



MSSM 4G[📶] scenario

[Sho IWAMOTO](#) (岩本 祥)

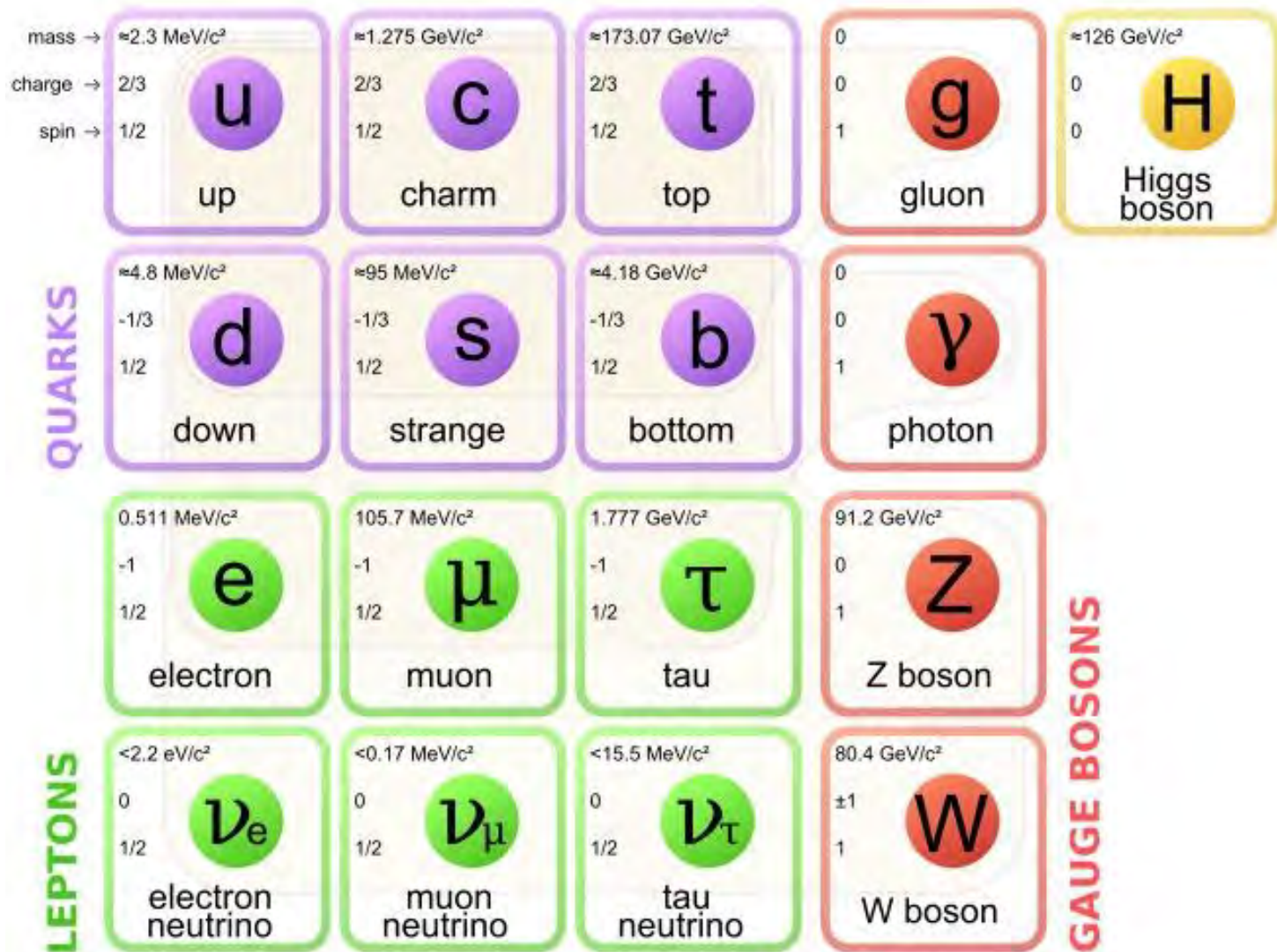
20 Sep. 2016

Seminar @ The University of Tokyo

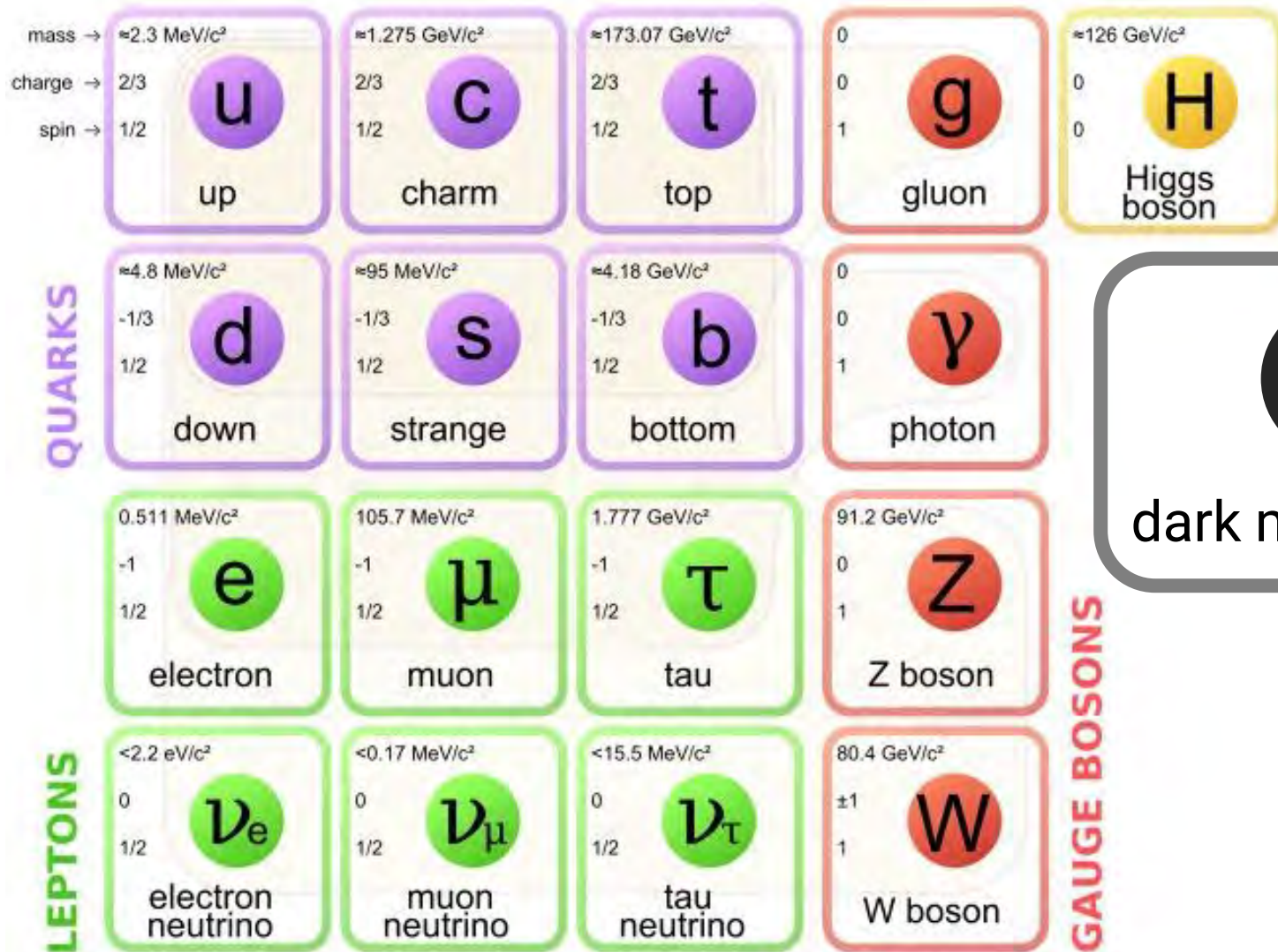
Based on [[1608.00283](#)] in collaboration with
M. Abdullah, J. L. Feng, and B. Lillard (UC Irvine)

The Standard Model of Particle Physics

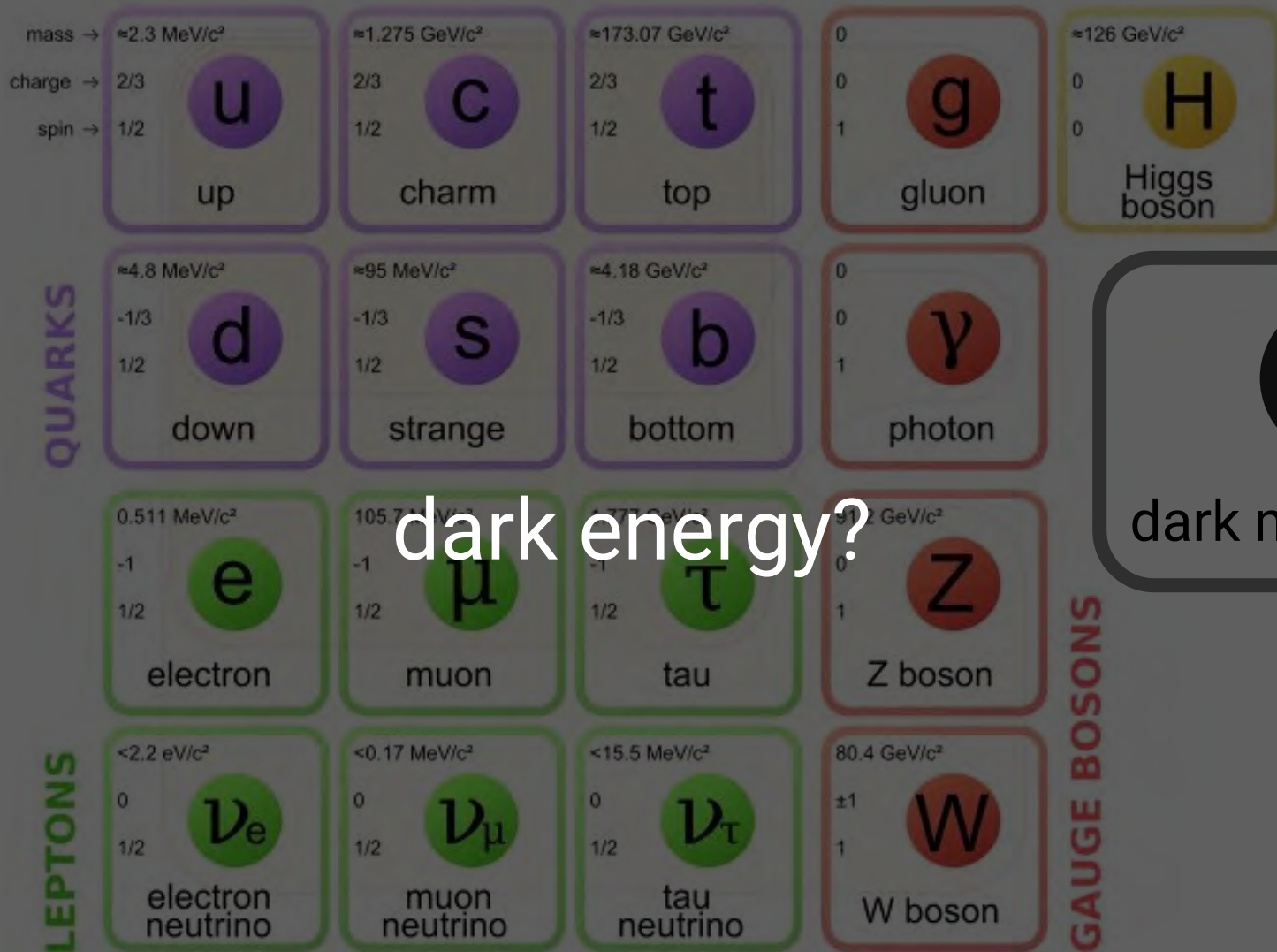
Universe =



Universe =



Universe =



dark energy?



Hints of “New Physics”

- Dark matter
- Dark energy
- Neutrino mass
- Gauge coupling unification
- Higgs mass (“naturalness”)
- Muon “ $g - 2$ ”
- ...

New Physics Candidates

-
-
-
-

etc...

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New Physics Candidates

- SUSY [supersymmetry]
 -
 -
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- etc...

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New Physics Candidates

- SUSY [supersymmetry]



Please fill this list
with your models
/ models you like



etc...

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New Physics Candidates

- SUSY [supersymmetry]
- Gauge-Higgs unification
- Hidden strong $SU(N)$
- etc...

Hints of “New Physics”

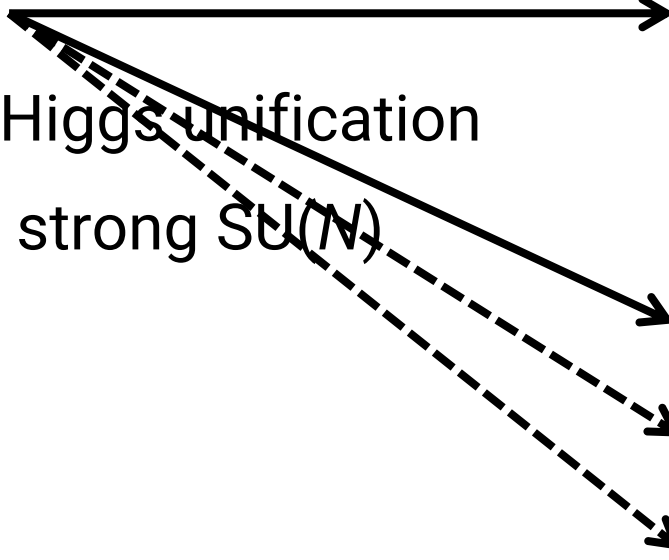
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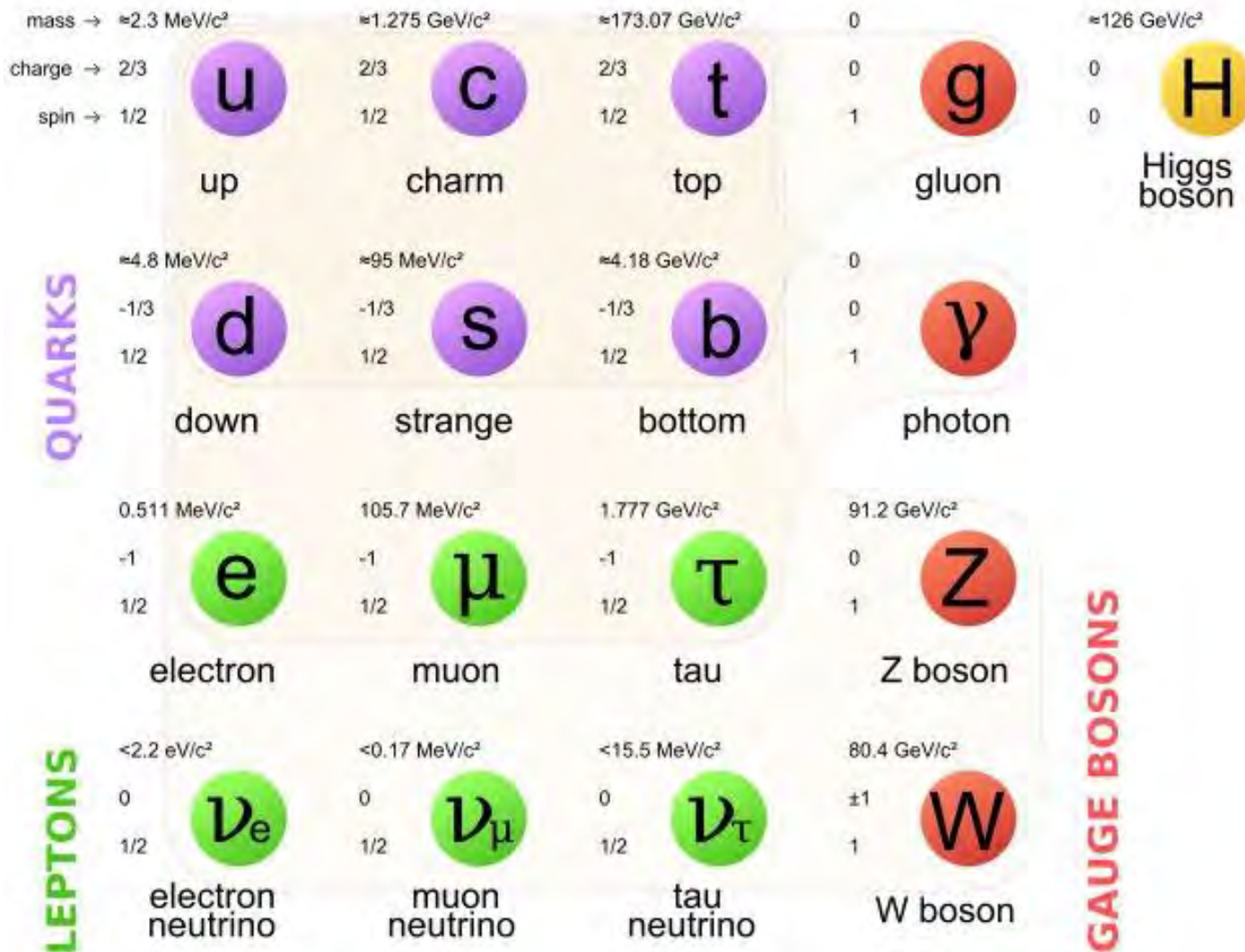
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■ SM =



■ MSSM =

[Minimal Supersymmetric Standard Model]

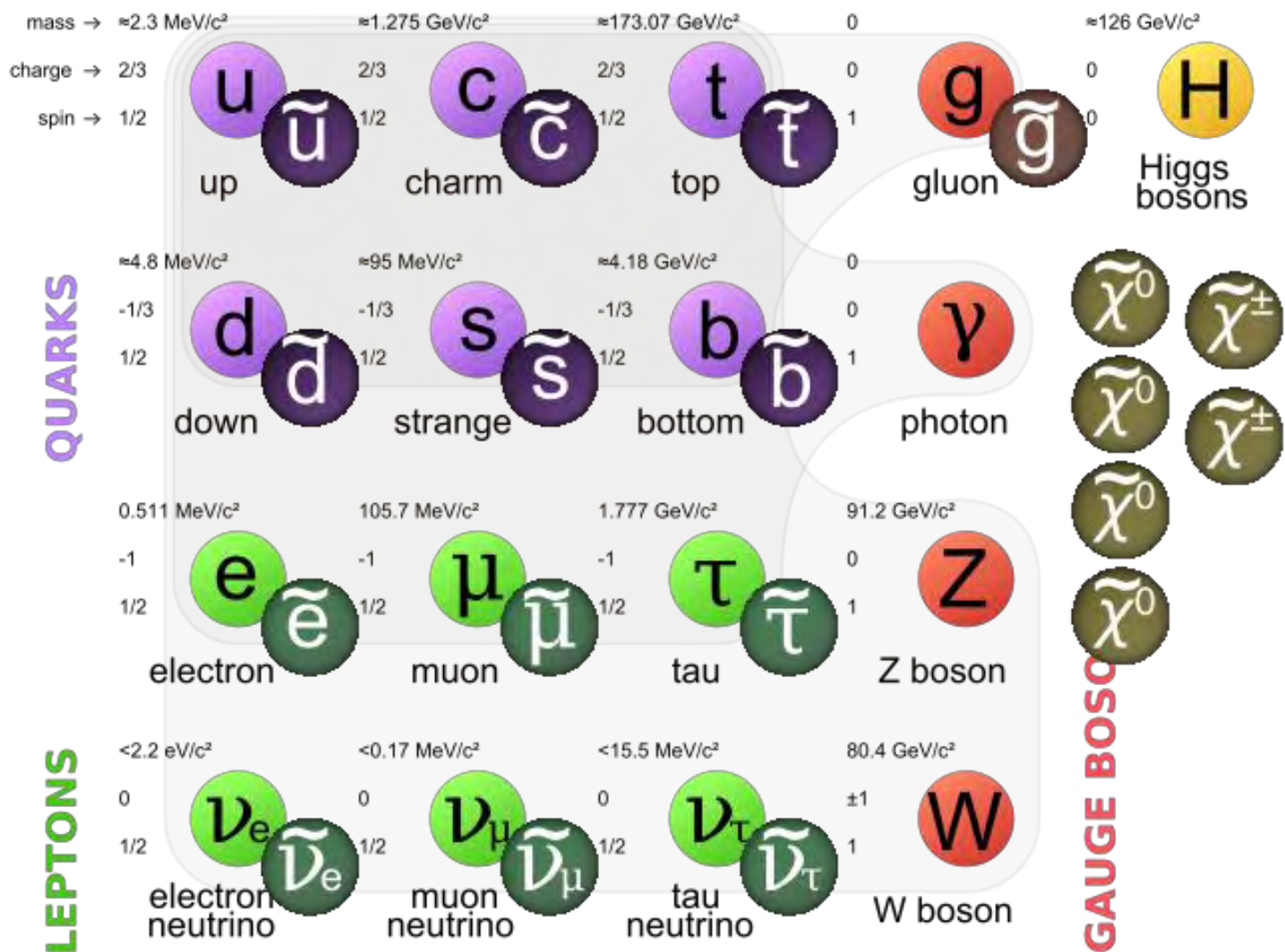


Image by [MissBJ](#) [CC BY 3.0], via [Wikimedia Commons](#) (changes were made by S.I)

New Physics Candidates

■ SUSY

Hints of “New Physics”

■ Dark matter

■ Dark energy

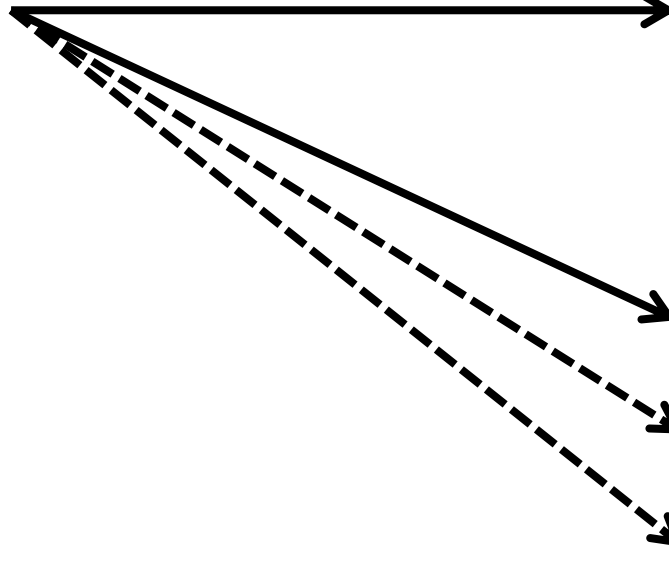
■ Neutrino mass

■ Gauge coupling unification

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■ Muon “ $g - 2$ ”

■ ...



