



# Long-lived sleptons at a 100 TeV pp collider

(and at the 14 TeV LHC)

Sho IWAMOTO (岩本 祥)

13 Dec. 2015

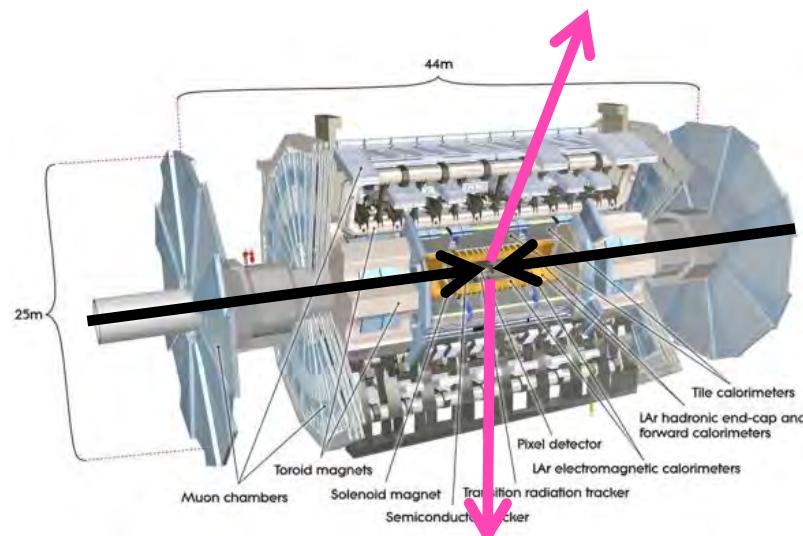
IPS 61st annual meeting @ Bar Ilan University

Based on

J. L. Feng (UC Irvine), SI, Y. Shadmi, S. Tarem (Technion) [[1505.02996](#)]

Sleptons  $\tilde{l}$  : a particle predicted in SUSY  
[SUSY-partner of leptons]

- Mass  $\gtrsim 100 \text{ GeV}$  (LEP)
- Charge: EM-charged
- Lifetime: ?????
  - If long-lived (“stable”)  $\longrightarrow$  charged track



- Expected reach “ $m_{\tilde{l}}$ ”  
at 100 TeV pp collider
  - New phenomenon  
at 100 TeV pp collider
- “Muon radiative energy loss”**

# 1. Motivation for long-lived $\tilde{l}$

## 2. searches at the LHC

## 3. at 100 TeV collider?

- Muon radiative energy loss for BKG reduction

## 4. Results

- Expected reach:  $m_{\tilde{l}}$

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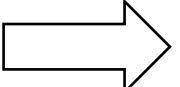
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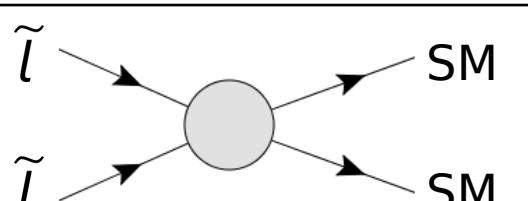
$$\Omega_{\text{DM}} h^2 = 0.12 \quad \dots \text{how to realize?}$$

- A hypothesis: “superWIMP scenario”

$$\text{LSP} = \tilde{G}, \text{ NLSP} = \tilde{l} \quad \dots \text{long-lived } \tilde{l}$$

$$\tau(\tilde{l} \rightarrow l\tilde{G}) = \frac{5.7 \times 10^{-7} \text{ sec}}{\equiv 170 \text{ m}} \cdot \left( \frac{m_{\tilde{l}}}{1 \text{ TeV}} \right)^{-5} \left( \frac{m_{\tilde{G}}}{1 \text{ MeV}} \right)^2$$

  $\tilde{l}$  : freeze-out with  $\Omega_{\text{slepton}} h^2 \gg 0.12$ ,  
and then decay.

