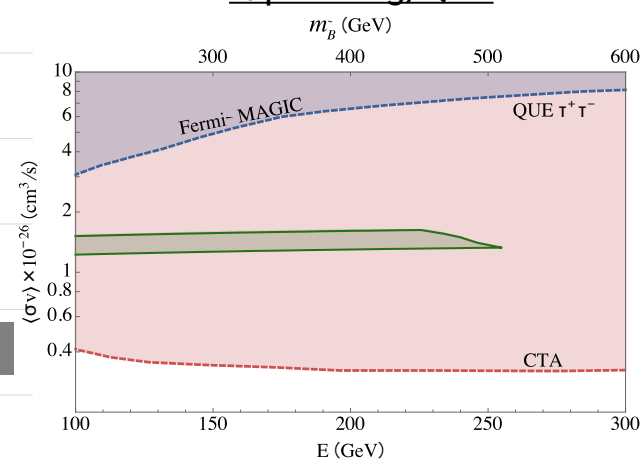
# Summary : Future prospects

	e-mixing	$\mu$ -mixing	$\tau$ -mixing
CTA 500hr	covers $m_{\tilde{B}} > 340\text{--}380$ GeV		<b>full coverage</b>
HL-LHC (slepton)	covers $m_{\tilde{B}} < 400$ (480) GeV (but not “degenerate” region)		—
HL-LHC (lepton)	covers $m_{\tau_4} < 350$ (430) GeV equivalent to $m_{\tilde{B}} < 380$ (480) GeV		—

e/ $\mu$ -mixing, QUE / QDEE



$\tau$ / $\mu$ -mixing, QUE





Introduction: why overabundant?

Model: **MSSM4G**  solves overabundance.

Analysis:

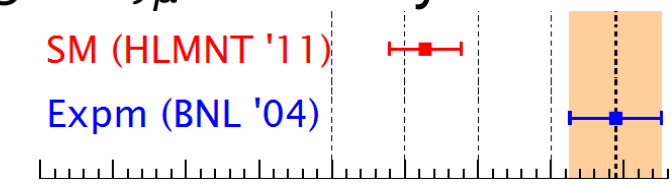
- cosmic rays (CTA, Fermi, MAGIC)
- colliders (LHC)
- direct detection (LUX)

Summary with discussion seeds

: “muon  $g-2$  problem”

$$\left( a_\mu := \frac{g_\mu - 2}{2} \right)$$

■  $(g - 2)_\mu$  anomaly



SM (HLMNT '11)

Expm (BNL '04)

$$a_\mu^{\text{SM}} = (116\,591\,828 \pm 49) \times 10^{-11}$$

$$a_\mu^{\text{exp}} = (116\,592\,089 \pm 63) \times 10^{-11}$$

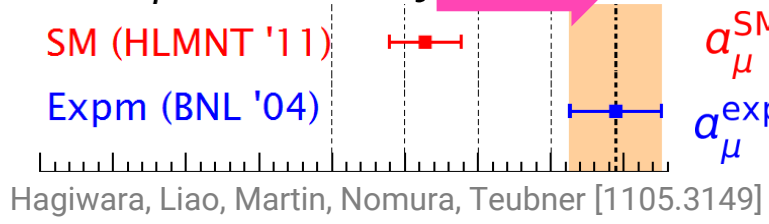
Hagiwara, Liao, Martin, Nomura, Teubner [1105.3149]

3.3 $\sigma$  discrepancy

MSSM: extra contribution  $\rightarrow$  MSSM **may** explain this anomaly.