New Physics Candidates

■ SUSY

Hints of “New Physics”

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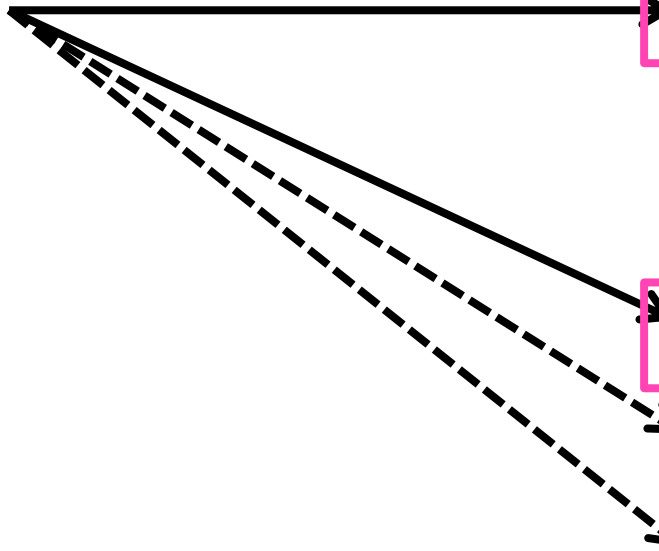
■ Neutrino mass

■ Gauge coupling unification

■ Higgs mass (“naturalness”)

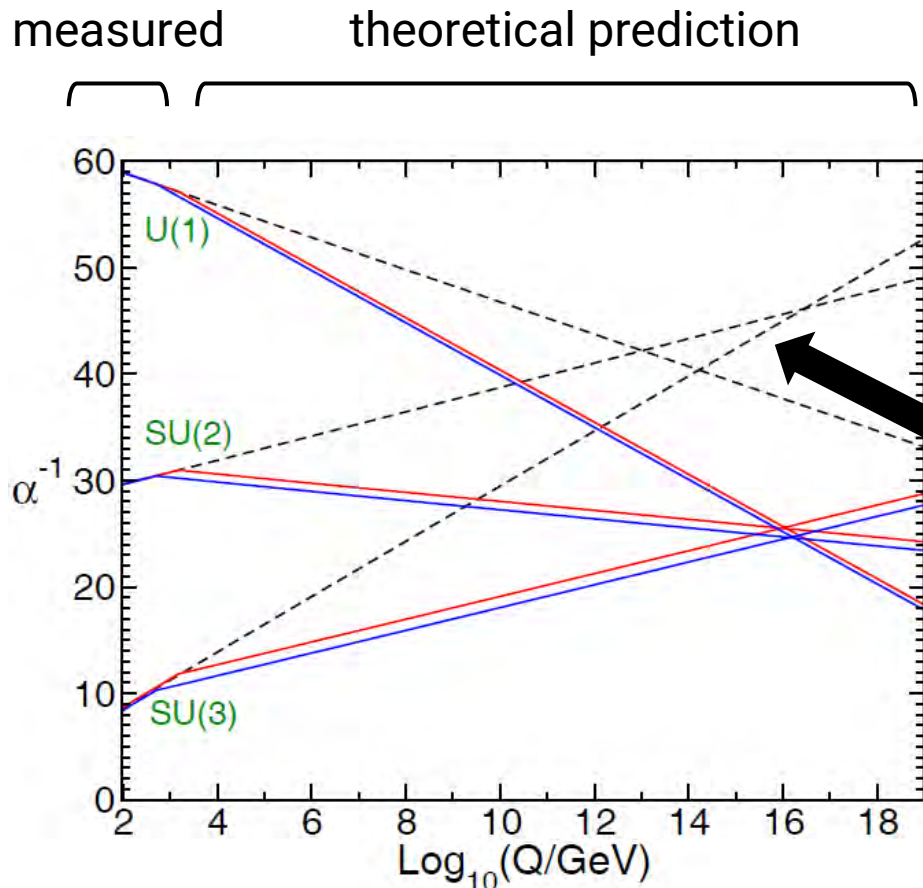
■ Muon “ $g - 2$ ”

■ ...



Gauge coupling unification

- SM \ni 3 forces : U(1), SU(2), SU(3) [Why three?]



Gauge coupling unification

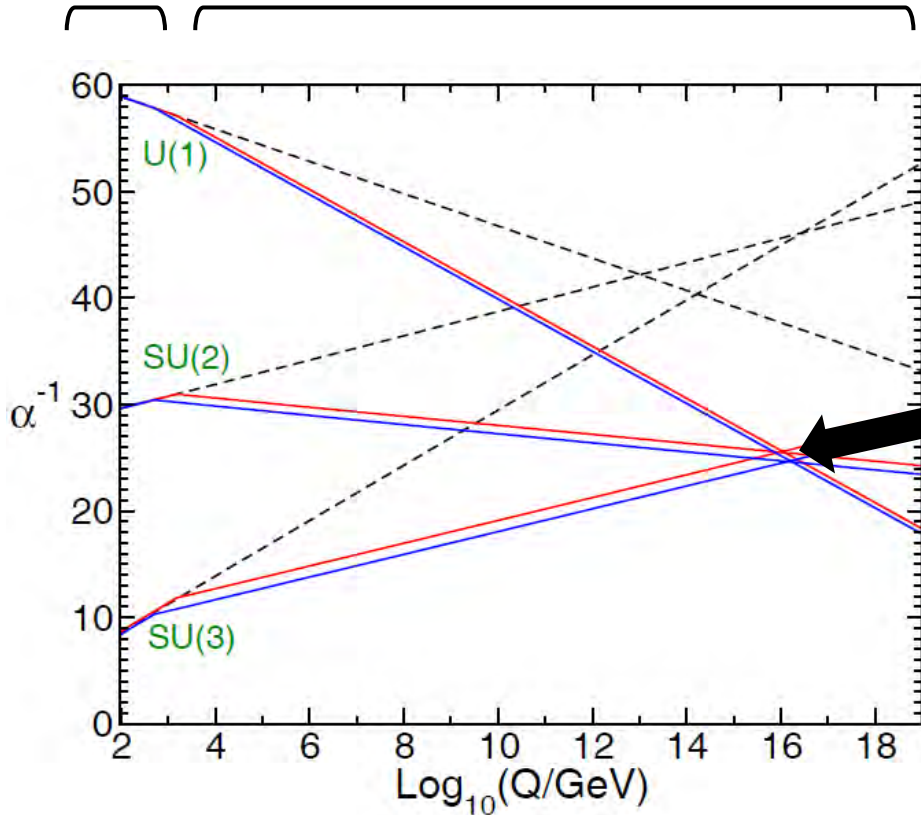
	mass \rightarrow $\approx 2.3 \text{ MeV}/c^2$	$\approx 1.275 \text{ GeV}/c^2$	$\approx 173.07 \text{ GeV}/c^2$	0	$\approx 126 \text{ GeV}/c^2$
charge \rightarrow	2/3	2/3	2/3	0	0
spin \rightarrow	1/2	1/2	1/2	1	0
QUARKS	u up	c charm	t top	g gluon	H Higgs boson
	$\approx 4.8 \text{ MeV}/c^2$	$\approx 95 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$	0	
	-1/3	-1/3	-1/3	0	
	1/2	1/2	1/2	1	
	d down	s strange	b bottom	γ photon	
LEPTONS	$0.511 \text{ MeV}/c^2$	$105.7 \text{ MeV}/c^2$	$1.777 \text{ GeV}/c^2$	$91.2 \text{ GeV}/c^2$	
	-1	-1	-1	0	
	1/2	1/2	1/2	1	
	e electron	μ muon	τ tau	Z Z boson	
	$< 2.2 \text{ eV}/c^2$	$< 0.17 \text{ MeV}/c^2$	$< 15.5 \text{ MeV}/c^2$	$80.4 \text{ GeV}/c^2$	
	0	0	0	± 1	
	1/2	1/2	1/2	1	
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	
					GAUGE BOSONS

Figure from S. P. Martin, *A Supersymmetry Primer*, [hep-ph/9709356](https://arxiv.org/abs/hep-ph/9709356)

Gauge coupling unification

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measured theoretical prediction



Gauge coupling unification

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	spin	1/2	1/2	1/2	0	0			
	u	\bar{u}	c	\bar{c}	t	\bar{t}	g	\bar{g}	H
	up	charm	top	gluon	Higgs bosons				
	d	\bar{d}	s	\bar{s}	b	\bar{b}	γ	$\tilde{\chi}^0$ $\tilde{\chi}^\pm$	
	down	strange	bottom	photon					
LEPTONS	mass \rightarrow	$\approx 4.8 \text{ MeV}/c^2$	$\approx 95 \text{ MeV}/c^2$	$\approx 1.777 \text{ GeV}/c^2$	0	$91.2 \text{ GeV}/c^2$			
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	e	\bar{e}	μ	$\bar{\mu}$	τ	$\bar{\tau}$	Z	$\tilde{\chi}^0$ $\tilde{\chi}^\pm$	
	electron	muon	tau	Z boson					
	ν_e	$\bar{\nu}_e$	ν_μ	$\bar{\nu}_\mu$	ν_τ	$\bar{\nu}_\tau$	W	$\tilde{\chi}^0$ $\tilde{\chi}^\pm$	
electron neutrino	muon neutrino	tau neutrino	W boson						
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	charge \rightarrow	0	0	0	± 1	± 1			
	spin	1/2	1/2	1/2	0	1			

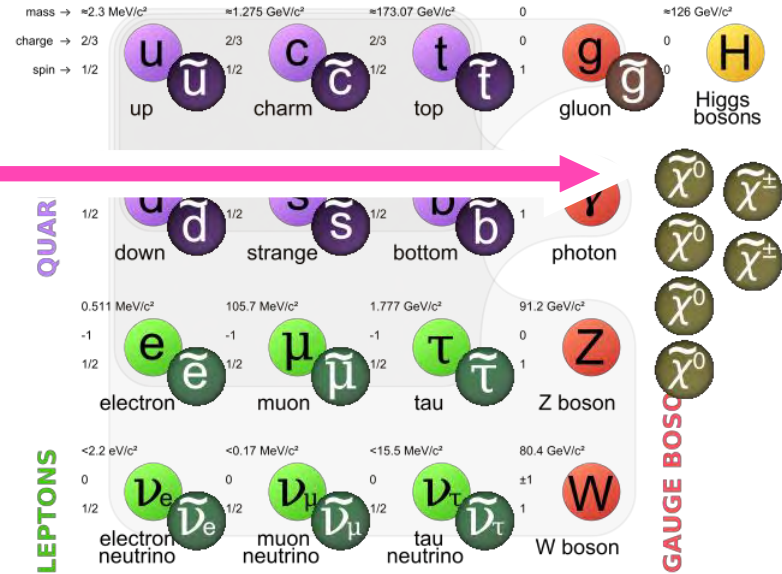
Figure from S. P. Martin, *A Supersymmetry Primer*, hep-ph/9709356

■ MSSM \ni Dark matter candidate



■ Dark matter?

- stable (at least 10^{10} yr)
- charge neutral
- density $\Omega h^2 = 0.12$
- not detected by astrophysics / direct search / LHC



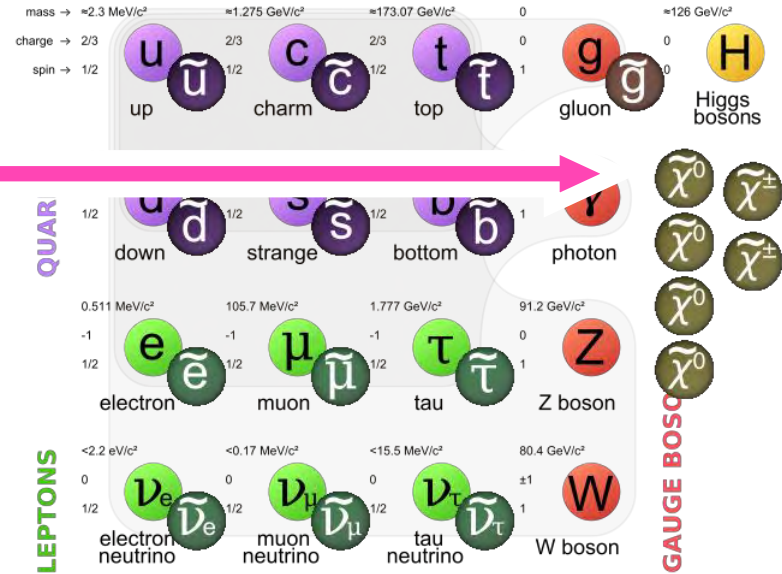
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if we introduce R-parity

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- MSSM \ni Dark matter candidate



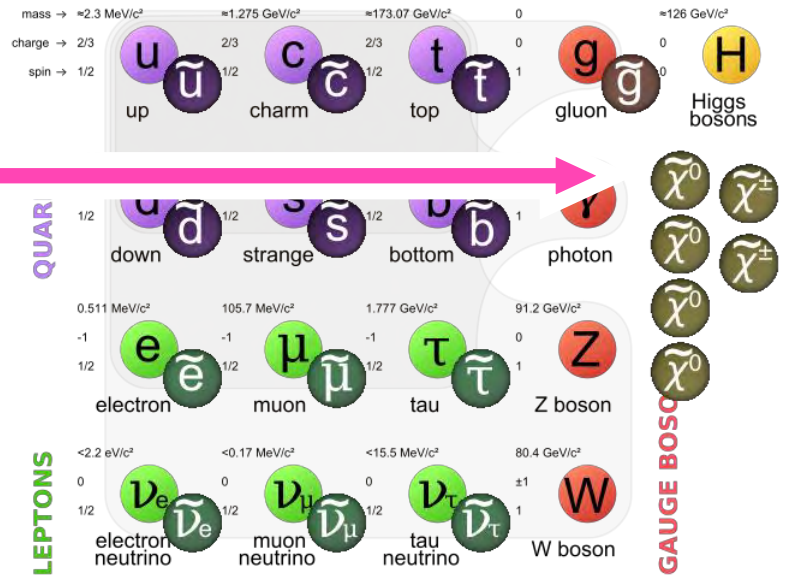
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$$\tilde{\chi}^0 = \tilde{B} \oplus \tilde{W}^0 \oplus \tilde{H}_d^0 \oplus \tilde{H}_u^0$$

- \tilde{B} -like?

→ “overabundant” problem

- \tilde{W} -like?

$$\Omega h^2 \gg 0.12$$

- \tilde{H} -like?

$$\tilde{\chi}^0 = \tilde{B} \oplus \tilde{W}^0 \oplus \tilde{H}_d^0 \oplus \tilde{H}_u^0$$

• \tilde{B} -like?

→ “overabundant” problem

• \tilde{W} -like?

$h^2 \sim 0.12$

• \tilde{H} -like?

MSSM 4G³ model

solves this problem!

Introduction: why overabundant?

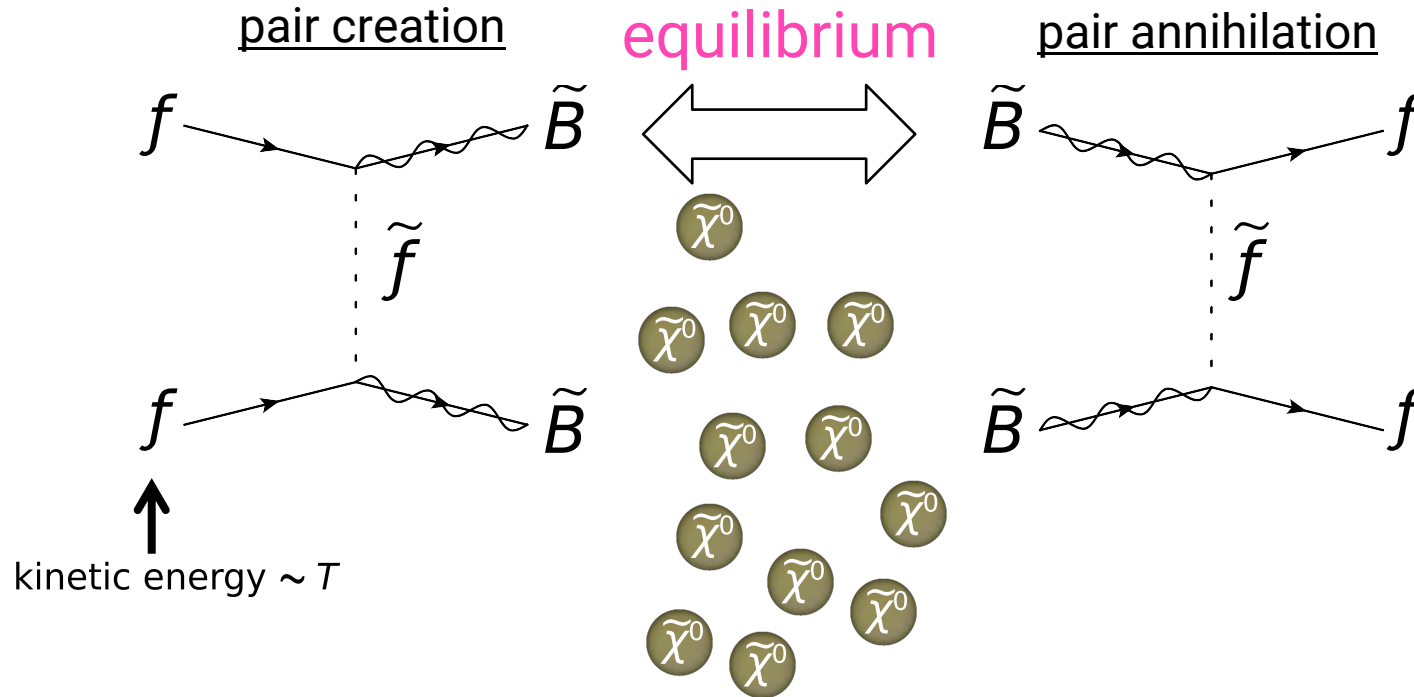
Model: **MSSM4G**  solves overabundance.