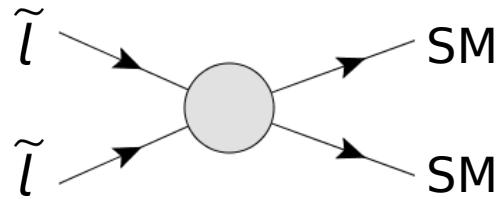
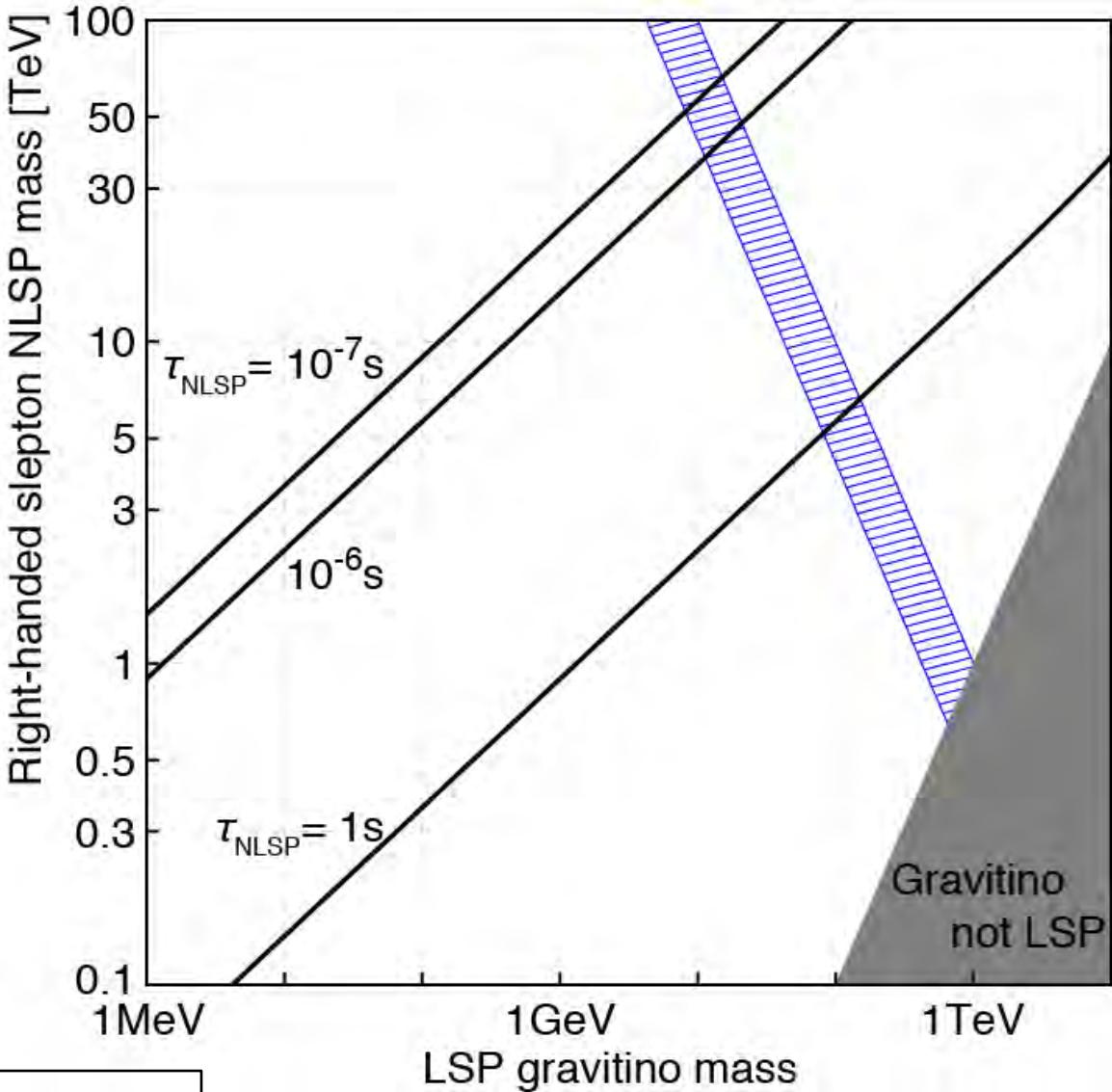


$$\langle \sigma v \rangle \approx \frac{4\pi\alpha^2}{m_{l_R}^2} + \frac{16\pi\alpha^2 m_{\tilde{B}}^2}{\cos^4 \theta_W (m_{l_R}^2 + m_{\tilde{B}}^2)^2}$$

$$\Omega_{\tilde{G}} h^2 = \frac{m_{\tilde{G}}}{m_{\tilde{l}}} \Omega_{\text{slepton}} h^2$$



## SuperWIMP scenario



$$\langle \sigma v \rangle \approx \frac{4\pi\alpha^2}{m_{\tilde{l}_R}^2} + \frac{16\pi\alpha^2 m_{\tilde{B}}^2}{\cos^4 \theta_W (m_{\tilde{l}_R}^2 + m_{\tilde{B}}^2)^2}$$

# 1. Motivation for long-lived $\tilde{l} = \Omega_{\text{DM}} h^2$

2. searches at the LHC

- superWIMP
- $\tilde{B}-\tilde{l}$  co-annihilation

3. at 100 TeV collider?