$$\left( a_\mu := \frac{g_\mu - 2}{2} \right)$$

■  $(g - 2)_\mu$  anomaly **PUSH UP**

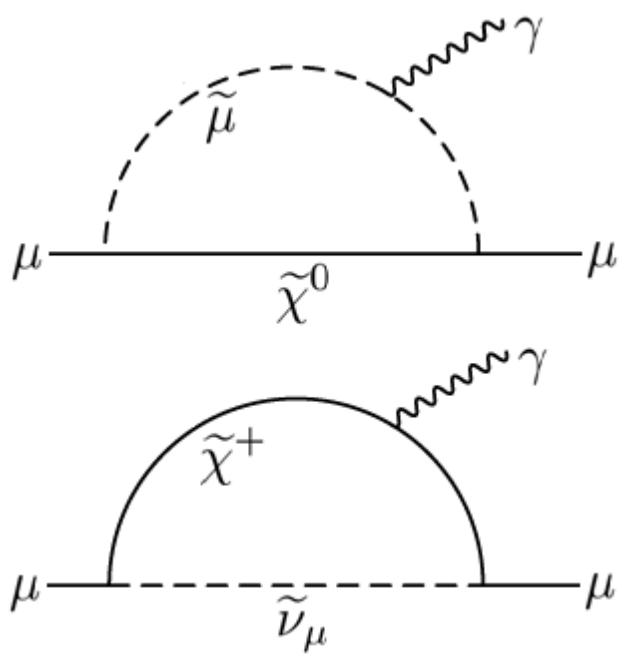


$$a_\mu^{\text{SM}} = (116\,591\,828 \pm 49) \times 10^{-11}$$

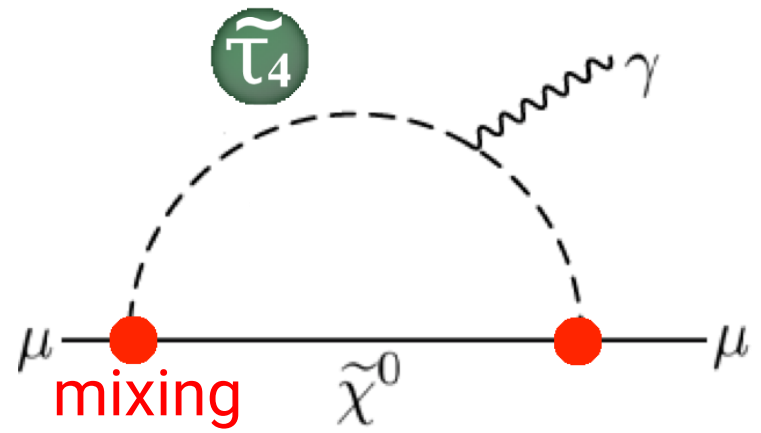
$$a_\mu^{\text{exp}} = (116\,592\,089 \pm 63) \times 10^{-11}$$

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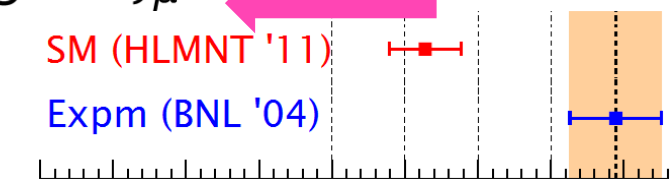
**4G extra contribution?**



$$\left( a_\mu := \frac{g_\mu - 2}{2} \right)$$

■  $(g - 2)_\mu$  anomaly

**PUSH DOWN**



$$a_\mu^{\text{SM}} = (116\,591\,828 \pm 49) \times 10^{-11}$$

$$a_\mu^{\text{exp}} = (116\,592\,089 \pm 63) \times 10^{-11}$$

Hagiwara, Liao, Martin, Nomura, Teubner [1105.3149]

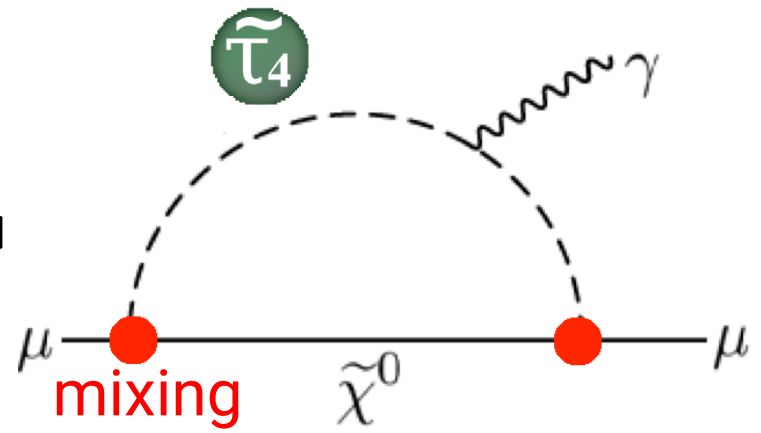
**3.3 $\sigma$  discrepancy**

MSSM: extra contribution  $\rightarrow$  MSSM **may** explain this anomaly.