Analysis:

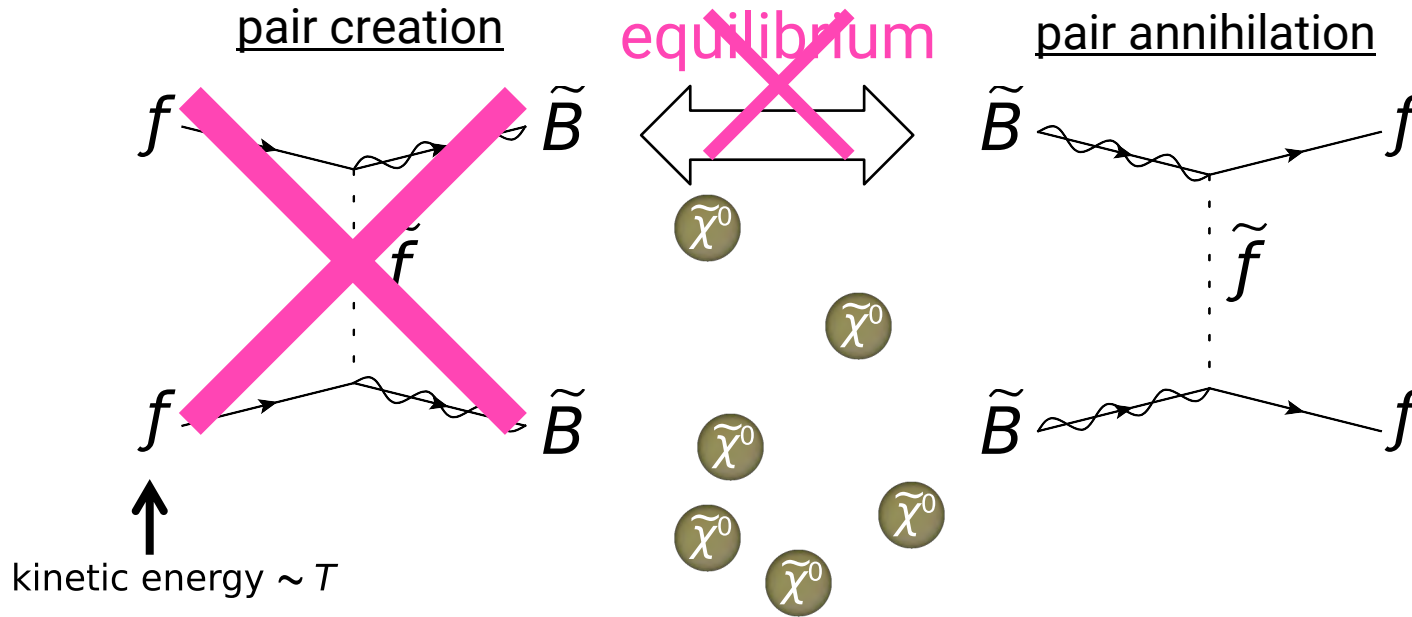
- cosmic rays (CTA, Fermi, MAGIC)
- colliders (LHC)
- direct detection (LUX)

Summary with discussion seeds

■ Early Universe with $T > m_{\tilde{B}}$



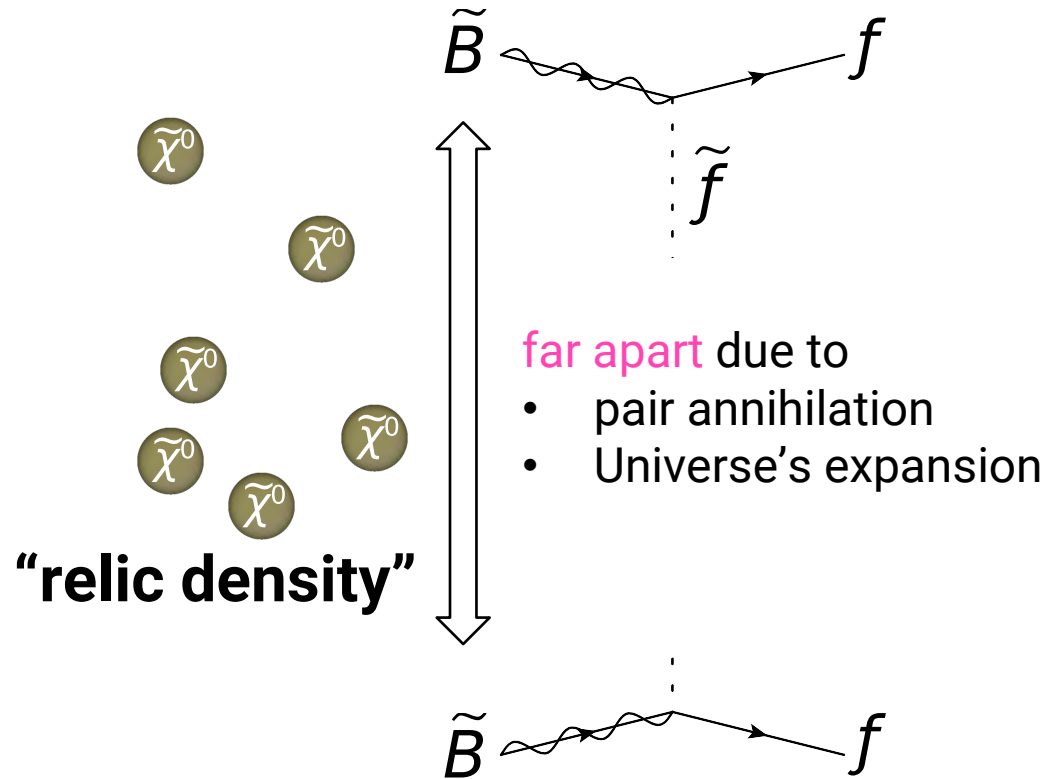
■ Early Universe with $T \lesssim m_{\tilde{B}}$



■ Early Universe with $T \lesssim m_{\tilde{B}}/20$

pair creation

pair annihilation



■ “observed” relic density Ωh^2

← “proper” crosssection $\langle \sigma v \rangle$ of $(DM)(DM) \rightarrow SM$

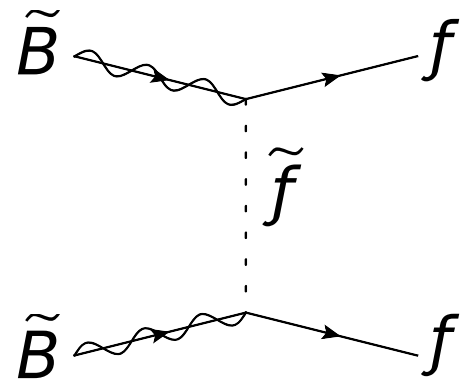
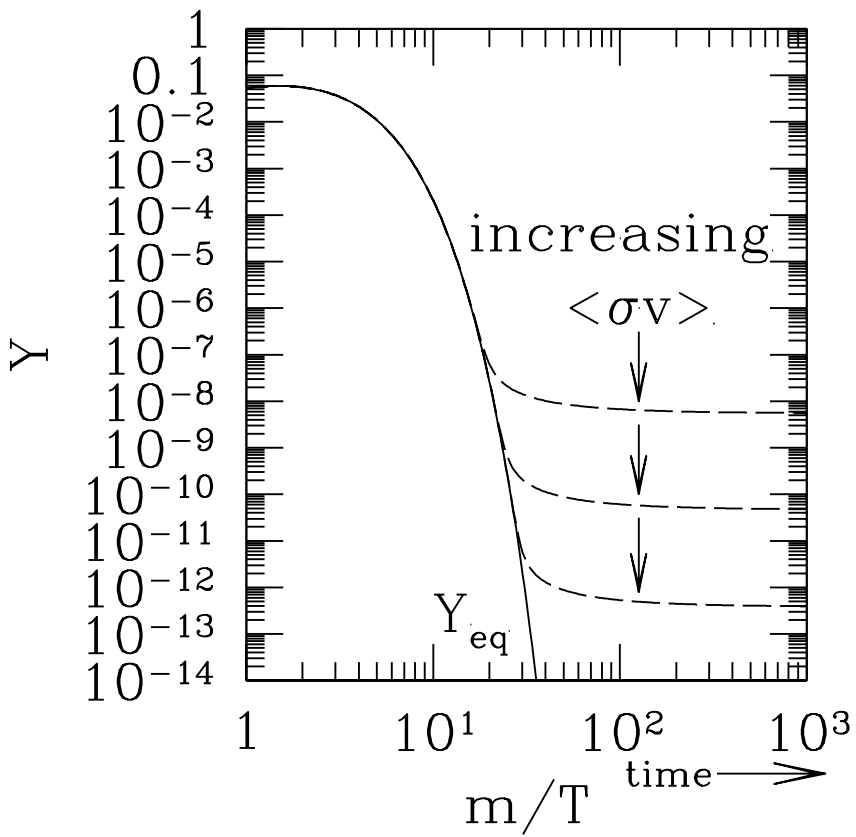


Figure from Gelmini and Gondolo, [1009.3690](https://arxiv.org/abs/1009.3690)

- “observed” relic density Ωh^2

← “proper” crosssection $\langle \sigma v \rangle$ of $(\text{DM})(\text{DM}) \rightarrow \text{SM}$

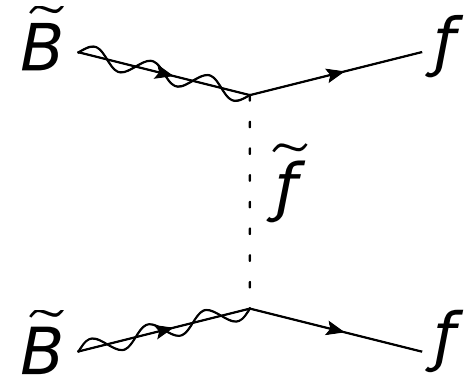
- pure \tilde{B} -DM (i.e., LSP $\tilde{\chi}^0$ is \tilde{B} -like)

➤ $\langle \sigma v \rangle$ strongly depends on $m_{\tilde{f}}$

↳ $m_{\tilde{f}} \sim 100 \text{ GeV}$

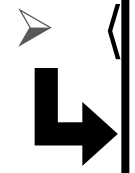
$m_{\tilde{f}} \gg 100 \text{ GeV} \implies \langle \sigma v \rangle$ too small

\implies “overabundant” problem

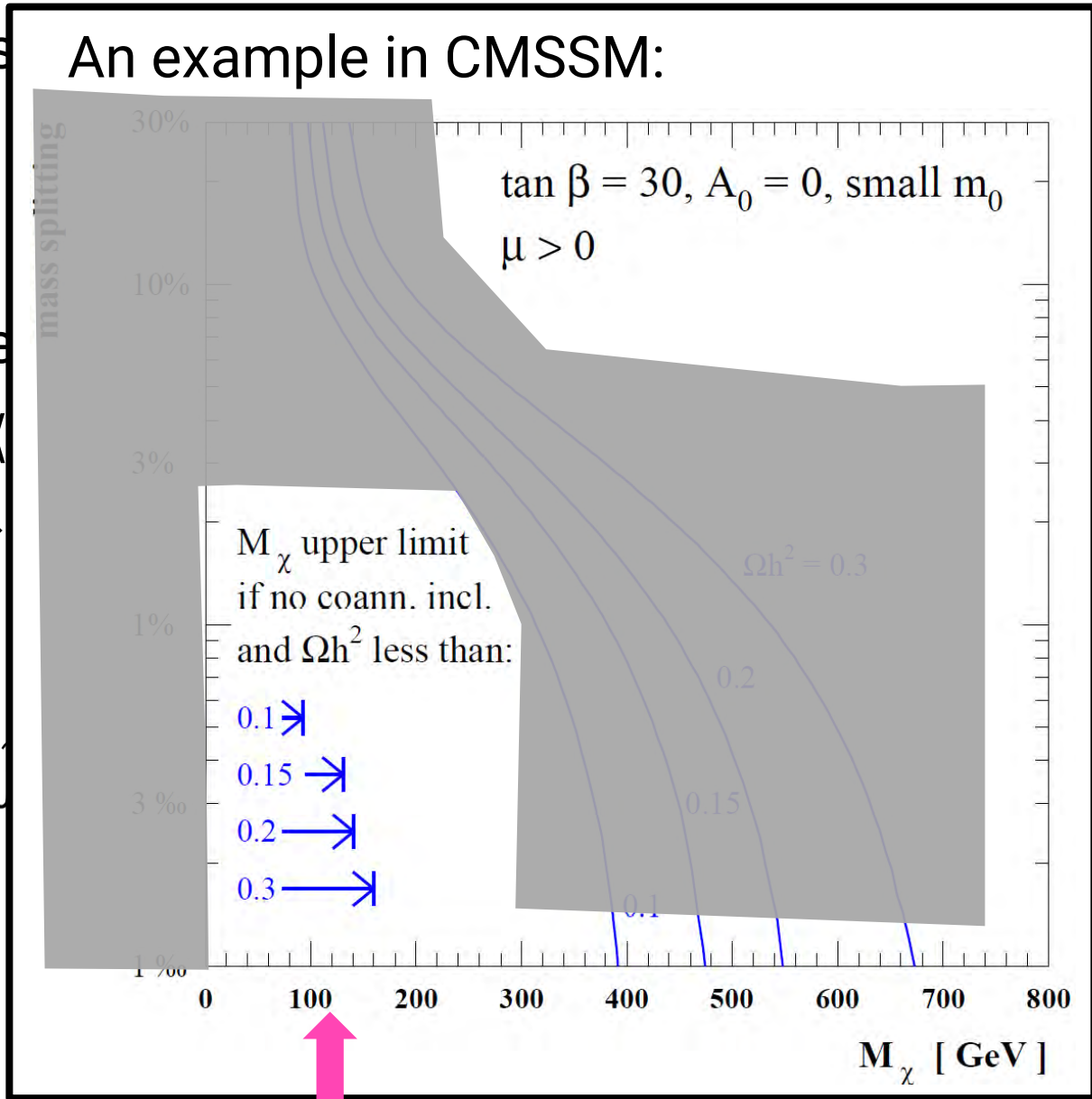


■ “obs

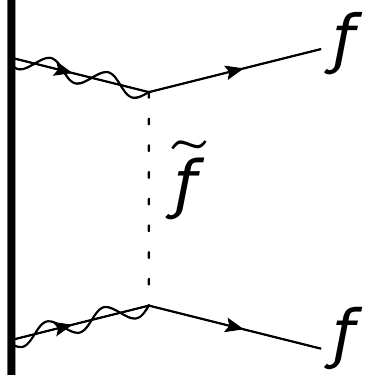
■ pure



$m_{\tilde{f}}$



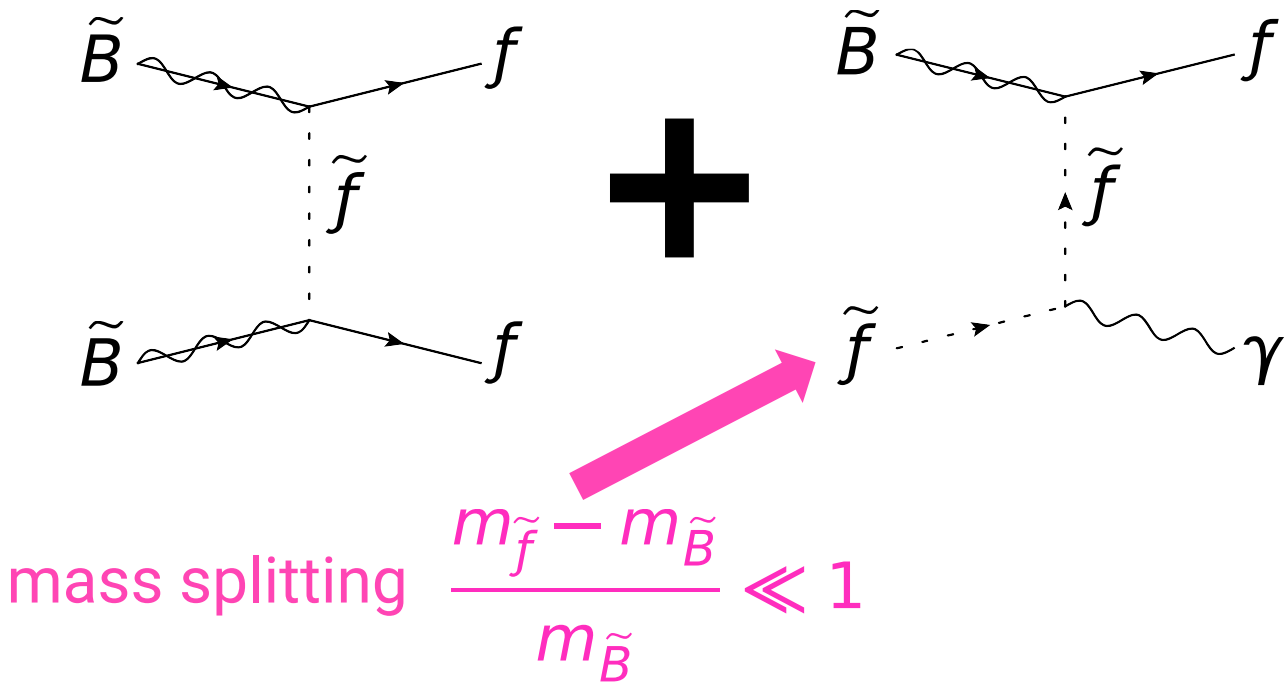
$\tilde{f} \rightarrow f + f$



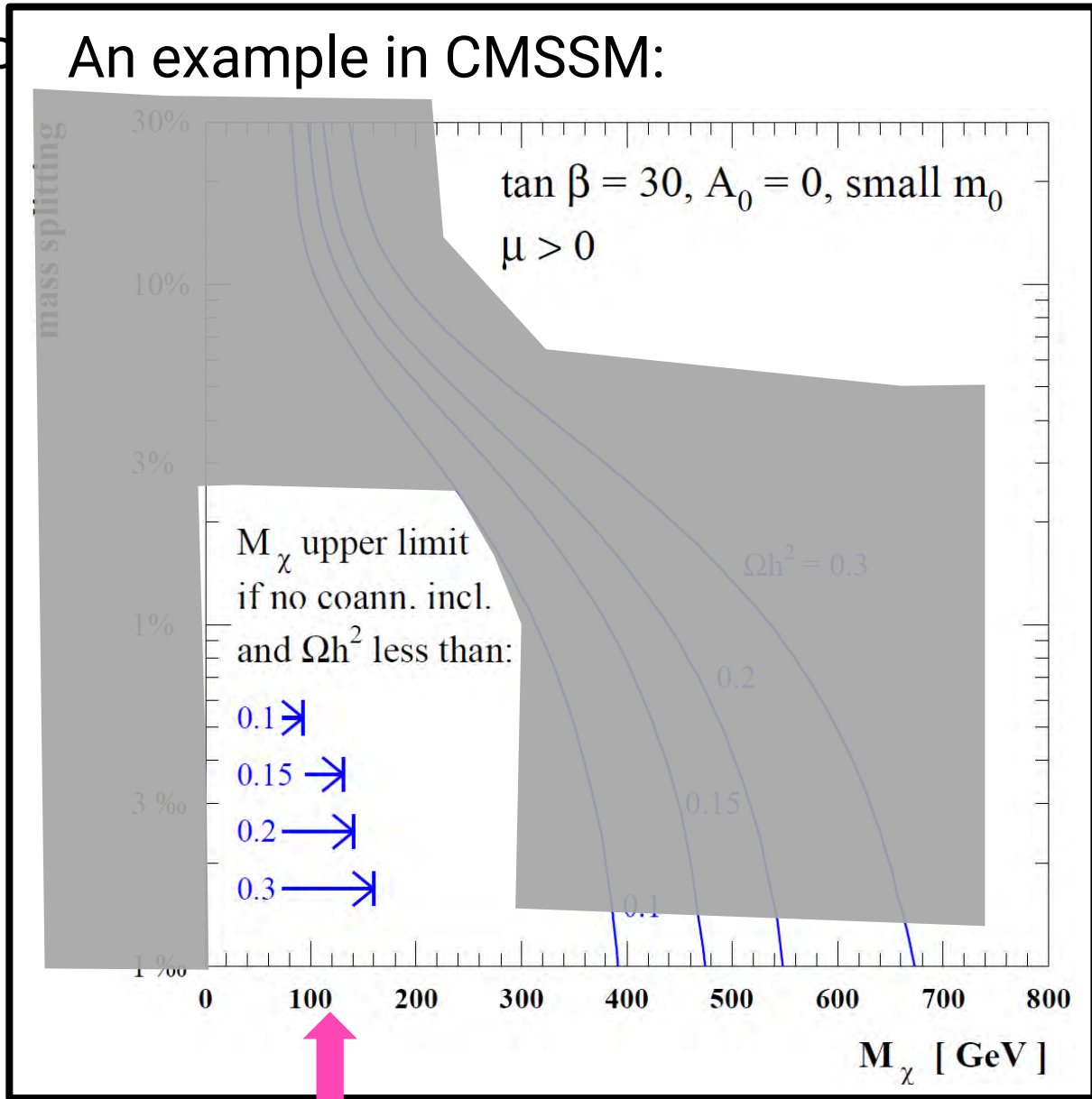
problem

Figure from Edsjö, Schelke, Ullio, Gondolo, hep-ph/0301106

- An old solution to increase $\langle \sigma v \rangle$: “co-annihilation”



■ An example in CMSSM:



on"

f

γ

Figure from Edsjö, Schelke, Ullio, Gondolo, hep-ph/0301106

■ An example in CMSSM with $\tilde{\tau}$ -coannihilation:

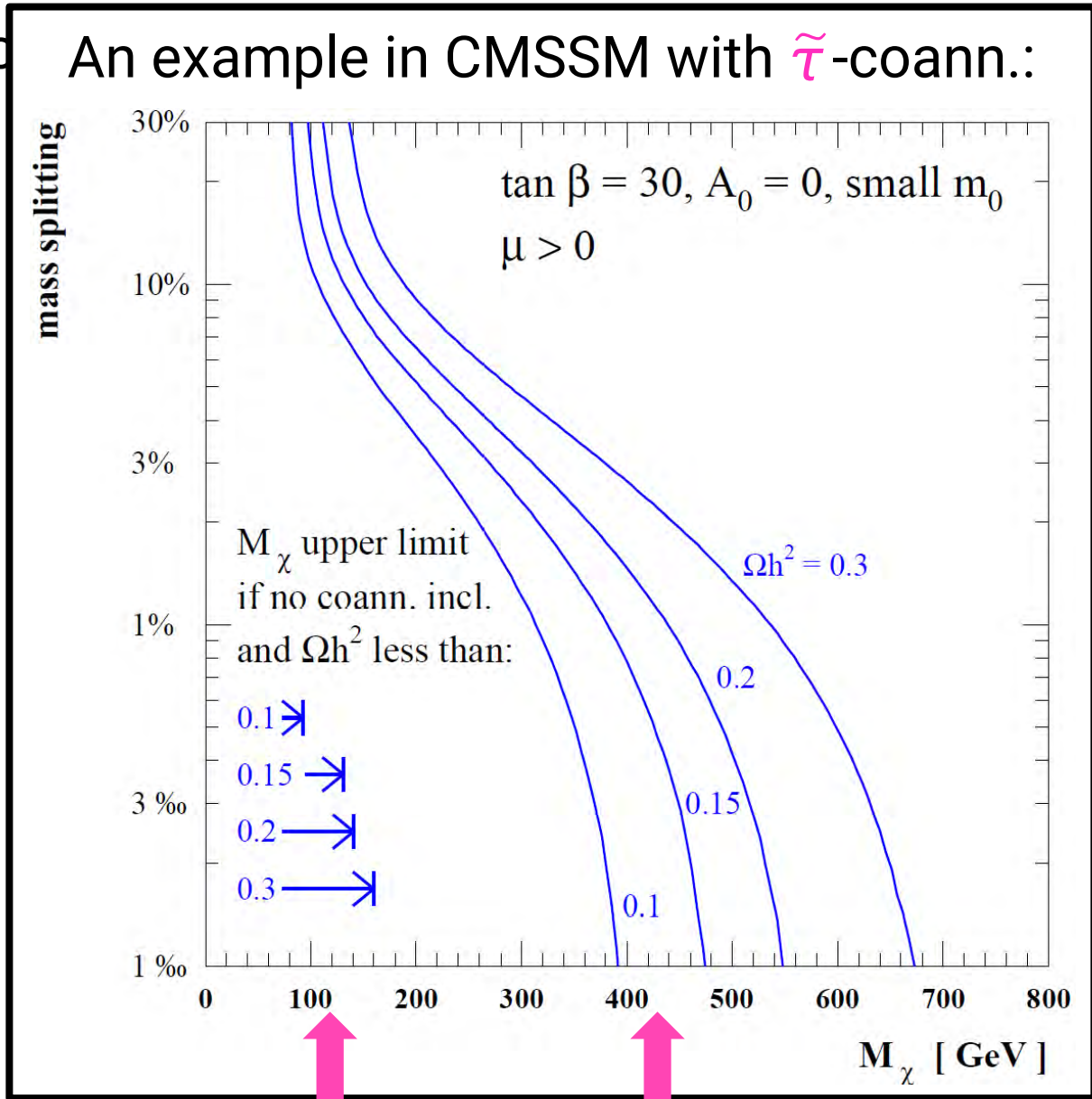


Figure from Edlö, Schelke, Ullio, Gondolo, hep-ph/0301106

Introduction: why overabundant?