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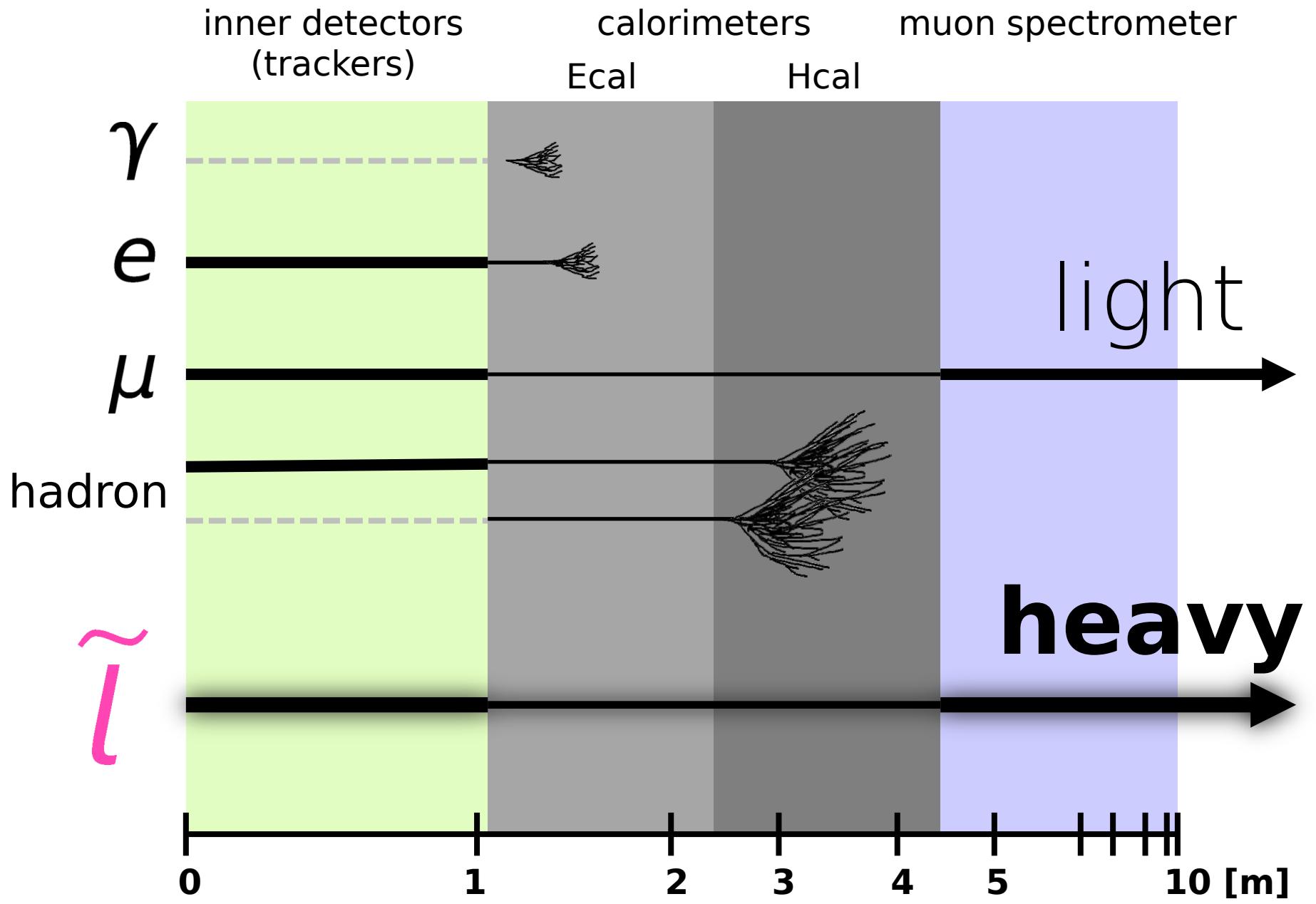
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## **“Mass measurement” to distinguish long-lived sleptons**

$$m = \frac{p}{\beta\gamma} = \frac{p}{\beta/\sqrt{1 - \beta^2}}$$

momentum & velocity

■ **mass** measurement =  $\pmb{p}$  &  $\pmb{\beta}$  measurements  
-----  
 $(\beta = v/c)$



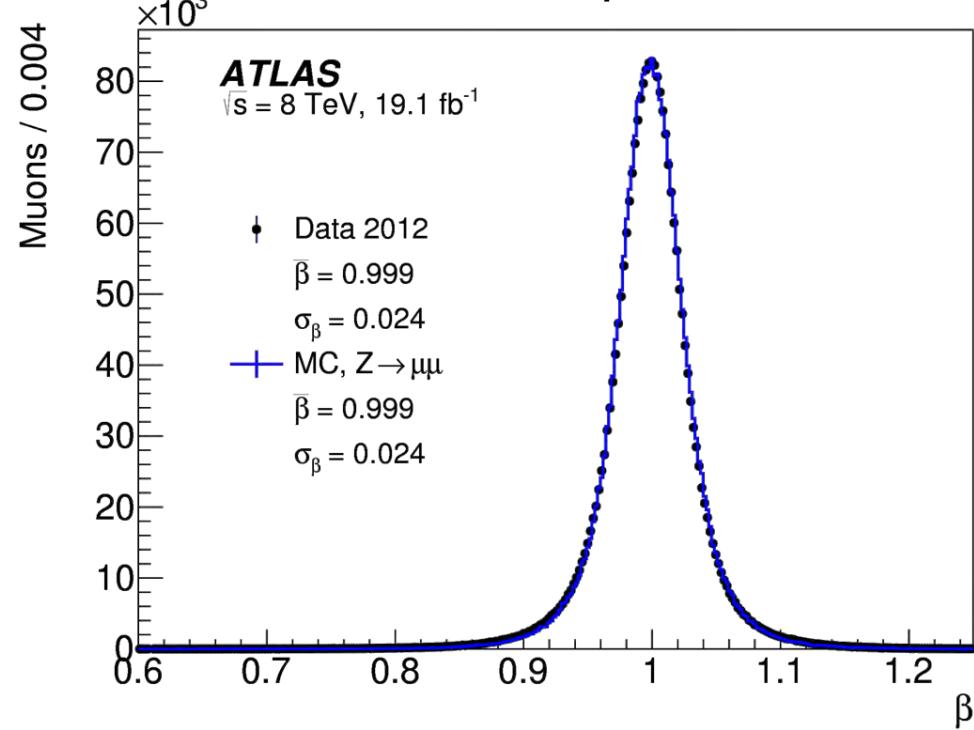
- TOF [time-of-flight]  
$$\beta = \Delta L / \Delta t$$
- $dE/dx$  [ionization energy loss]