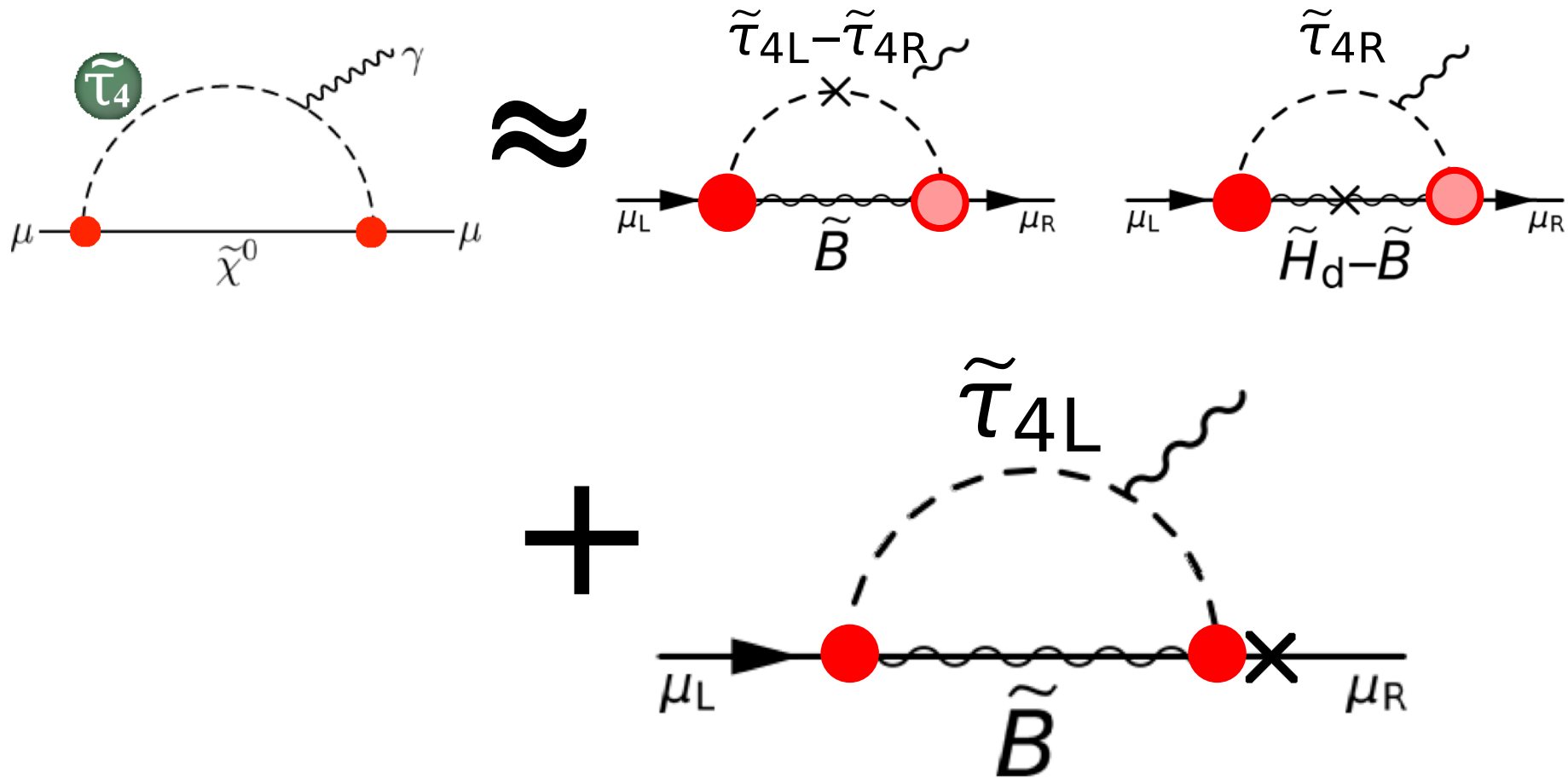
**4G extra contribution?**

0

$\geq$



■ Why always negative?