Model: **MSSM4G**  solves overabundance.

Analysis:

- cosmic rays (CTA, Fermi, MAGIC)
- colliders (LHC)
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Summary with discussion seeds

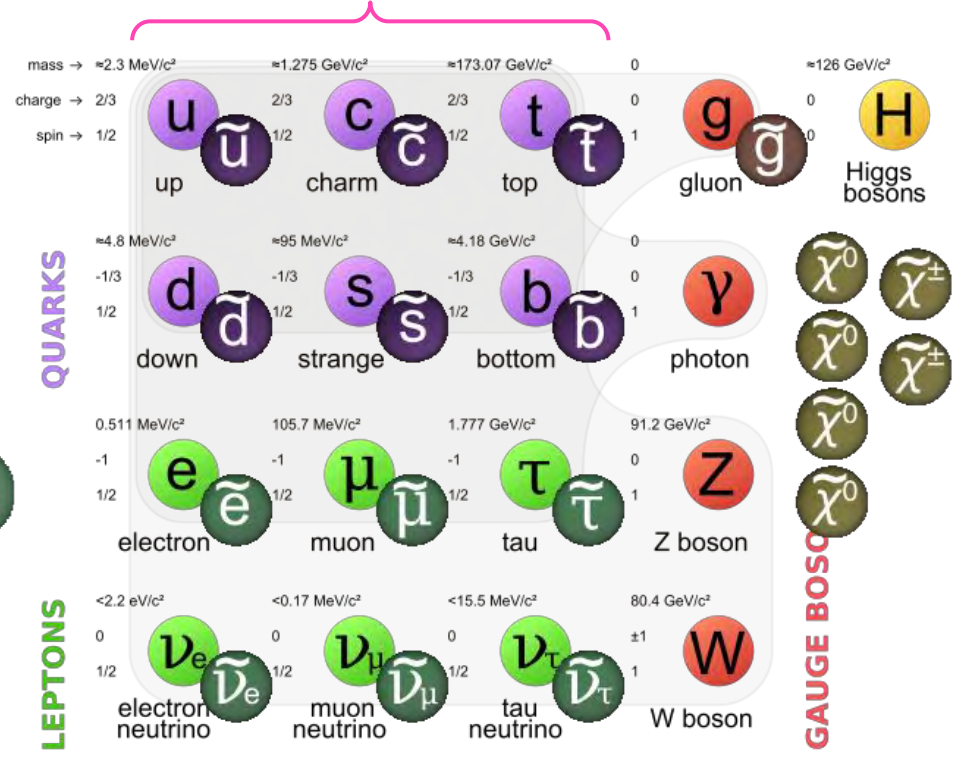
■ MSSM = 3G generations

+

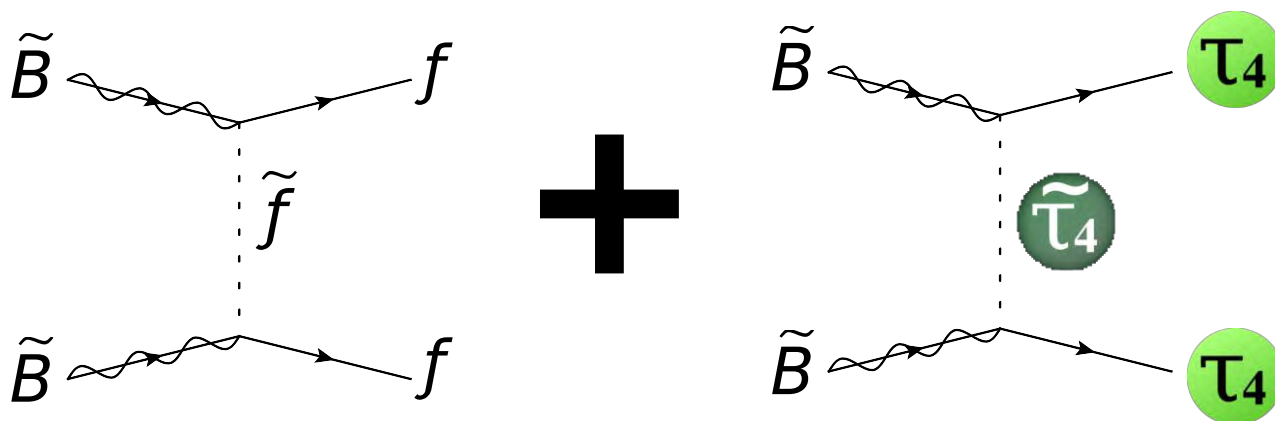
extra vector-like
4th-Generation lepton

||

MSSM4G



- A new solution to increase $\langle\sigma v\rangle$: MSSM4G



extra annihilation channel

→ larger Ωh^2

→ “proper” $\langle\sigma v\rangle$

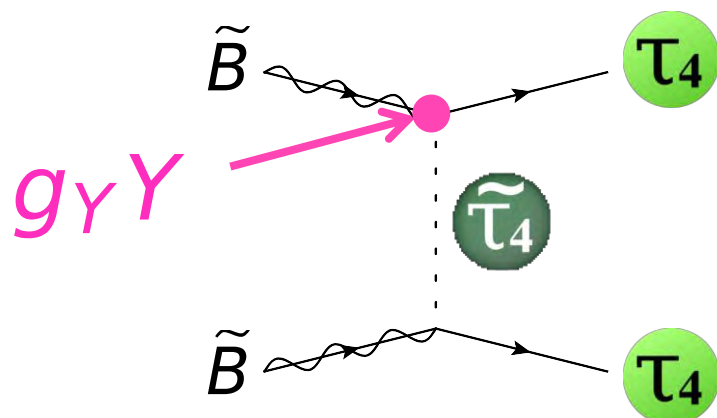
if $\tau_{\tilde{4}} \gtrsim \tilde{B} > \tau_4$

$$\langle\sigma v\rangle = \frac{g_Y^4 Y_L^2 Y_R^2 m_f^2}{2\pi m_{\tilde{B}}} \frac{\sqrt{m_{\tilde{B}}^2 - m_f^2}}{(m_{\tilde{B}}^2 + m_{\tilde{f}}^2 - m_f^2)^2}$$

$$(Q_i, \bar{U}_i, \bar{D}_i, L_i, \bar{E}_i) + (H_u, H_d) \quad [\text{MSSM}]$$

$(i = 1 \dots 3)$

$$+ (E_4, \bar{E}_4) \quad [\text{MSSM4G}]$$



$$\Rightarrow \langle \sigma \nu \rangle \propto Y^4$$

	SU(3) _{color}	SU(2) _{weak}	U(1) _Y
Q_i	3	2	1/6
\bar{U}_i	$\bar{3}$	1	-2/3
\bar{E}_i	1	1	1
\bar{D}_i	$\bar{3}$	1	1/3
L_i	1	2	-1/2
H_u	1	2	1/2
H_d	1	2	-1/2
\bar{E}_4	1	1	1
E_4	1	1	-1

$$W = Y_u H_u Q \bar{U} + Y_d H_d Q \bar{D} + Y_e H_d L \bar{E}$$

$$+ M_{E_4} E_4 \bar{E}_4 + \epsilon_i H_d L_i \bar{E}_4$$

[vector-like mass]

[mixing with SM leptons]

■ MSSM + $E\bar{E}$ → breaks coupling unification

■ QUE model : MSSM + $Q\bar{Q}U\bar{U}E\bar{E}$

✓ gauge coupling unification

✓ SU(5) GUT

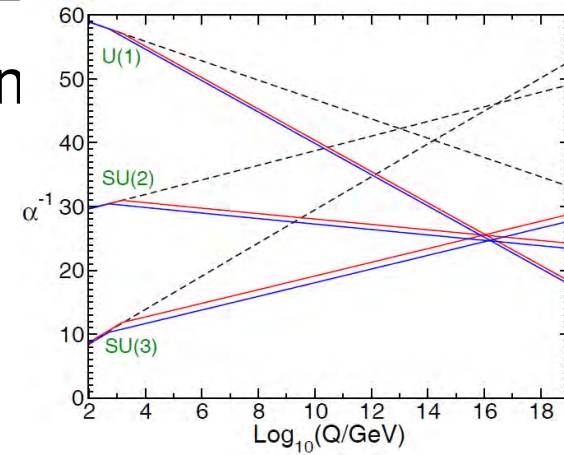
➤ extra $H_u Q_4 \bar{U}_4$ interaction → m_h **UP**

■ QDEE model : MSSM + $Q\bar{Q}D\bar{D}E\bar{E}E\bar{E}$

✓ gauge coupling unification

✗ SU(5) GUT

➤ extra $H_d Q_4 \bar{D}_4$ coupling → m_h slightly **UP**



■ MSSM + $E\bar{E}$ → breaks coupling unification

■ QUE model : MSSM + $Q\bar{Q}U\bar{U}E\bar{E}$

⇒ MSSM + $T_4, B_4, t_4, \tau_4,$

$\tilde{T}_{4L}, \tilde{T}_{4R}, \tilde{B}_{4L}, \tilde{B}_{4R}, \tilde{t}_{4L}, \tilde{t}_{4R}, \tilde{\tau}_{4L}, \tilde{\tau}_{4R}$

■ QDEE model : MSSM + $Q\bar{Q}D\bar{D}E\bar{E}E\bar{E}$

⇒ MSSM + $T_4, B_4, b_4, \tau_4, \tau_5,$

$\tilde{T}_{4L}, \tilde{T}_{4R}, \tilde{B}_{4L}, \tilde{B}_{4R}, \tilde{b}_{4L}, \tilde{b}_{4R}, \tilde{\tau}_{4L}, \tilde{\tau}_{4R}, \tilde{\tau}_{5L}, \tilde{\tau}_{5R}$

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assumed to be “decoupled” (very heavy)
and we will ignore them.

■ QDEE model : MSSM + $Q\bar{Q}D\bar{D}E\bar{E}E\bar{E}$

⇒ MSSM + ~~$T_4, B_4, b_4, \tau_4, \tau_5,$~~

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Other working assumptions

- $M_1 \ll \mu \ll M_2$
→ LSP $\tilde{\chi}_1^0$ is \tilde{B} -like
- All the other SUSY particles & extra Higgses are decoupled.

■ MSSM + $E\bar{E}$ → breaks coupling

■ QUE model : MSSM + $Q\bar{Q}U\bar{U}E\bar{E}$

⇒ SM + $\tilde{\chi}_1^0 (\approx \tilde{B})$, τ_4 ,
 $\underbrace{\tilde{\tau}_{4L}, \tilde{\tau}_{4R}}_{\text{assumed to be equal-mass}}$

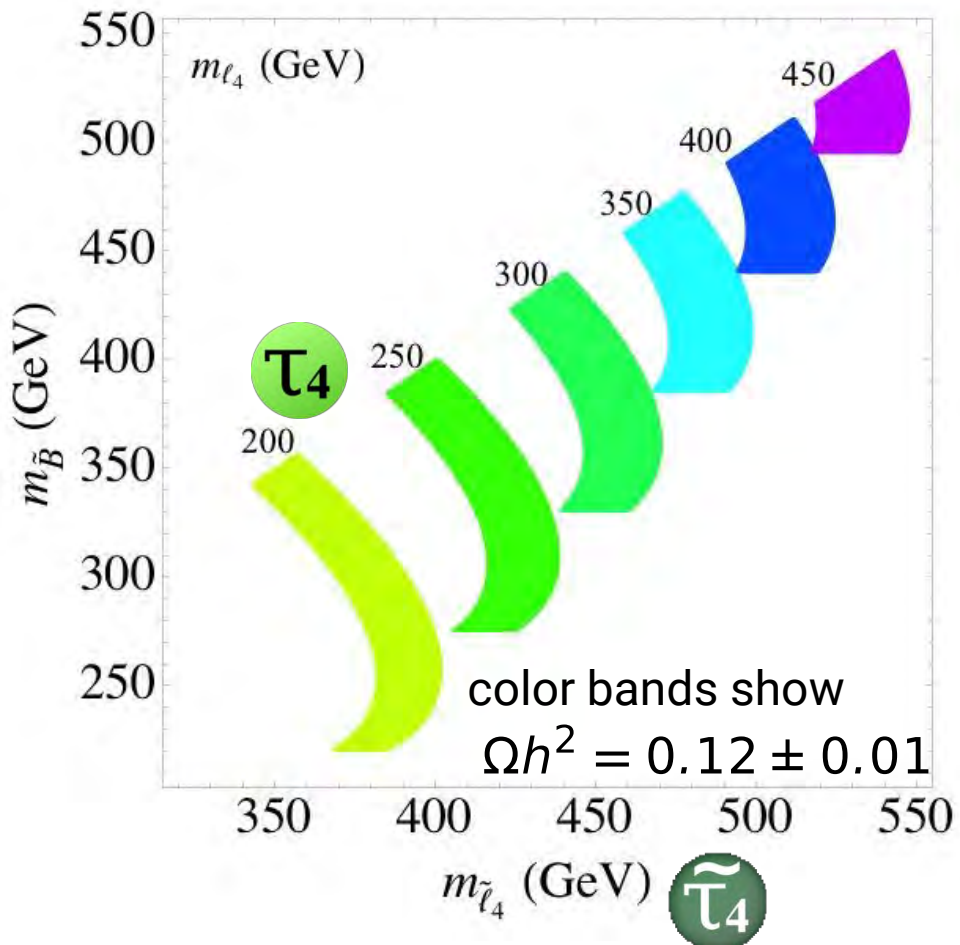
■ QDEE model : MSSM + $Q\bar{Q}D\bar{D}E\bar{E}E\bar{E}$

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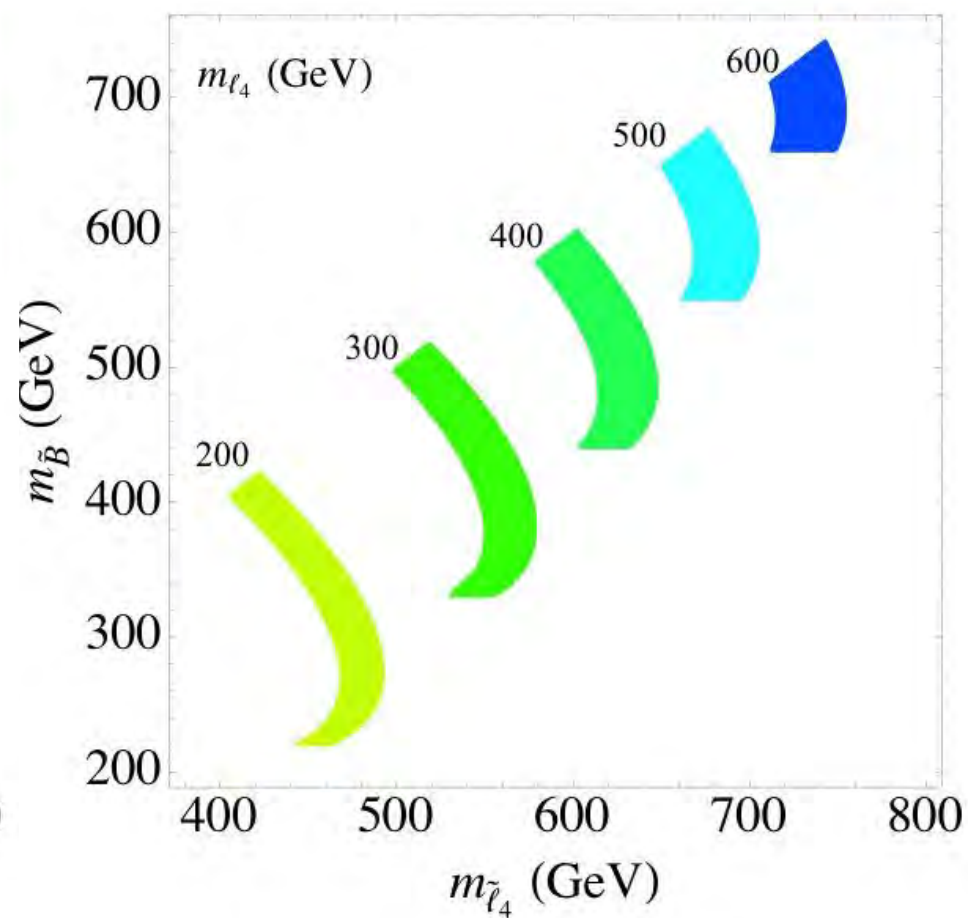
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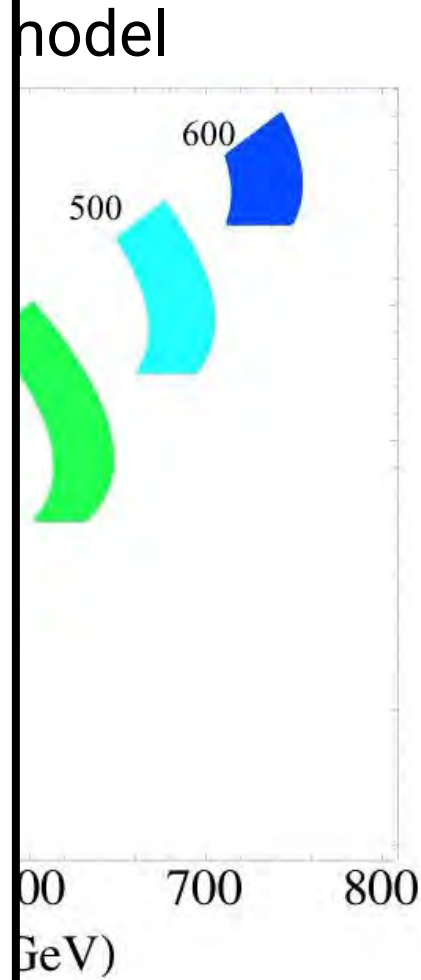
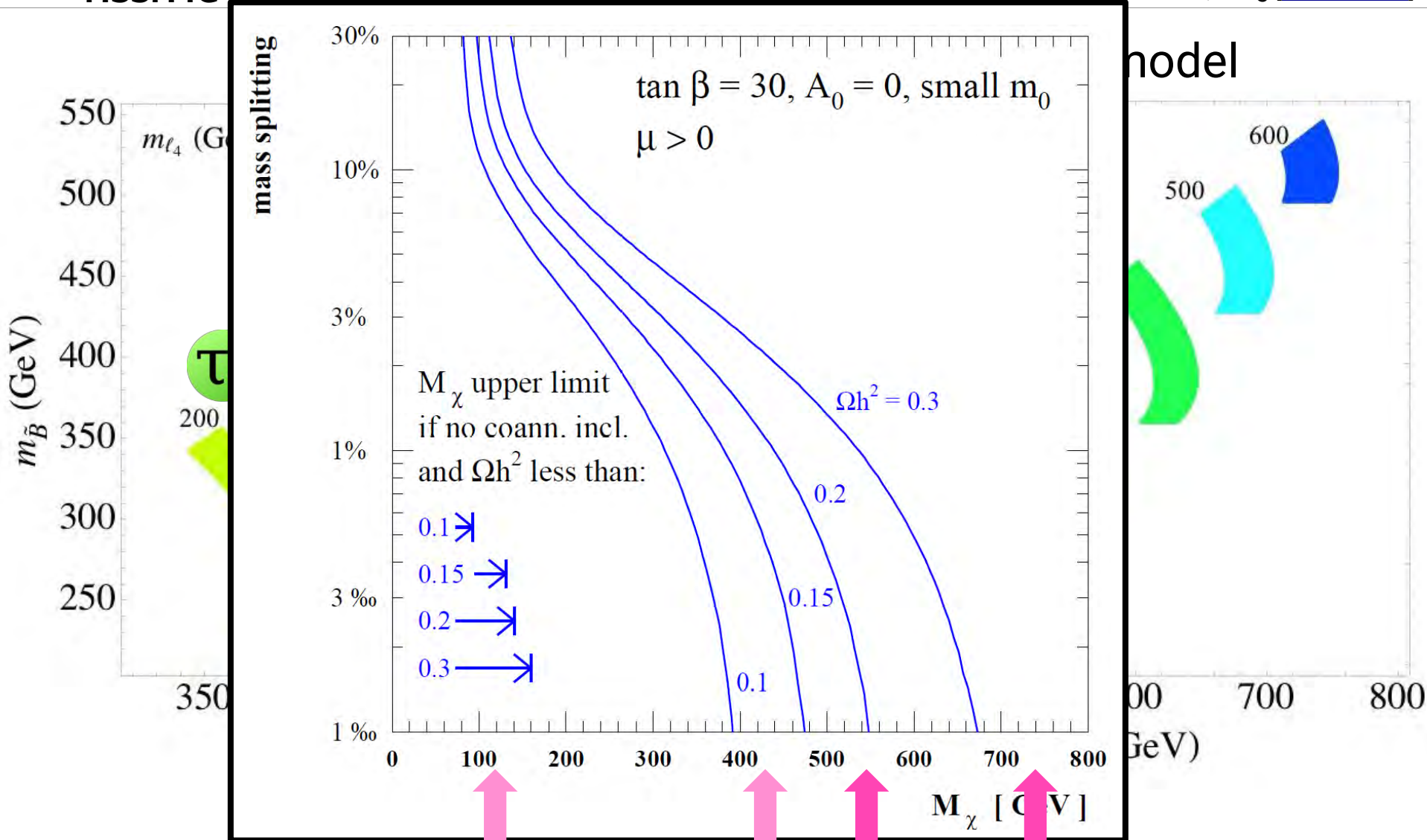
QUE model



QDEE model



$$\tilde{\tau}_4 \gtrsim \tilde{B} > \tau_4$$



$\tilde{\tau}_4 \gtrsim \tilde{B} > \tau_4$

vanilla stau-coann. QUE QDEE

Introduction: why overabundant?