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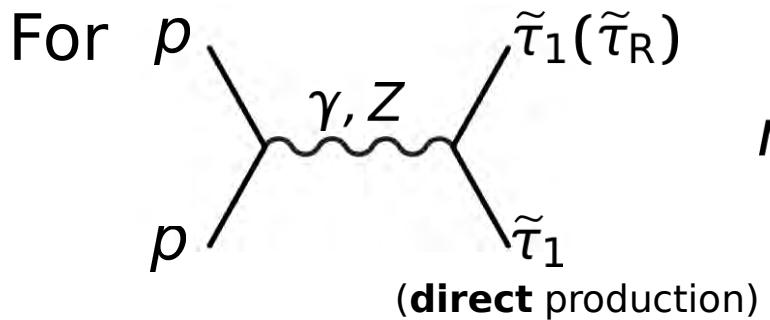
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■ **mass** measurement =  $\pmb{p}$  &  $\pmb{\beta}$  measurements  
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ATLAS: **muon**  $\beta$  resolution

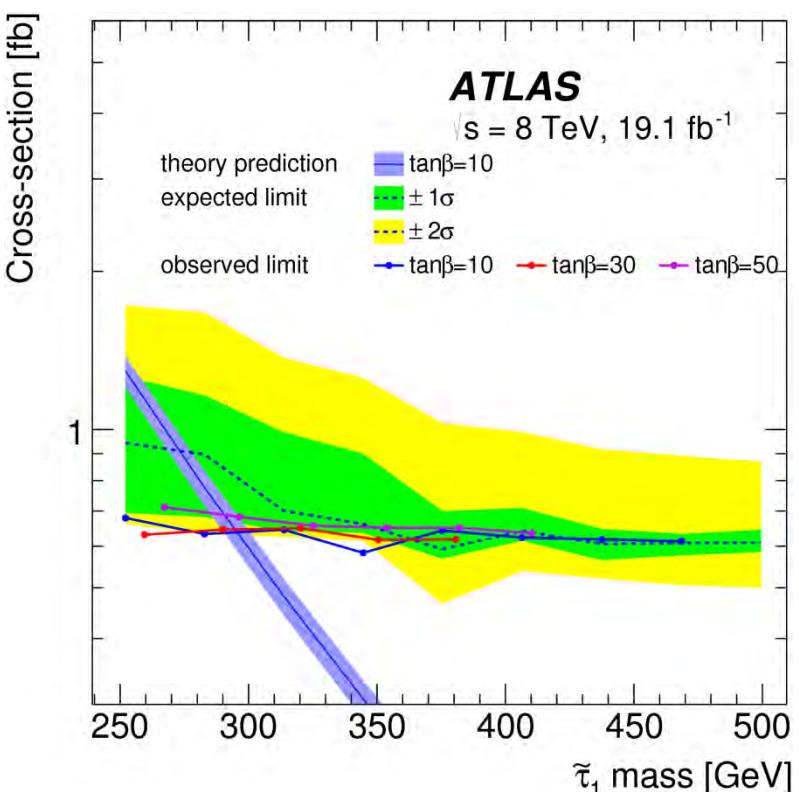
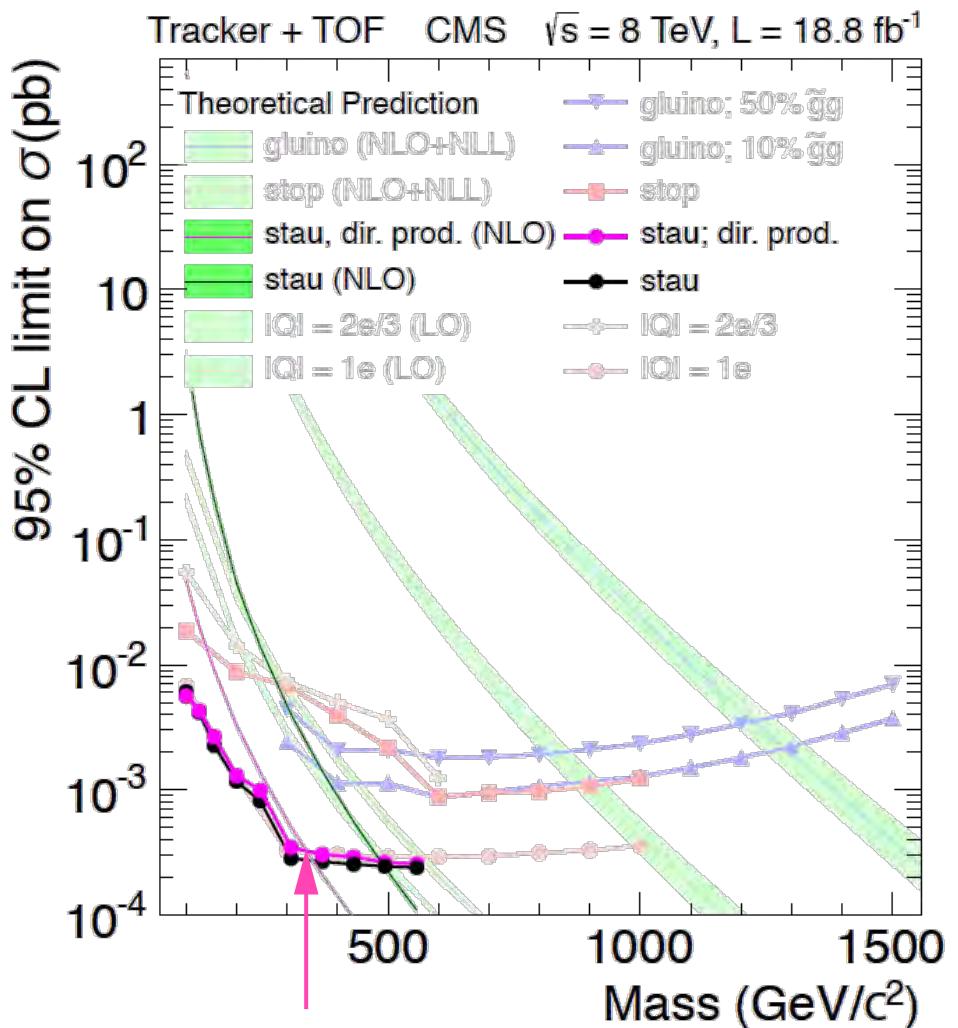