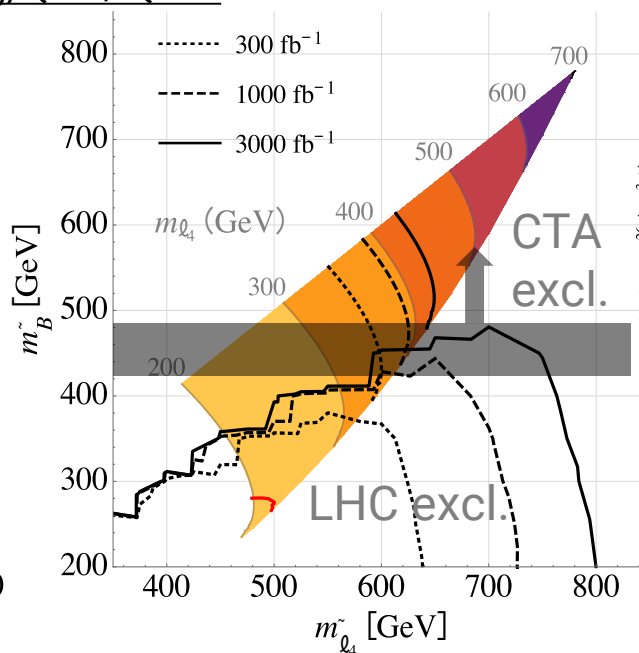
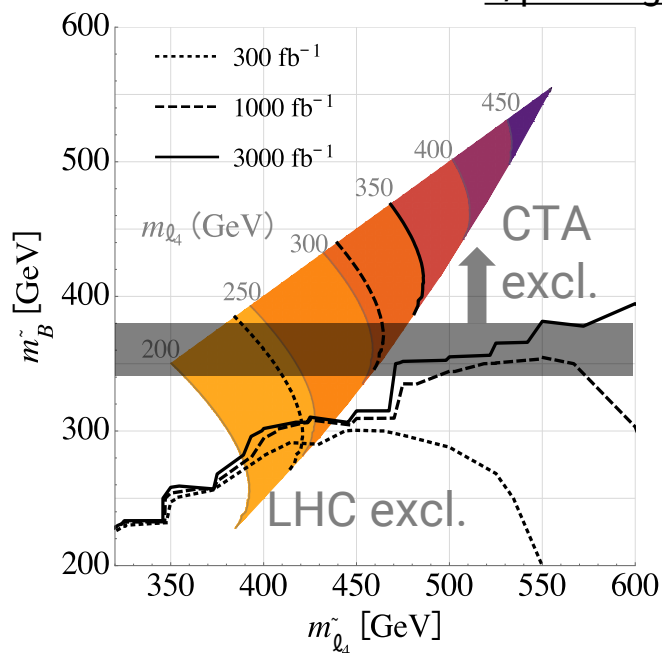


$$= -\frac{|\epsilon|^2}{16\pi^2} \frac{m_\mu^2}{6(|M_E|^2 + m_{\tilde{E}_c}^2)} N_1 \left( \frac{\mu^2}{|M_E|^2 + m_{\tilde{E}_c}^2} \right)$$

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CTA 500hr	covers $m_{\tilde{B}} > 340\text{--}380$ GeV		<b>full coverage</b>
HL-LHC (slepton)	covers $m_{\tilde{B}} < 400$ (480) GeV (but not “degenerate” region)		—
HL-LHC (lepton)	covers $m_{\tau_4} < 350$ (430) GeV equivalent to $m_{\tilde{B}} < 380$ (480) GeV		—

e/ $\mu$ -mixing, QUE / QDEE



$\tau$ / $\mu$ -mixing, QUE