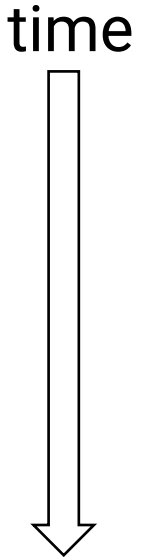
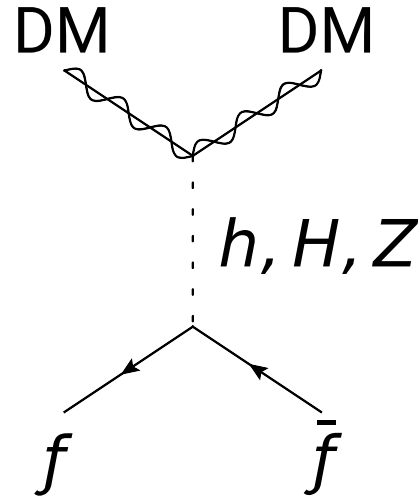
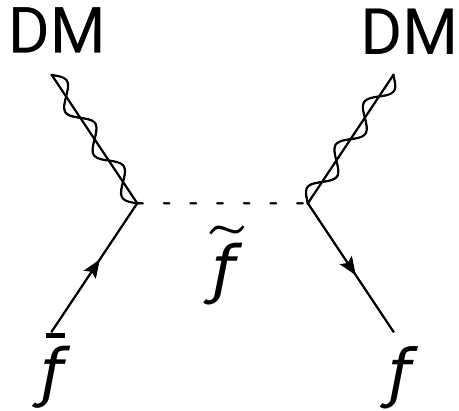
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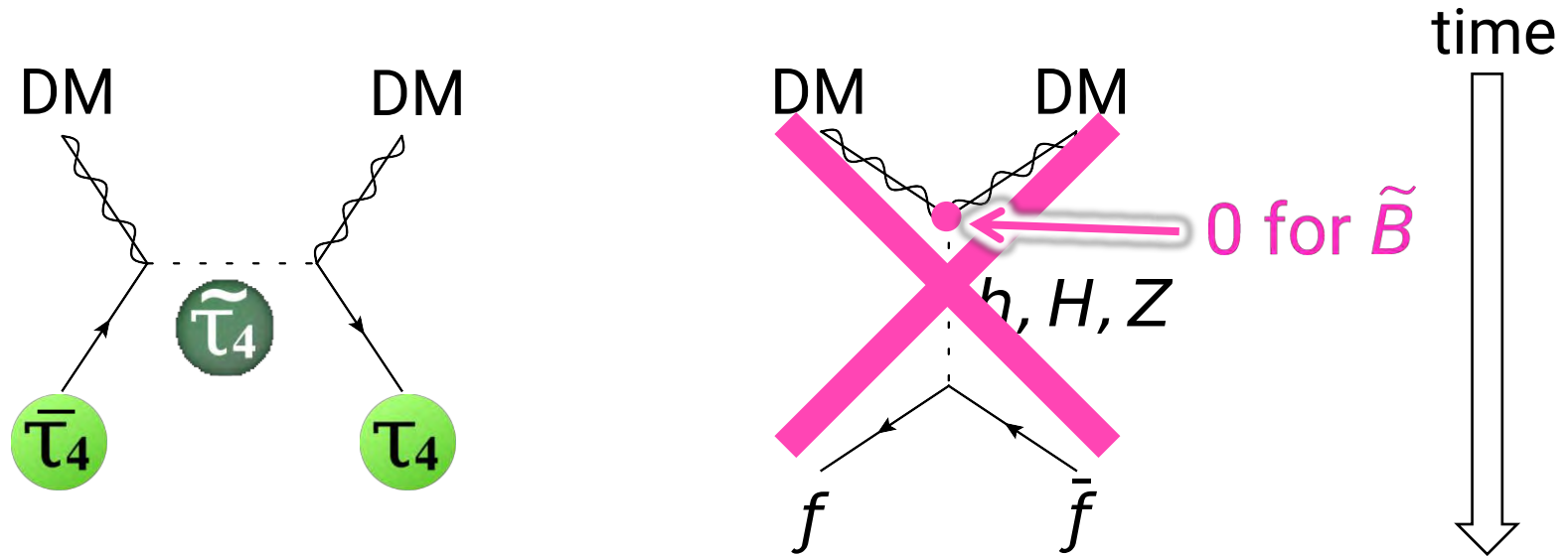
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- direct detection (LUX)

Summary with discussion seeds

- DM indirect detection (= searches for DM annihilation)



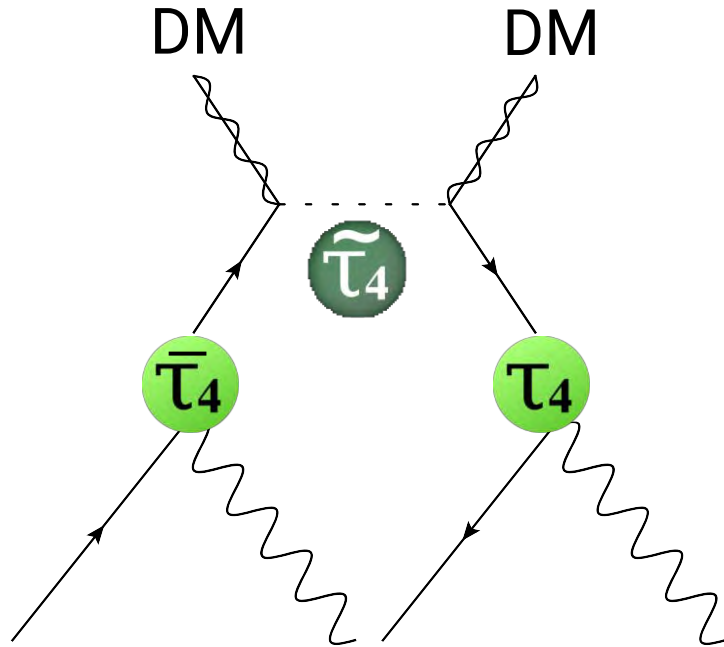
- DM indirect detection (= searches for DM annihilation)



$$\langle \sigma v \rangle = \frac{g_Y^4 Y_L^2 Y_R^2}{2\pi} \frac{m_f^2}{m_{\tilde{B}}^2} \frac{\sqrt{m_{\tilde{B}}^2 - m_f^2}}{(m_{\tilde{B}}^2 + m_f^2 - m_f^2)^2}$$

(in convention of $Q = T_3 + Y$)

- DM indirect detection (= searches for $DM DM \rightarrow \tau_4 \bar{\tau}_4$)



$$\tau_4 \rightarrow \begin{cases} W + \nu \\ Z + l \\ h + l \end{cases} \quad \left(\begin{array}{l} \nu = \nu_e, \nu_\mu, \nu_\tau \\ l = e, \mu, \tau \end{array} \right)$$

$$W\nu : Zl : hl \sim 2 : 1 : 1$$

$$W \ni Y_e H_d L \bar{E} + M_{E_4} E_4 \bar{E}_4 + \epsilon_i H_d L_i \bar{E}_4$$

[vector-like mass] [mixing with SM leptons]

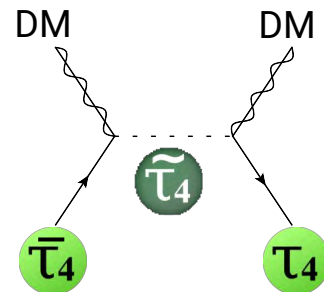
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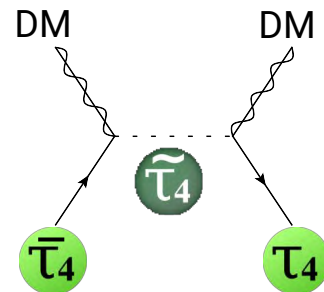


	DM DM →
$\tau_{4(5)}$ mixes with e	$W^+W^- \quad ZZ \quad hh \quad \nu\bar{\nu} \quad e^+e^-$
$\tau_{4(5)}$ mixes with μ	$W^+W^- \quad ZZ \quad hh \quad \nu\bar{\nu} \quad \mu^+\mu^-$
$\tau_{4(5)}$ mixes with τ	$W^+W^- \quad ZZ \quad hh \quad \nu\bar{\nu} \quad \tau^+\tau^-$

■ DM indirect detection

$$W \ni Y_e H_d L \bar{E} + M_{E_4} E_4 \bar{E}_4 + \epsilon_i H_d L_i \bar{E}_4$$

$$W\nu : Zl : Hl \sim 2 : 1 : 1$$

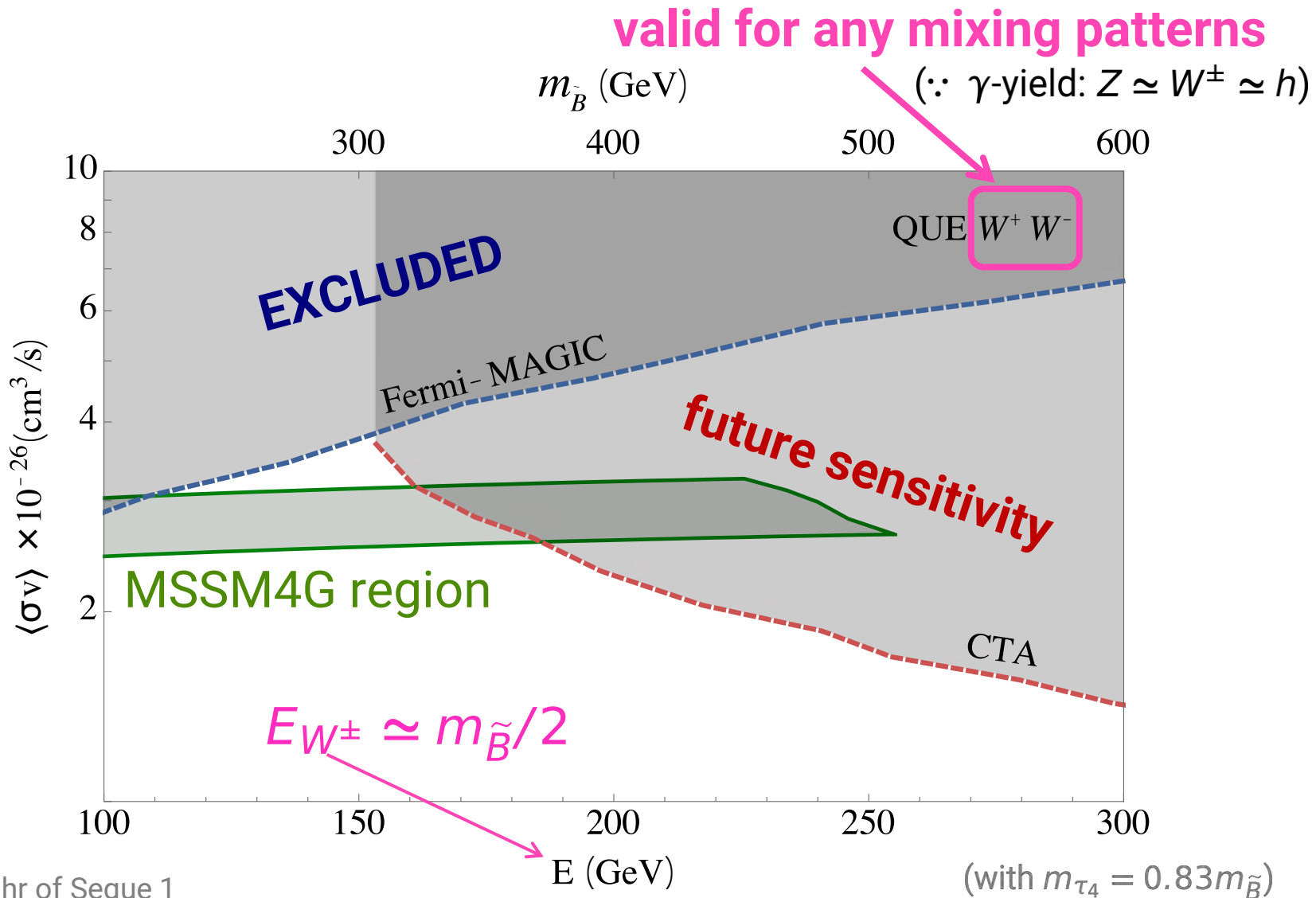


insensitive (IceCube)

	DM DM →				less sensitive / large BKG uncertainty
$\tau_{4(5)}$ mixes with e	W^+W^-	ZZ	hh	$\nu\bar{\nu}$	e^+e^-
$\tau_{4(5)}$ mixes with μ	W^+W^-	ZZ	hh	$\nu\bar{\nu}$	$\mu^+\mu^-$
$\tau_{4(5)}$ mixes with τ	W^+W^-	ZZ	hh	$\nu\bar{\nu}$	$\tau^+\tau^-$

→ ... → γ

→ π^0 → γ



MAGIC: 158 hr of Segue 1

Fermi-LAT: 6 yr of 15 dSph (incl. Segue 1)

DM profile: NFW

Fermi-LAT dominates MAGIC in almost all E -range.

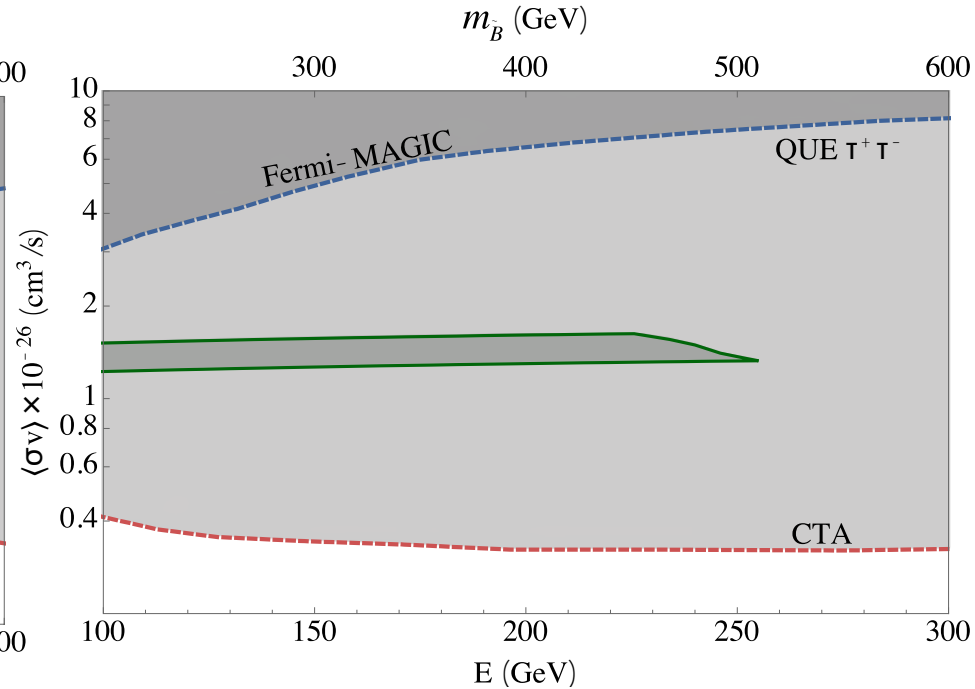
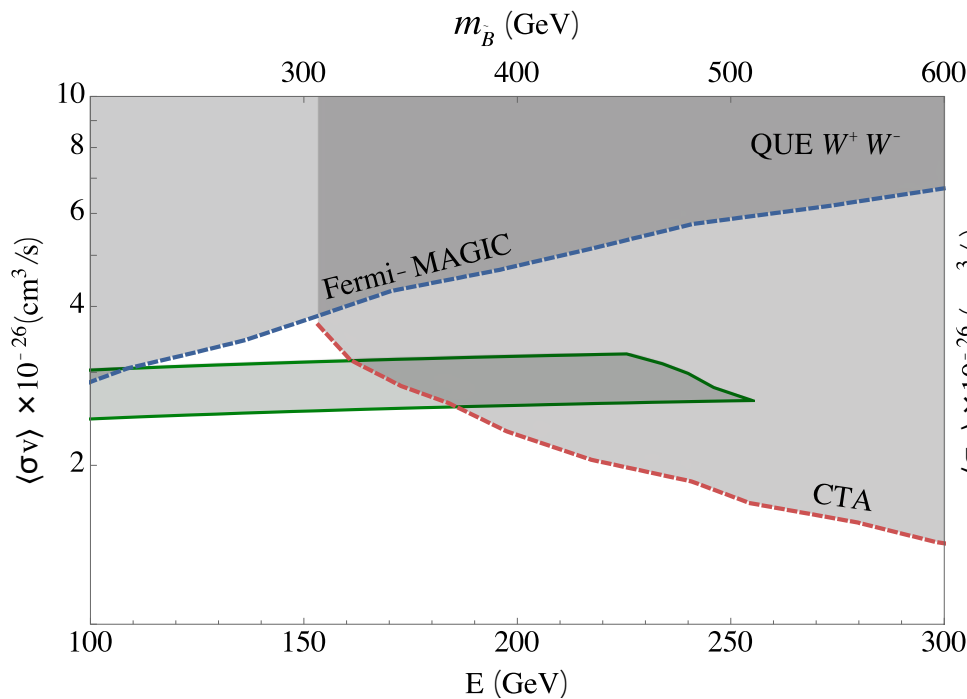
CTA prospect : 500hr of Milky Way

DM profile: Einasto

No syst. unc. (stat only)

WW (any mixing pattern)

$\tau\tau$ (only for τ -mixing cases)



- ✓ τ -mixing fully covered
- ✓ e/ μ -mixing with $m_{\tilde{B}} > 340-380$ GeV covered

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(with $m_{\tau_4} = 0.83m_{\tilde{B}}$)