- TOF [time-of-flight]  
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$$m(\tilde{\tau}_1) > \begin{cases} 339 \text{ GeV [CMS]} \\ 286 \text{ GeV [ATLAS]} \end{cases}$$

[1305.0491] [1411.6795]



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3. at **100 TeV collider?**

➤ Muon radiative energy loss for BKG reduction

4. Results

➤ Expected reach:  $m_{\tilde{t}}$

ATLAS @8TeV [1411.6795]

$\tilde{t}$  selection flow:

- observed as a muon
- $p_T > 70 \text{ GeV}$
- $|\eta| < 2.4$
- $0.2 < \hat{\beta} < 0.95$

Our 100TeV simulation

$\tilde{t}$  selection flow:

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# Muon energy loss in matter

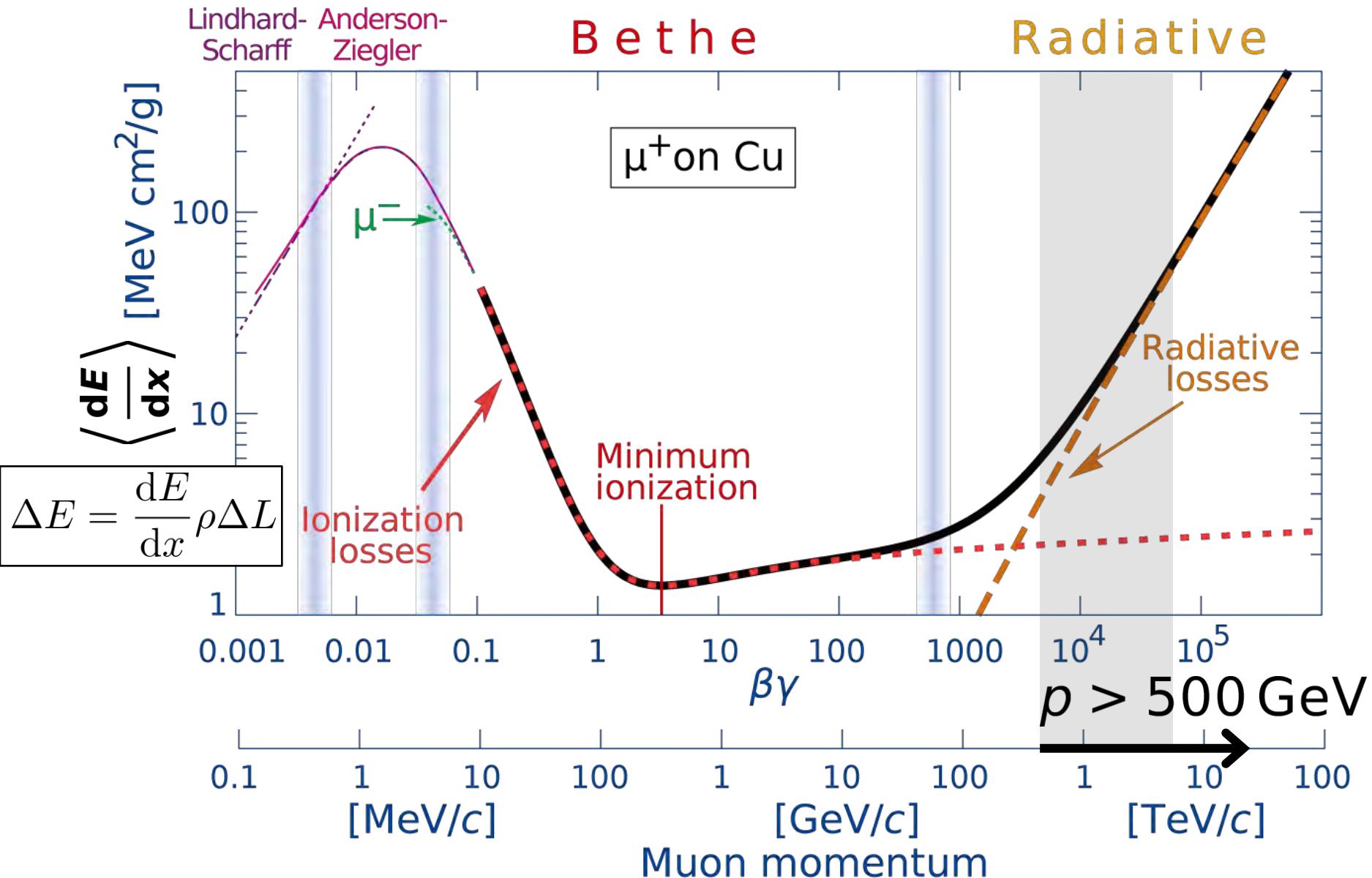


Figure from Groom, Mokhov, Striganov, [Atom. Nucl. Data Tab. 78](#) (2001) 183-356  
 [also in PDG Review "Passage of particles through matter"]

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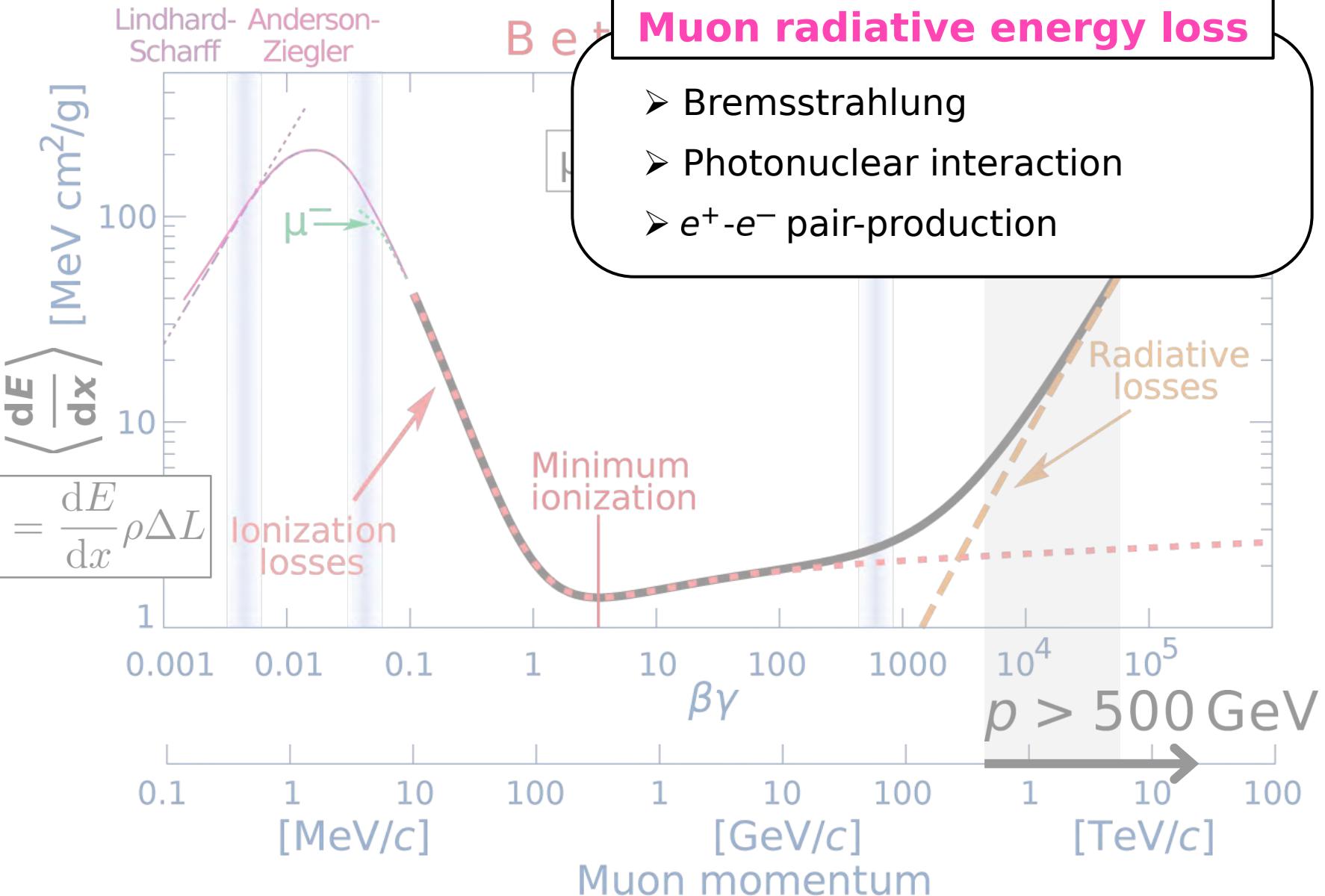
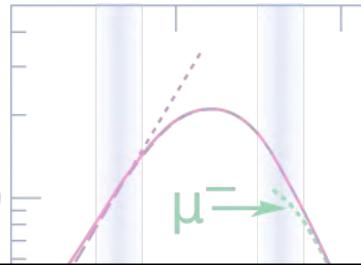