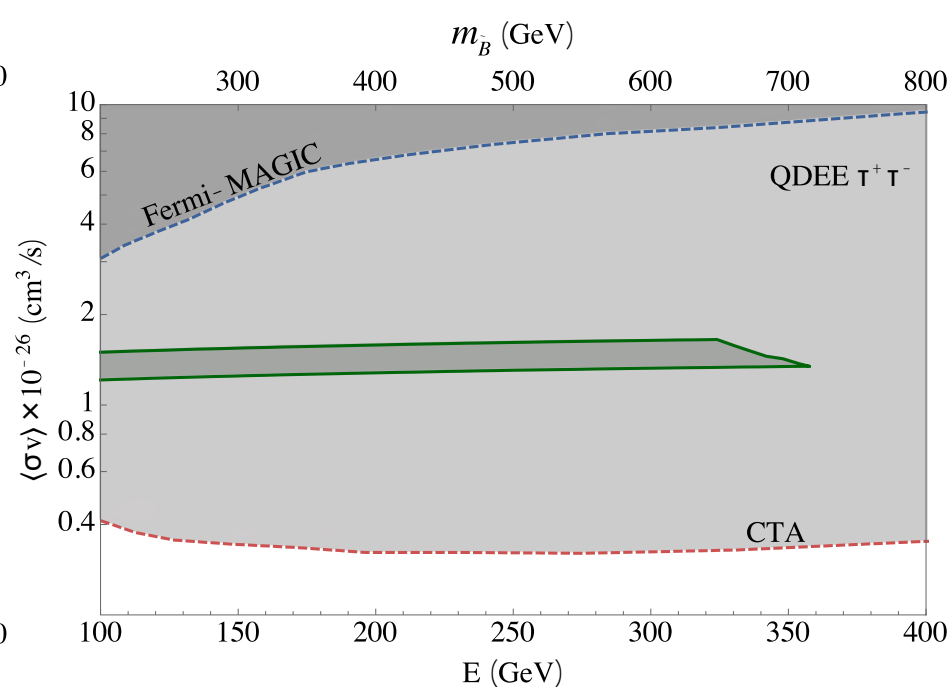
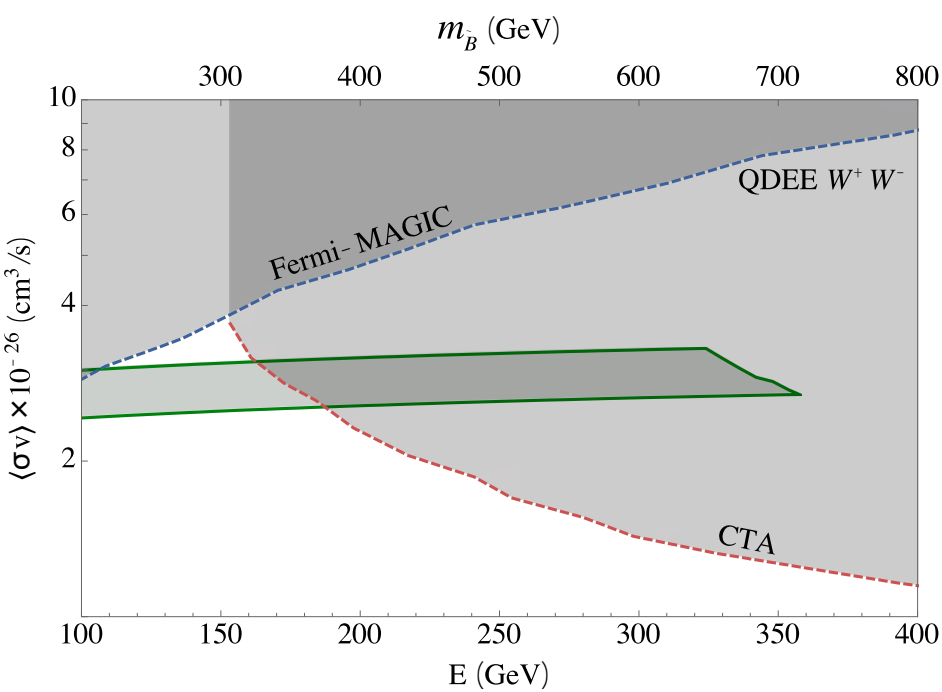
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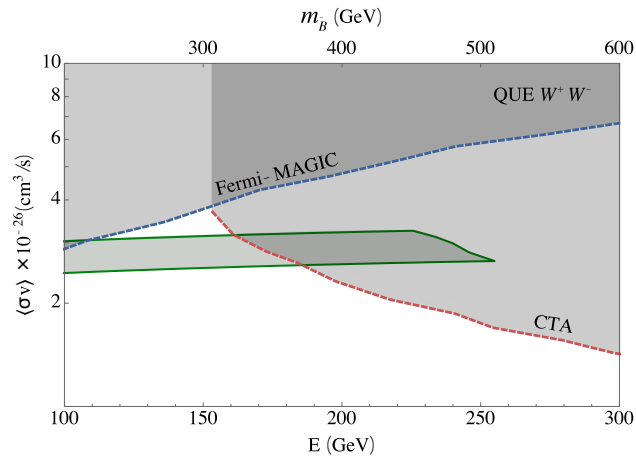
DM profile: Einasto

No syst. unc. (stat only)

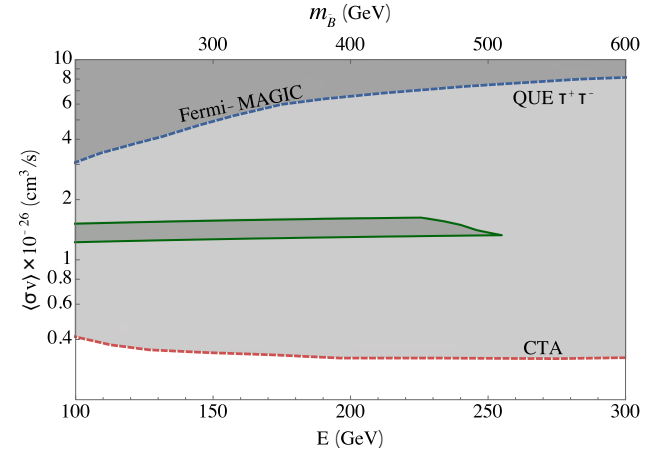
Summary

	e-mixing	μ -mixing	τ -mixing
CTA 500hr	covers $m_{\tilde{B}} > 340-380$ GeV		full coverage
HL-LHC			

e/ μ -mixing, QUE



τ / μ -mixing, QUE



Introduction: why overabundant?

Model: MSSM4G[📶] solves overabundance.

Analysis:

- cosmic rays (CTA, Fermi, MAGIC)
- colliders (LHC)
- direct detection (LUX)

Summary with discussion seeds

■ MSSM + $E\bar{E}$ → breaks coupling unification

■ QUE model : MSSM + $Q\bar{Q}U\bar{U}E\bar{E}$

⇒ SM + $\tilde{\chi}_1^0 (\approx \tilde{B})$, τ_4 ,
 $\underbrace{\tilde{\tau}_{4L}, \tilde{\tau}_{4R}}_{\text{assumed to be equal-mass}}$

■ QDEE model : MSSM + $Q\bar{Q}D\bar{D}E\bar{E}E\bar{E}$

⇒ SM + $\tilde{\chi}_1^0 (\approx \tilde{B})$, $\underbrace{\tau_4, \tau_5}_{\text{assumed to be equal-mass}}$,
 $\underbrace{\tilde{\tau}_{4L}, \tilde{\tau}_{4R}, \tilde{\tau}_{5L}, \tilde{\tau}_{5R}}_{\text{assumed to be equal-mass}}$

■ MSSM + $E\bar{E}$ → breaks coupling unification

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 τ_{4L}, τ_{4R}
 assumed to be equal-mass

extra lepton search (red line from τ_4)

slepton search (blue line from τ_{4L}, τ_{4R})

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⇒ SM + $\tilde{\chi}_1^0 (\approx \tilde{B}), \tau_4, \tau_5,$
 $\tau_{4L}, \tau_{4R}, \tau_{5L}, \tau_{5R}$
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extra lepton search (red line from τ_4, τ_5)

slepton search (blue line from $\tau_{4L}, \tau_{4R}, \tau_{5L}, \tau_{5R}$)

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⇒ SM + $\tilde{\chi}_1^0 (\approx \tilde{B})$, τ_4 ,

$\tilde{\tau}_{4L}, \tilde{\tau}_{4R}$

assumed to be equal-mass

slepton search

$\tilde{\tau}_4 \not\rightarrow \tau_4 + \tilde{B}$
 $\rightarrow (e, \mu, \tau) + \tilde{B}$
 $\equiv 2(4) \times \tilde{l}_R$

extra lepton search

$\tau_4 \rightarrow W\nu, Zl, hl$
 (as discussed before)
standard searches for vectorlike leptons (but 2x in QDEE)

+ $Q\bar{Q}D\bar{D}E\bar{E}E\bar{E}$

assumed to be equal-mass

τ_4, τ_5 ,

$\tilde{\tau}_{4L}, \tilde{\tau}_{4R}, \tilde{\tau}_{5L}, \tilde{\tau}_{5R}$

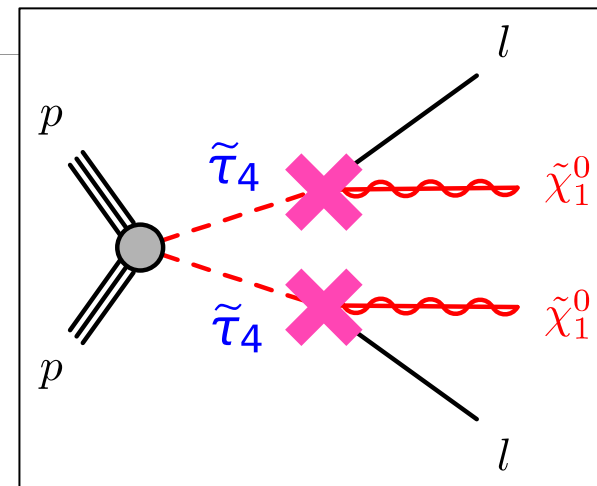
assumed to be equal-mass

Collider prospects for extra slepton searches

$$pp \rightarrow \tilde{\tau}_{4(5)} \tilde{\tau}_{4(5)}^* \equiv pp \rightarrow \tilde{l}_R \tilde{l}_R^*$$

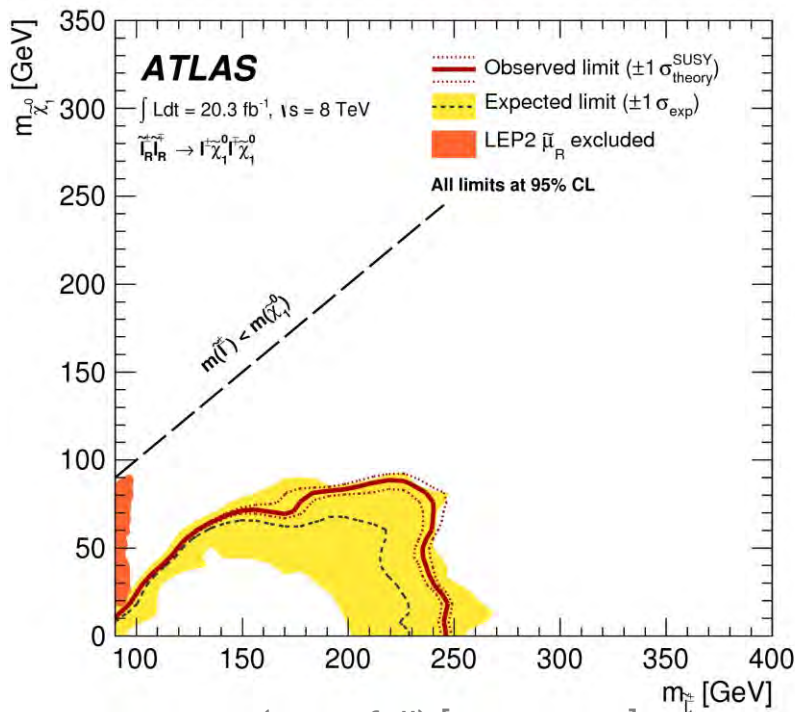
determined by mixing parameters

e/ μ -mixing \rightarrow slepton searches $\times 2$ (4)
($\tilde{e}_R, \tilde{\mu}_R$)

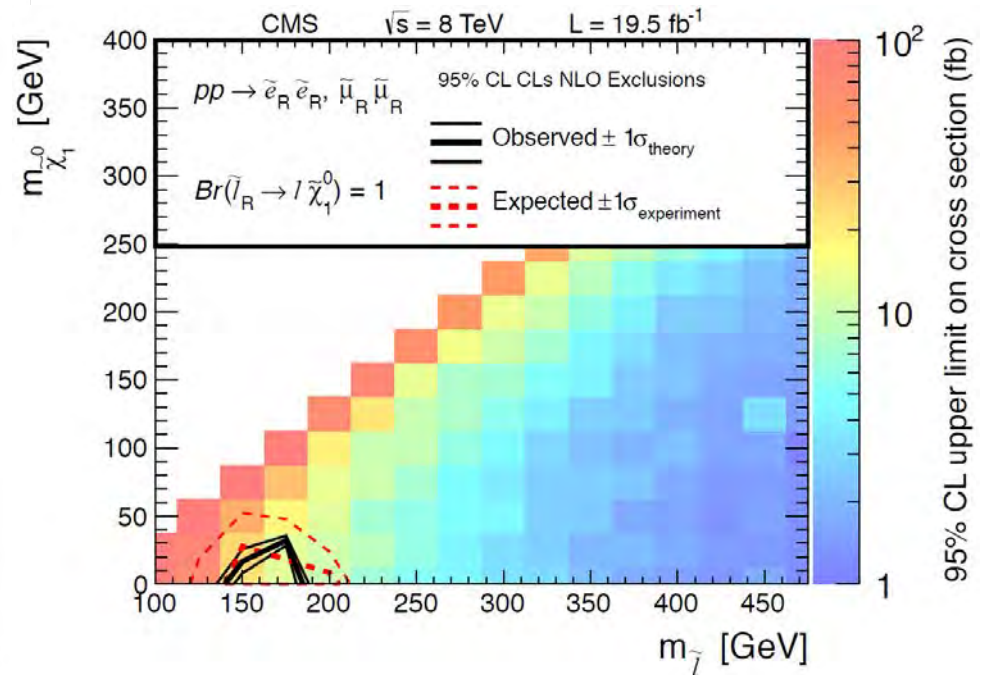


14 TeV prospects studied in [1408.2841](#) (Eckel, Ramsey-Musolf, Shepherd, Su)

\rightarrow re-interpreted



ATLAS (8TeV full) [[1403.5294](#)]



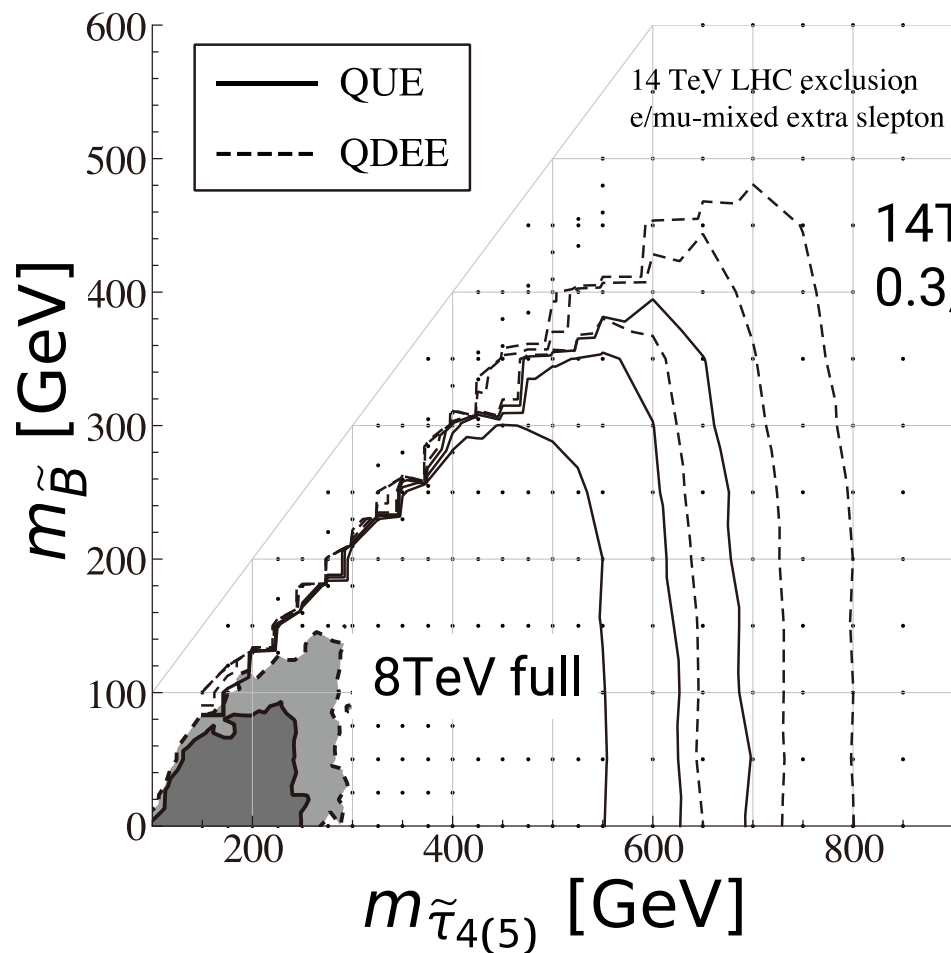
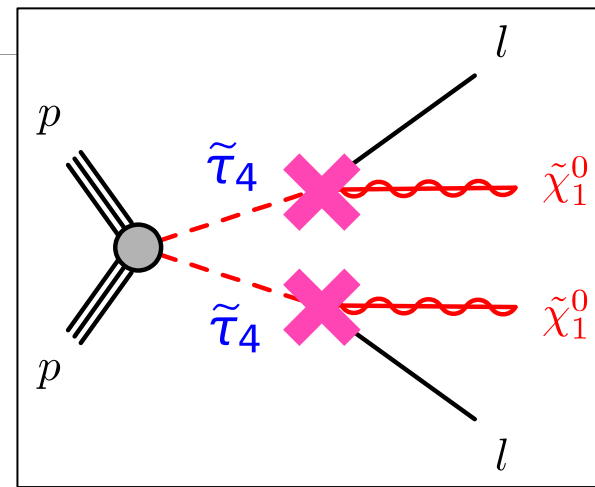
CMS (8TeV full) [[1405.7570](#)]

Collider prospects for extra slepton searches

$$pp \rightarrow \tilde{\tau}_{4(5)} \tilde{\tau}_{4(5)}^* \equiv pp \rightarrow \tilde{l}_R \tilde{l}_R^*$$

determined by mixing parameters

e/ μ -mixing \rightarrow slepton searches $\times 2$ (4)
 ($\tilde{e}_R, \tilde{\mu}_R$)



14TeV
 0.3, 1, 3/ab

- 2 lepton + MET + mT2 + jet-veto
- BKG taken from 1408.2841
 - MG5–Pythia–Delphes (also for signal)
 - rescaled by NLO K -factor
 - di-boson dominates
- Signal events at LO level
- Uncertainties = stat. + 5% syst.

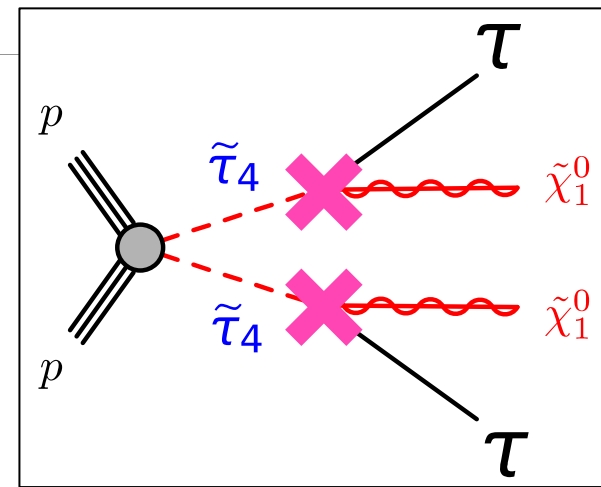
Collider prospects for extra slepton searches

$$pp \rightarrow \tilde{\tau}_{4,(5)} \tilde{\tau}_{4,(5)}^* \equiv pp \rightarrow \tilde{l}_R \tilde{l}_R^*$$

↑
determined by mixing parameters

τ -mixing \rightarrow stau searches $\times 2$ (4)

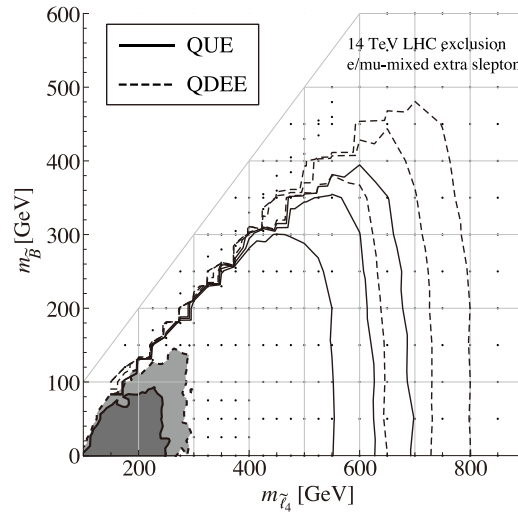
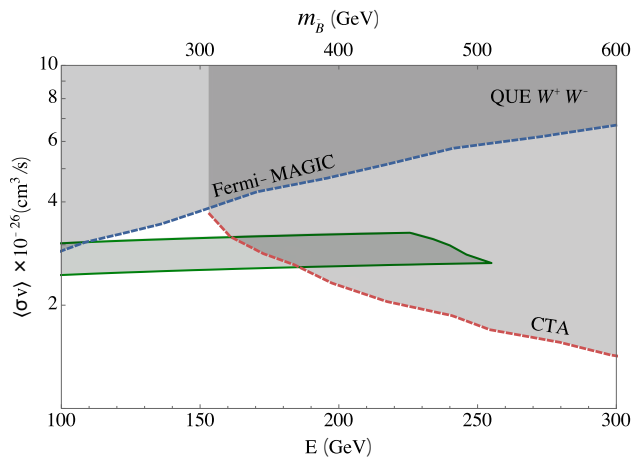
\rightarrow No constraint expected.



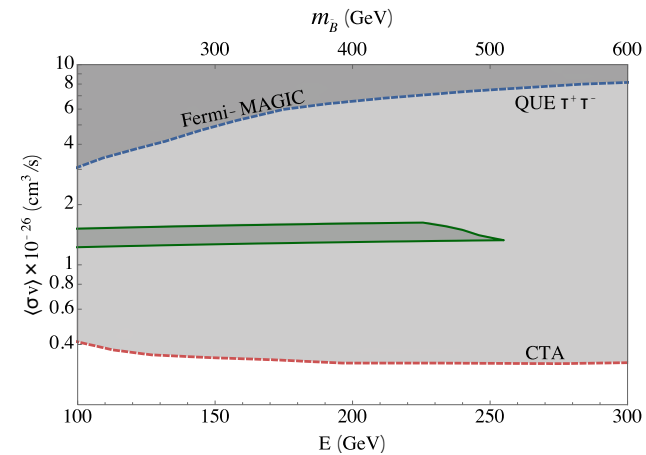
- LHC Run 1 provided no limit on MSSM stau mass.
- 14TeV, 3/ab LHC will not exclude MSSM4G parameter region.

	e-mixing	μ -mixing	τ -mixing
CTA 500hr	covers $m_{\tilde{B}} > 340-380$ GeV		full coverage
HL-LHC (slepton)	covers $m_{\tilde{B}} < 400$ (480) GeV (but not “degenerate” region)		—
HL-LHC (lepton)			

e/ μ -mixing



τ / μ -mixing, QUE



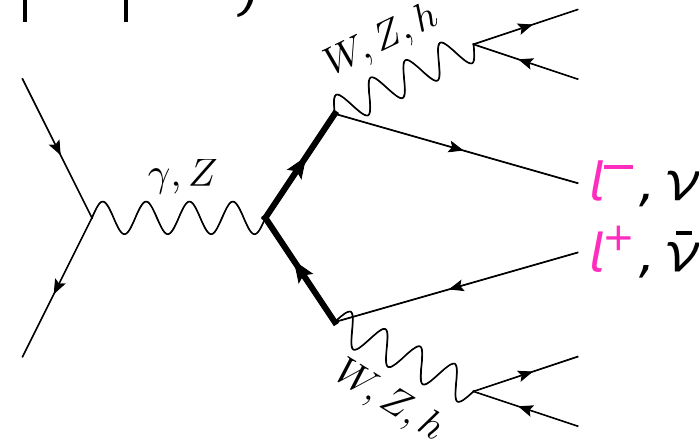
$$pp \rightarrow \tau_{4,(5)}^+ \tau_{4,(5)}^- \rightarrow (W\nu | hl | Zl)(W\nu | hl | hZ)$$

e/ μ -mixing case

“vectorlike lepton searches” by
multi- l^\pm signature ($3-5l^\pm$)

[Cf. ATLAS collaboration, [1506.01291](#)]

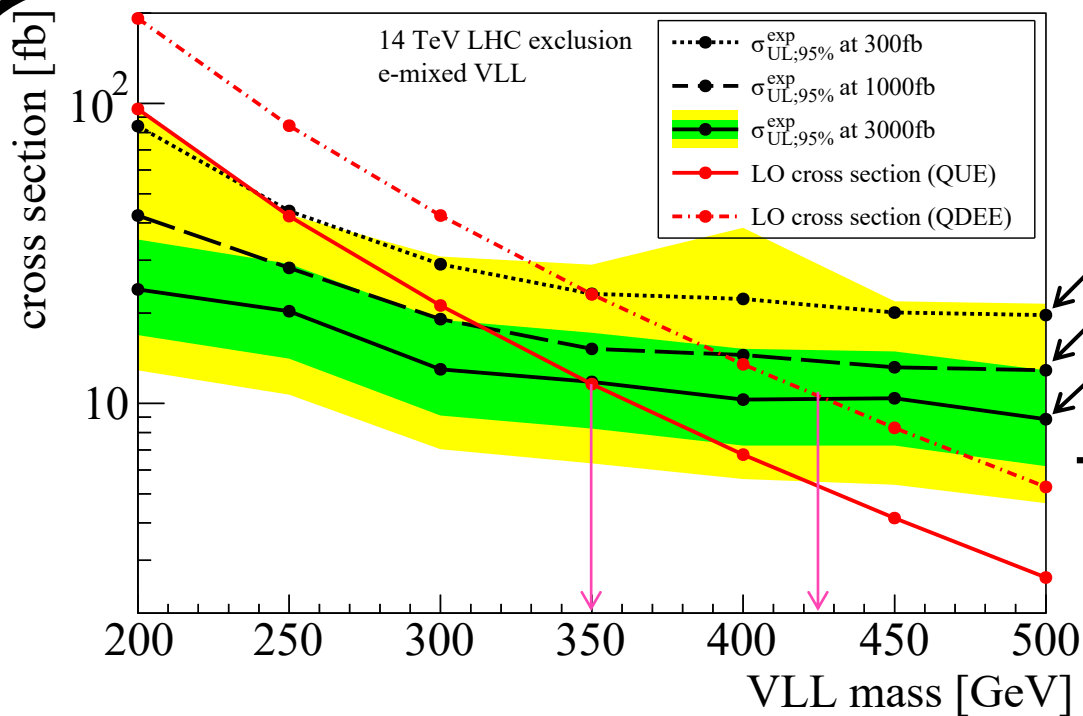
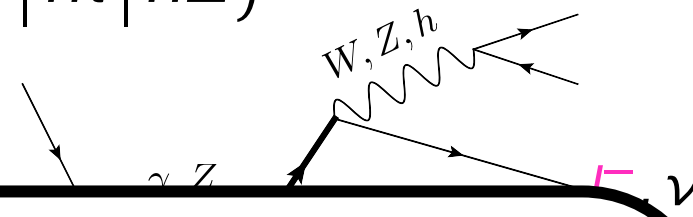
$$\left\{ \begin{array}{l} W\nu Zl \rightarrow 3l \text{ (1.3\%)} \\ W\nu hl \rightarrow 3l \text{ (0.6\%)} \\ hlZl \rightarrow 3l \text{ (0.8\%)} \\ hlhl \rightarrow 3l \text{ (0.8\%)} \end{array} \right. \quad \left\{ \begin{array}{l} W\nu Zl \rightarrow 4^+ l \text{ (0.4\%)} \\ hlZl \rightarrow 4^+ l \text{ (1.0\%)} \\ ZlZl \rightarrow 4^+ l \text{ (0.8\%)} \\ hlhl \rightarrow 4^+ l \text{ (0.2\%)} \end{array} \right.$$



→ Monte Carlo simulation

$$pp \rightarrow \tau_{4,(5)}^+ \tau_{4,(5)}^- \rightarrow (W\nu | hl | Zl)(W\nu | hl | hZ)$$

e/ μ -mixing case



- Snowmass BKG set is used.
 - MG5-Pythia-Delphes + NLO K -factor
 - di-boson + tt dominated
- SR dedicated for WZ / ZZ + leptons
 - 3L, 4L for WZ, and 4L, 5L for ZZ
 - tau-tag / b-tag not used (avoided)
- Signal by FR-MG5aMC-Pythia-Delphes (LO)
- Uncertainties = stat. + 20% syst.

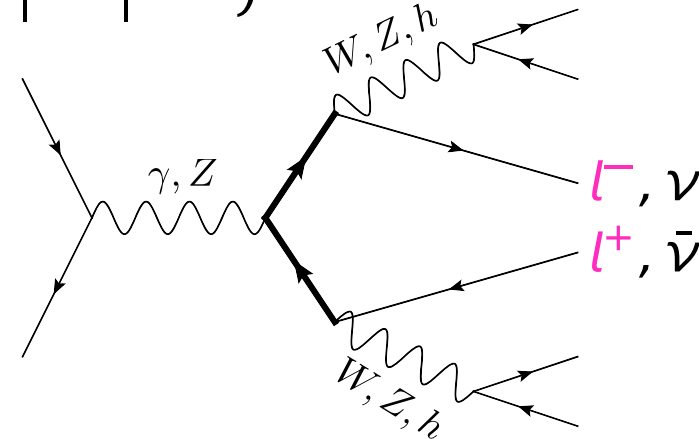
$$pp \rightarrow \tau_{4(5)}^+ \tau_{4(5)}^- \rightarrow (W\nu | hl | Zl)(W\nu | hl | hZ)$$

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→ 14TeV, 3/ab covers
 $m_{\tau_4} < 350 \text{ (425) GeV}$
QUE QDEE

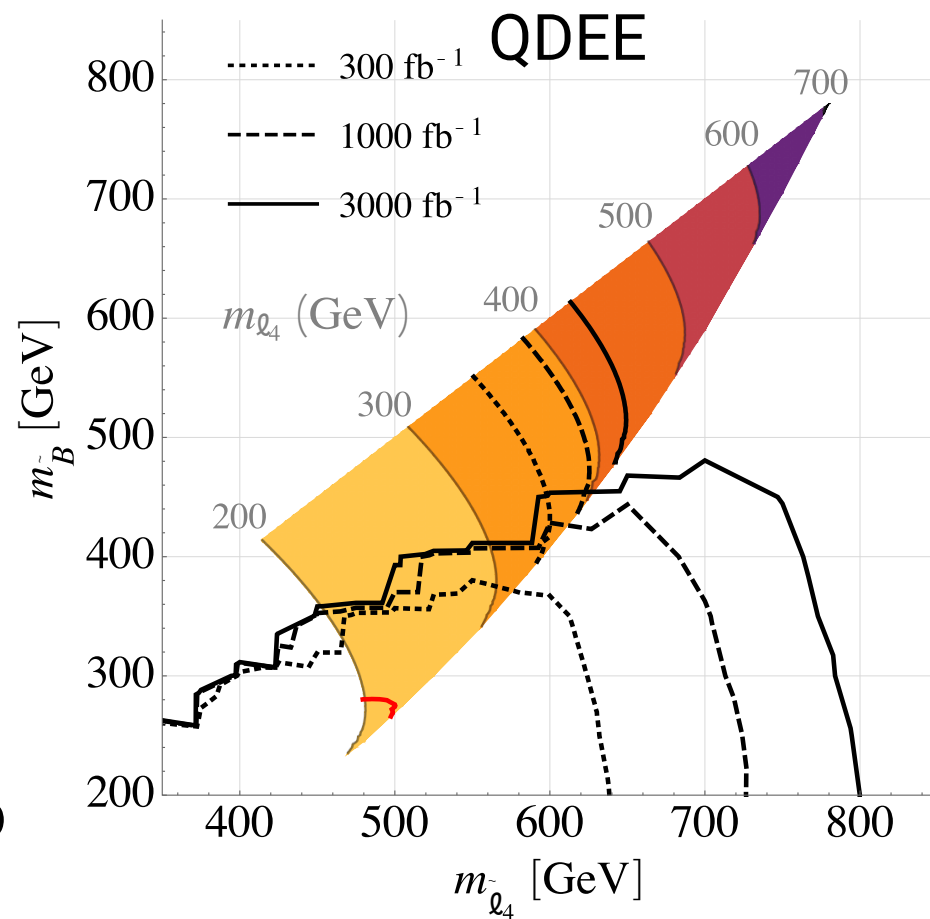
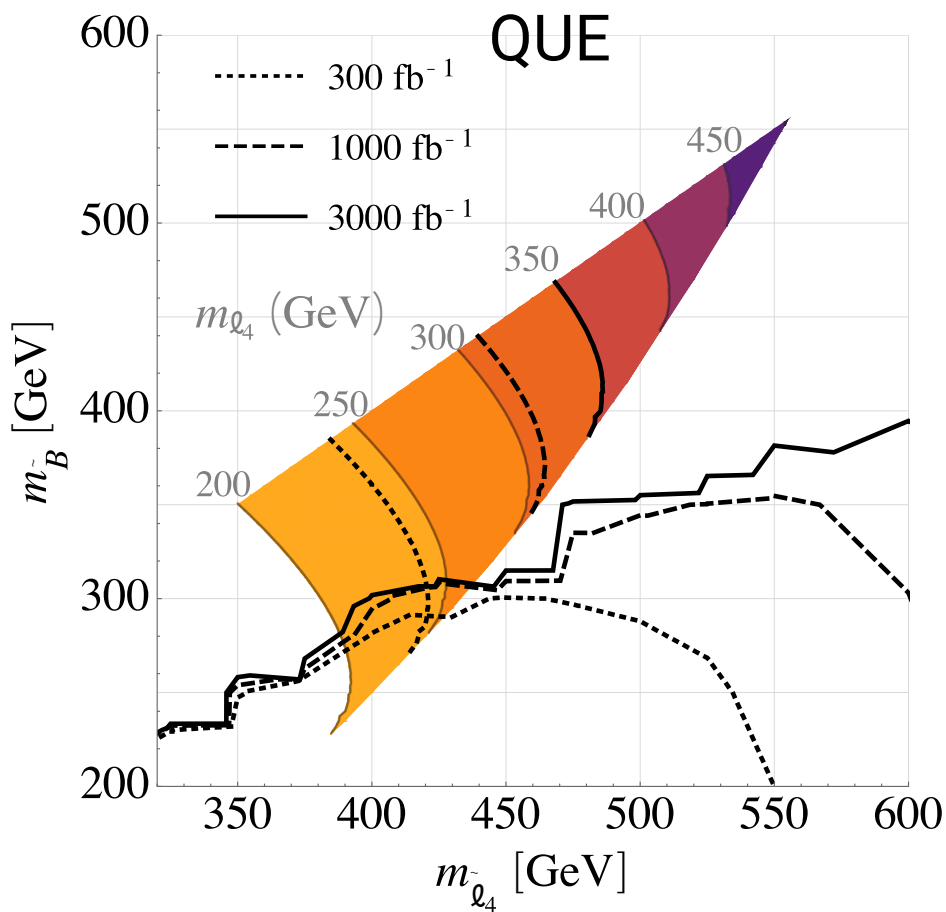
τ -mixing case

✓ [1510.03456](#) (Kumar and Matrin)

- SRs: 4(e, mu, had-tau)
- Signal and BKG by their MC (FR-MG5-Pythia-Delphes)
- no prospects for exclusion if BKG syst. unc. > 10%

→ 13 TeV, 3/ab covers
 $m_{\tau_4} < 234 \text{ (264) GeV}$
with “a very optimistic BKG estimation”

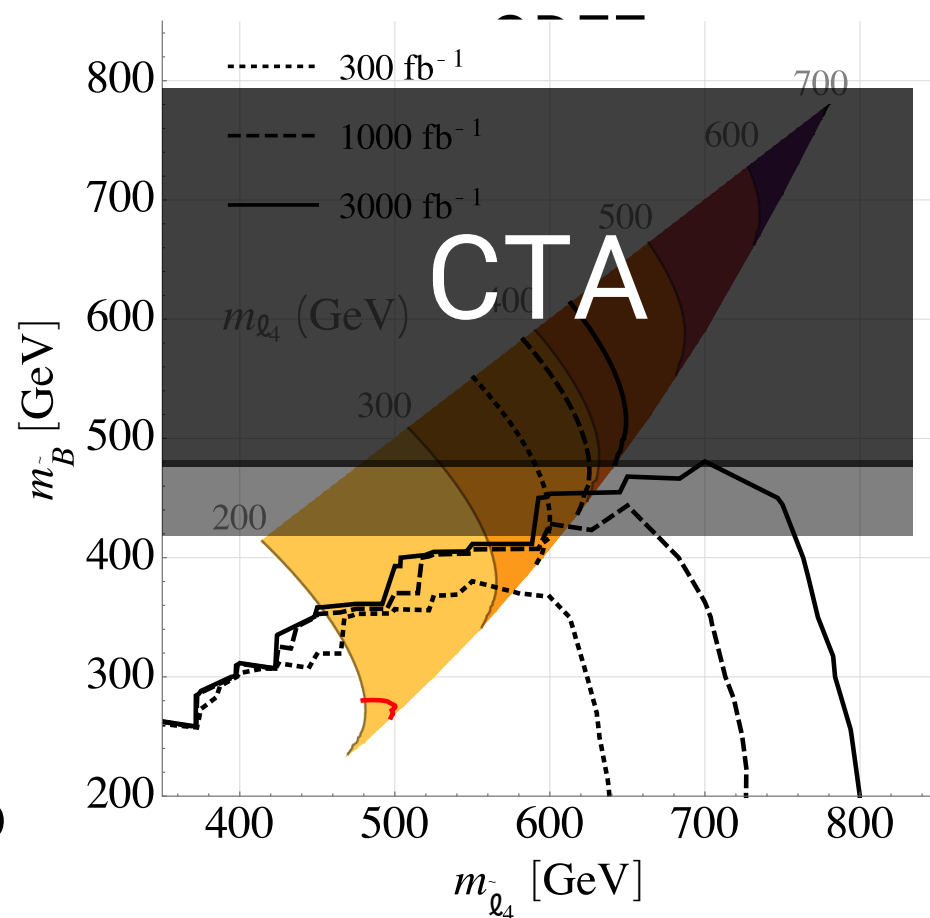
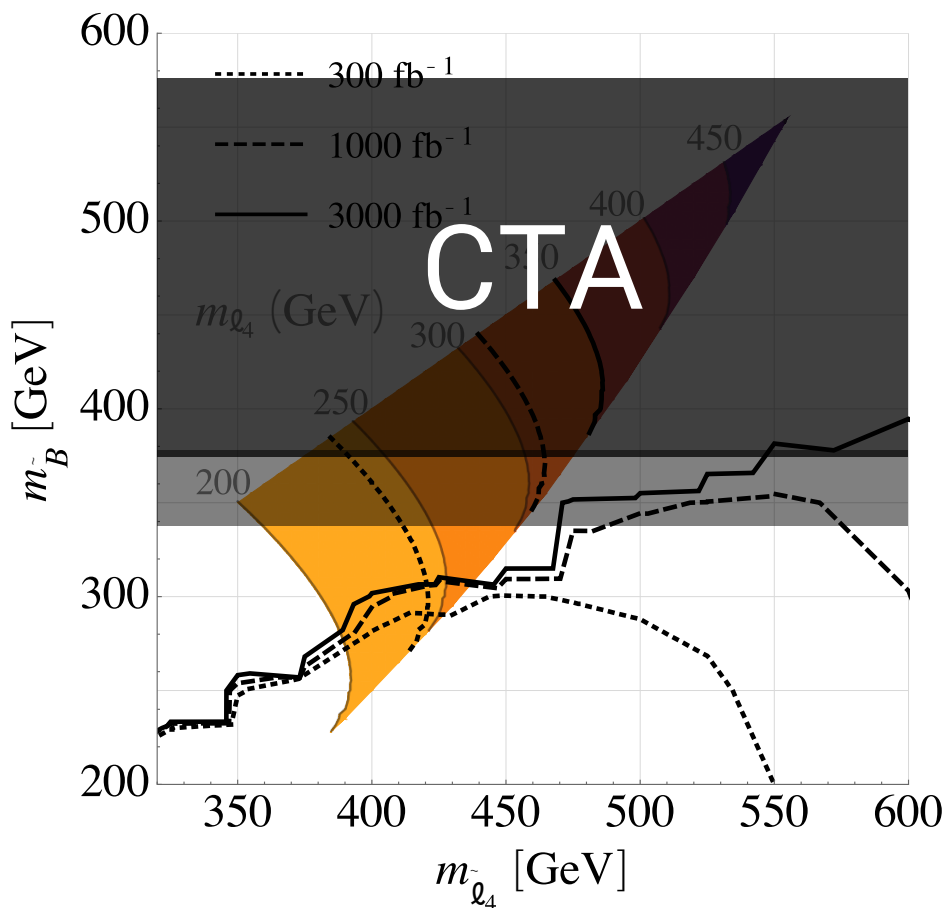
■ e/ μ -mixing cases



■ τ -mixing case

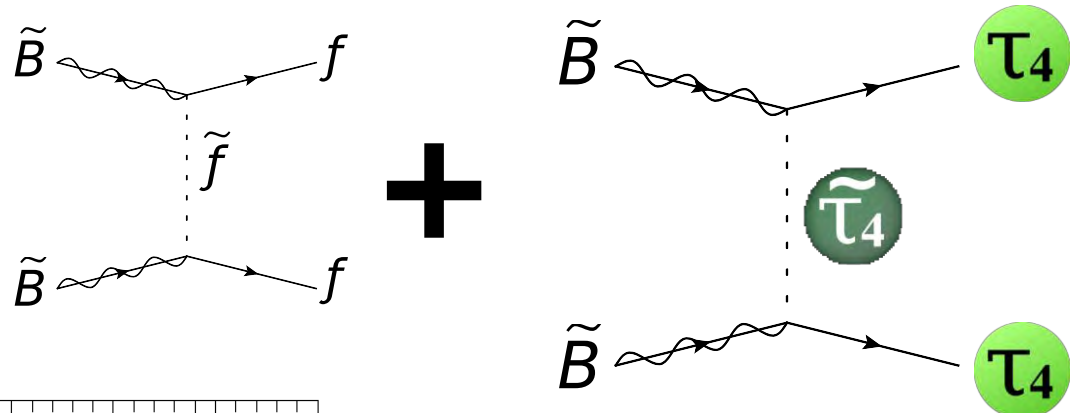
➤ LHC insensitive ... ($\tau \cdot \omega \cdot \tau$)

■ e/ μ -mixing cases



■ τ -mixing case

- LHC insensitive, but CTA covers full region



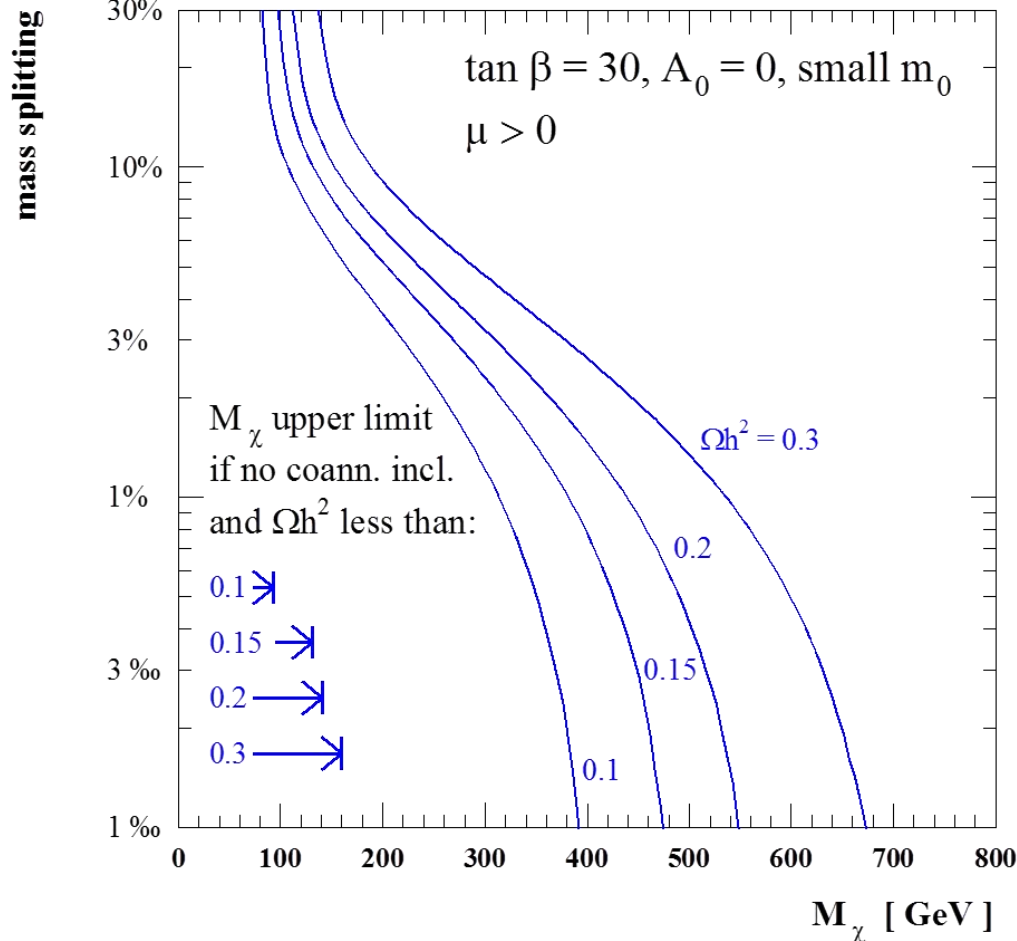
extra annihilation channel

→ larger Ωh^2
 → “proper” $\langle \sigma v \rangle$

if $\tau_4 \gtrsim \tilde{B} > \tau_4$

$\langle \sigma v \rangle \propto Y^4 \implies \text{MSSM} + E\bar{E}$

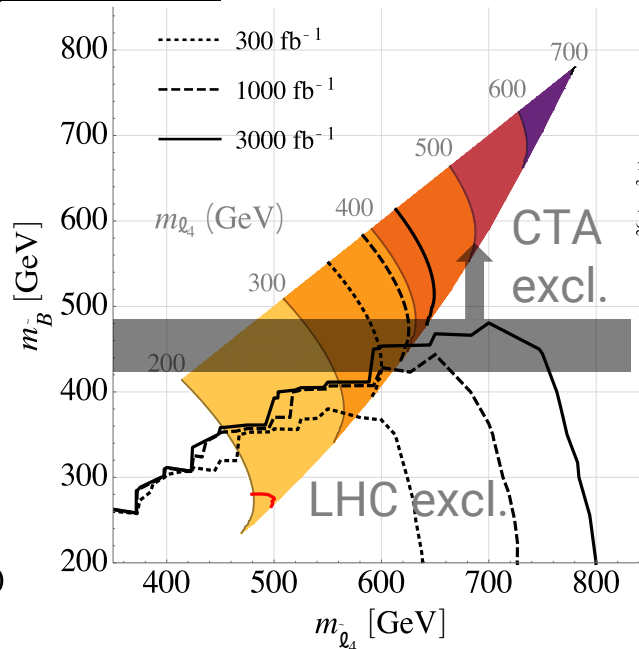
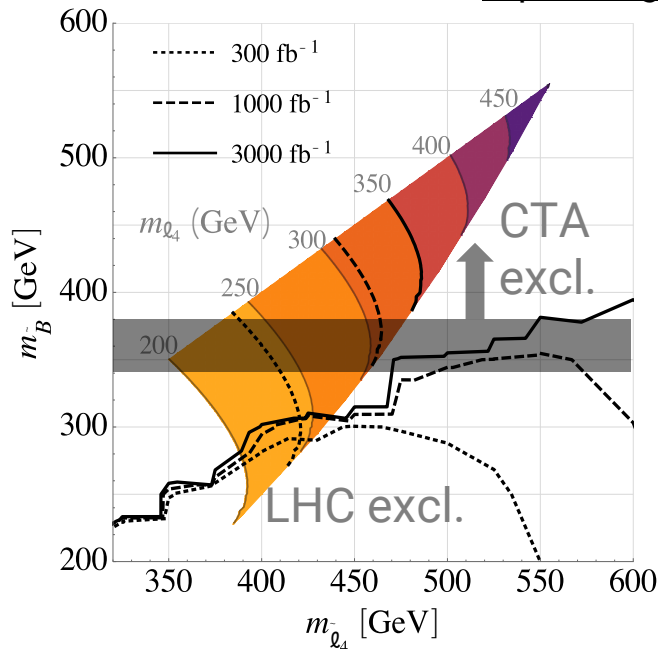
$$Y_u H_u Q \bar{U} + Y_d H_d Q \bar{D} + Y_e H_d L \bar{E} + M_{E_4} E_4 \bar{E}_4 + \epsilon_i H_d L_i \bar{E}_4$$



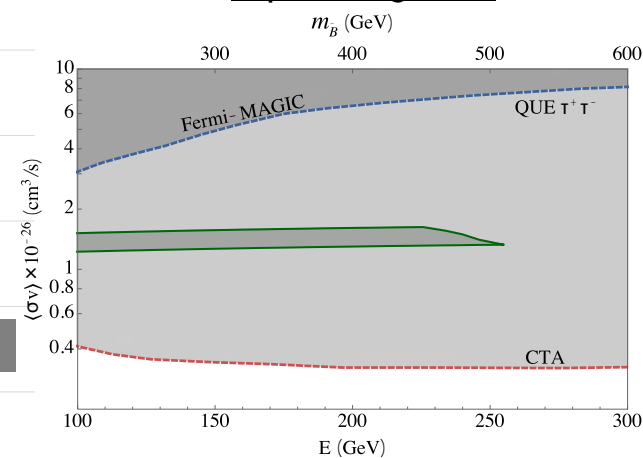
Summary : Future prospects

	e-mixing	μ -mixing	τ -mixing
CTA 500hr	covers $m_{\tilde{B}} > 340\text{--}380$ GeV		full coverage
HL-LHC (slepton)	covers $m_{\tilde{B}} < 400$ (480) GeV (but not “degenerate” region)		—
HL-LHC (lepton)	covers $m_{\tau_4} < 350$ (430) GeV equivalent to $m_{\tilde{B}} < 380$ (480) GeV		—

e/ μ -mixing, QUE / QDEE



τ / μ -mixing, QUE



Introduction: why overabundant?

Model: **MSSM4G**  solves overabundance.

Analysis:

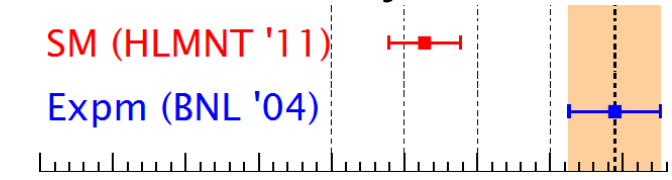
- cosmic rays (CTA, Fermi, MAGIC)
- colliders (LHC)
- direct detection (LUX)

Summary with discussion seeds

: “muon $g-2$ problem”

$$\left(a_\mu := \frac{g_\mu - 2}{2} \right)$$

■ $(g - 2)_\mu$ anomaly



SM (HLMNT '11)

Expm (BNL '04)

$$a_\mu^{\text{SM}} = (116\,591\,828 \pm 49) \times 10^{-11}$$

$$a_\mu^{\text{exp}} = (116\,592\,089 \pm 63) \times 10^{-11}$$

Hagiwara, Liao, Martin, Nomura, Teubner [1105.3149]

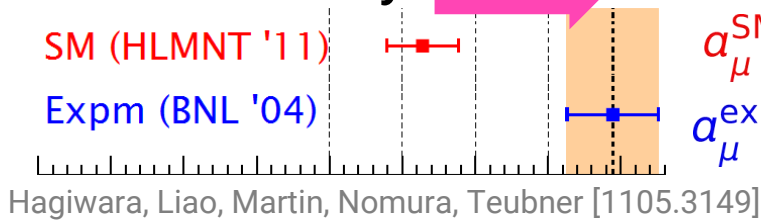
3.3 σ discrepancy

MSSM: extra contribution \rightarrow MSSM **may** explain this anomaly.

$$\left(a_\mu := \frac{g_\mu - 2}{2} \right)$$

■ $(g - 2)_\mu$ anomaly

PUSH UP



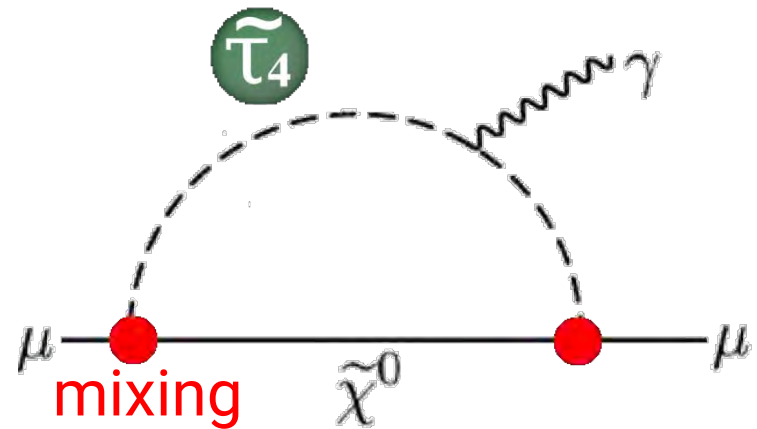
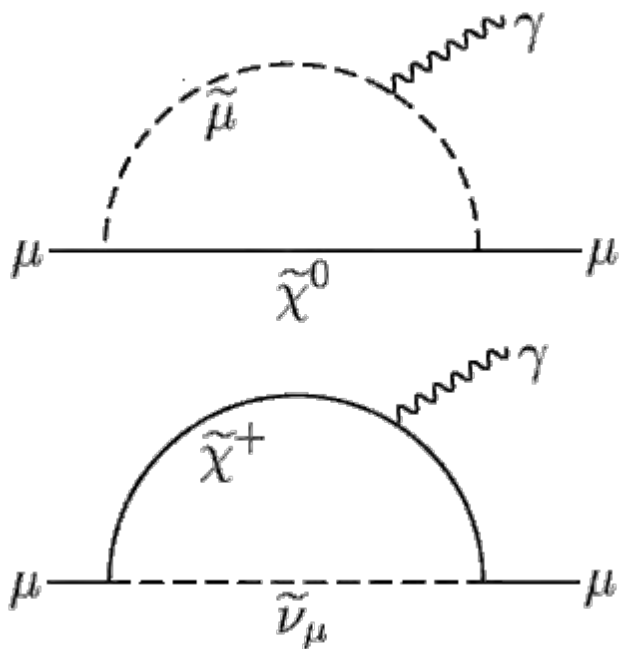
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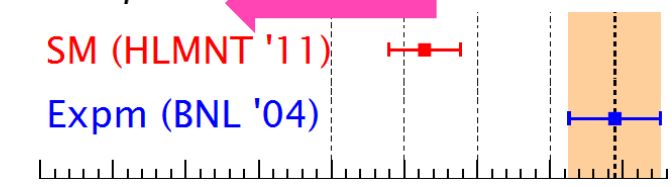
4G extra contribution?



$$\left(a_\mu := \frac{g_\mu - 2}{2} \right)$$

■ $(g - 2)_\mu$ anomaly

PUSH DOWN



$$a_\mu^{\text{SM}} = (116\,591\,828 \pm 49) \times 10^{-11}$$

$$a_\mu^{\text{exp}} = (116\,592\,089 \pm 63) \times 10^{-11}$$

Hagiwara, Liao, Martin, Nomura, Teubner [1105.3149]

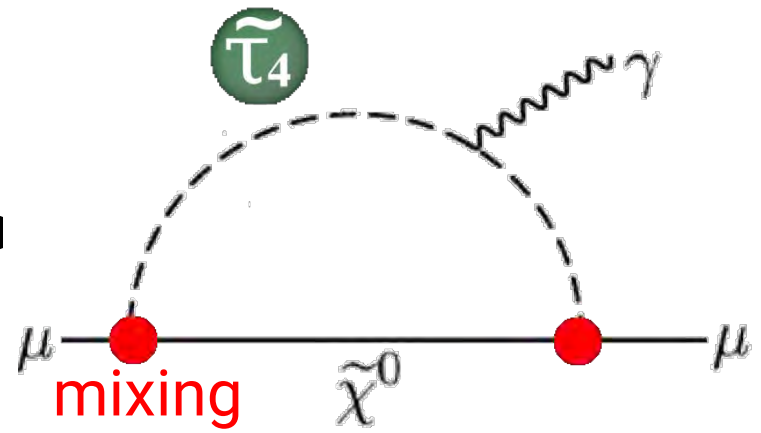
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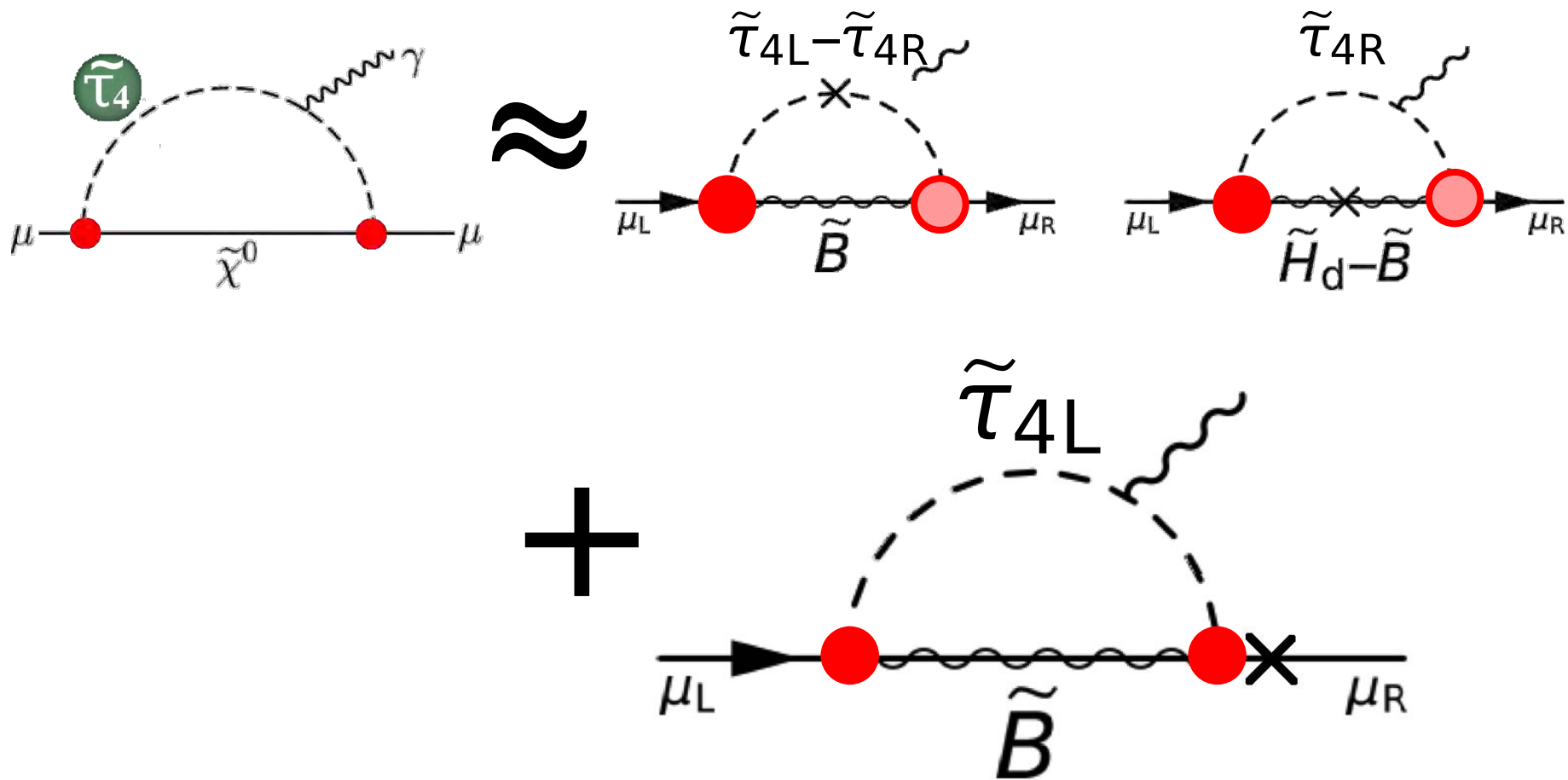
4G extra contribution?

0

\geq



■ Why always negative?

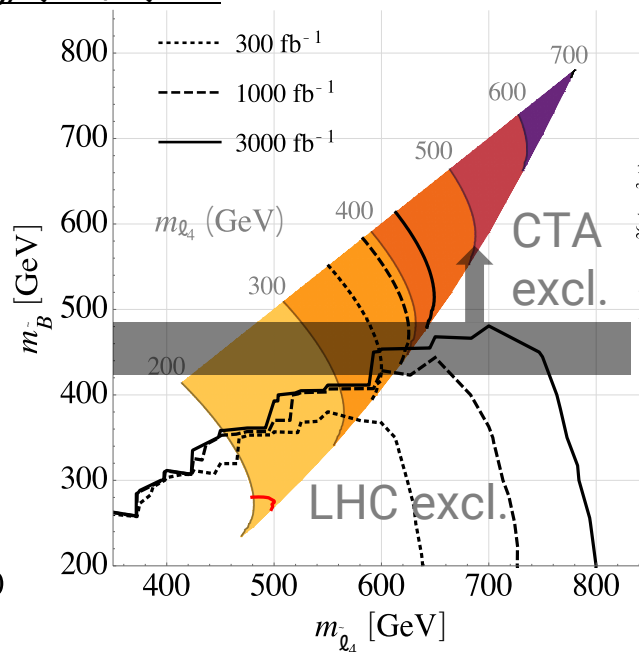
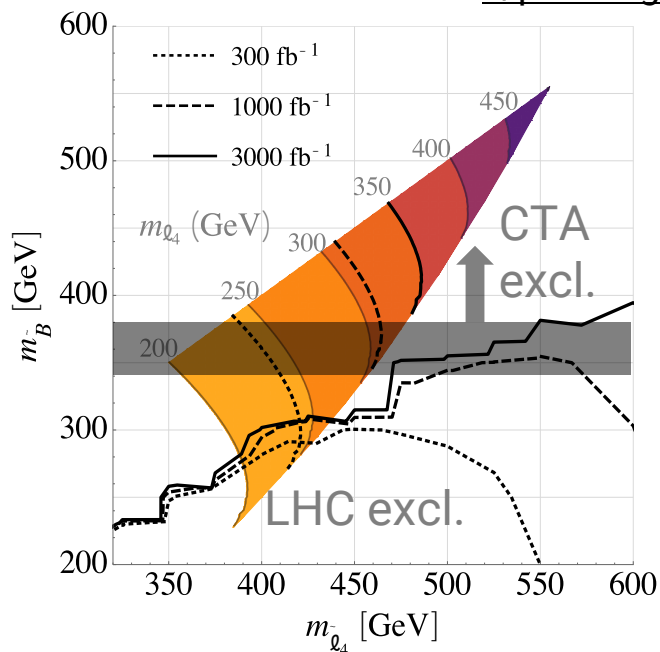


$$= -\frac{|\epsilon|^2}{16\pi^2} \frac{m_\mu^2}{6(|M_E|^2 + m_{\tilde{E}_c}^2)} N_1 \left(\frac{\mu^2}{|M_E|^2 + m_{\tilde{E}_c}^2} \right)$$

Summary : Future prospects

	e-mixing	μ -mixing	τ -mixing
CTA 500hr	covers $m_{\tilde{B}} > 340-380$ GeV		full coverage
HL-LHC (slepton)	covers $m_{\tilde{B}} < 400$ (480) GeV (but not “degenerate” region)		—
HL-LHC (lepton)	covers $m_{\tau_4} < 350$ (430) GeV equivalent to $m_{\tilde{B}} < 380$ (480) GeV		—

e/ μ -mixing, QUE / QDEE



τ / μ -mixing, QUE