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## Muon energy loss in matter

Lindhard-  
Scharff  
Anderson-  
Ziegler

eV cm<sup>2</sup>/g]



B e +

### Muon radiative energy loss

- Bremsstrahlung
- Photonuclear interaction
- $e^+ - e^-$  pair-production

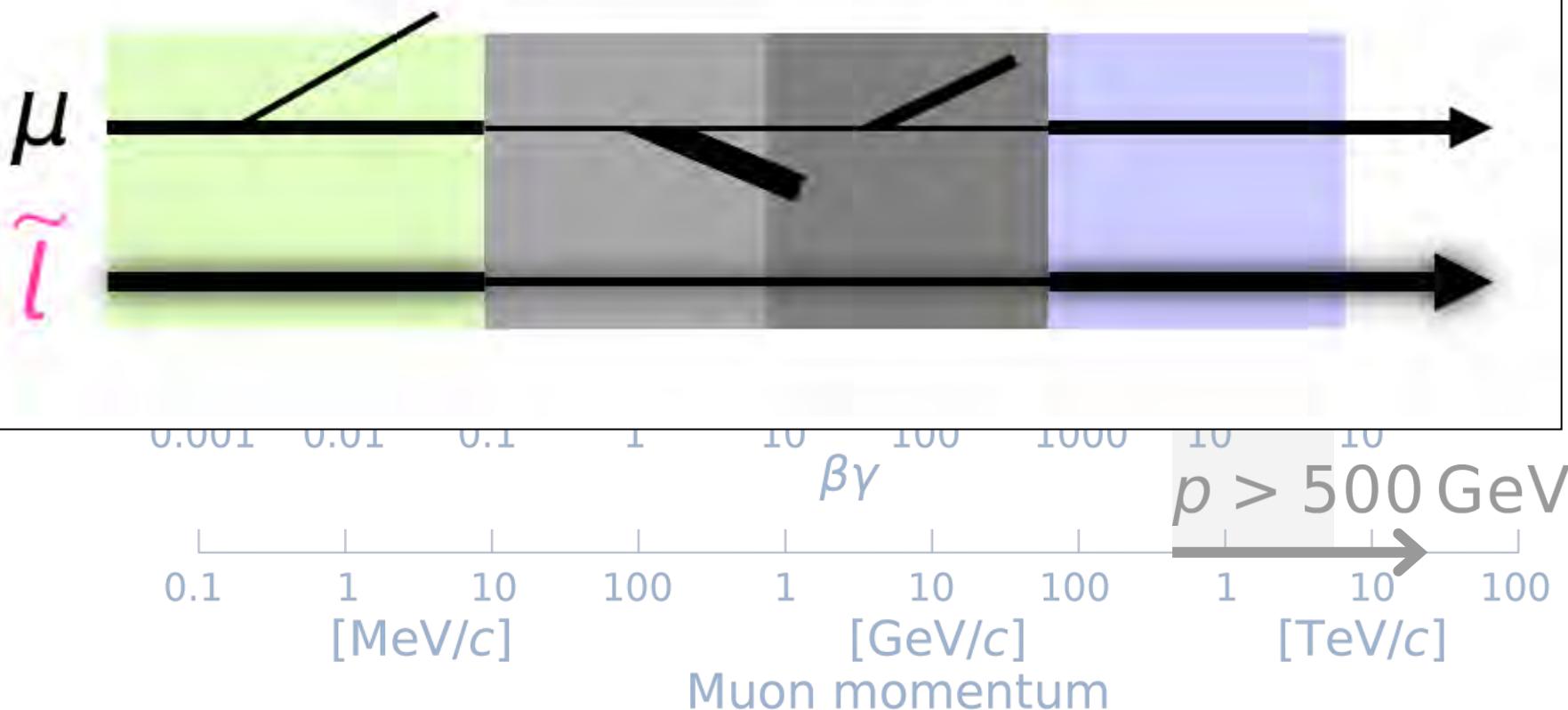
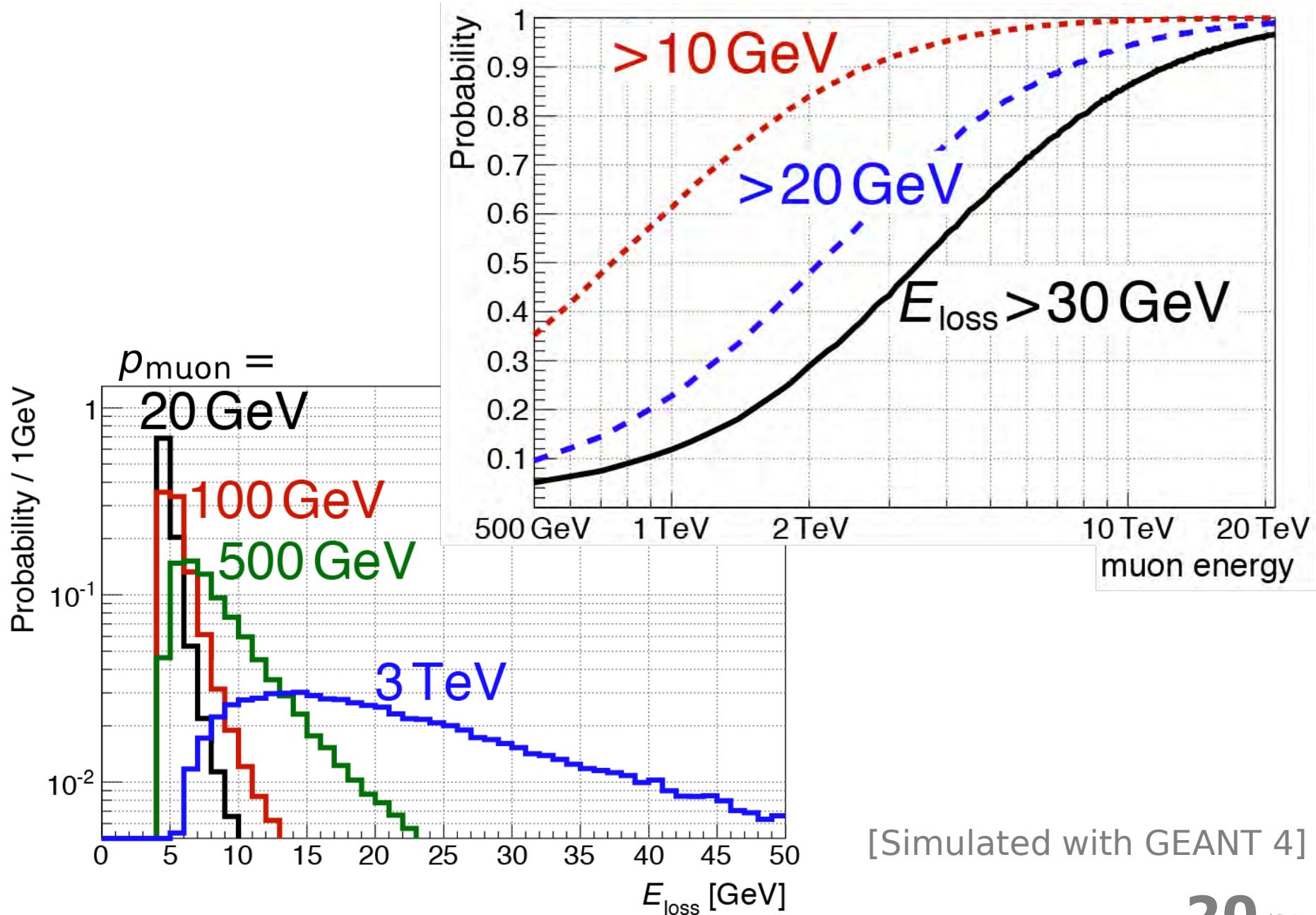


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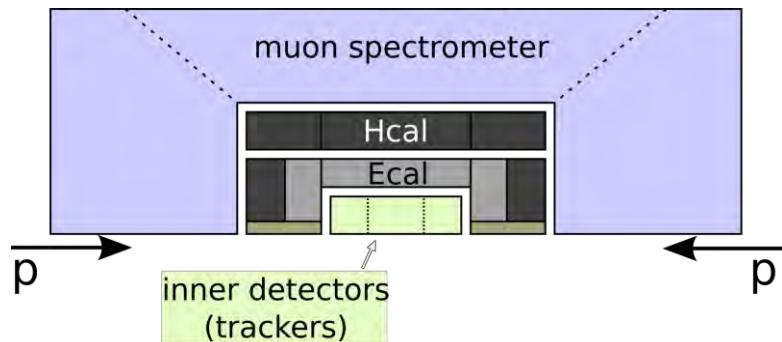
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### ■ Detector

- similar to ATLAS/CMS
- $\beta$ -resolution same as ATLAS  
(resolution: 2.4%)



### ■ Signal: Madgraph5 + Pythia6 + Delphes3 (calculated at the LO)

### ■ BKG: “Snowmass 2013” BKG set for 100TeV (publicly available)

### ■ Pile-up not considered

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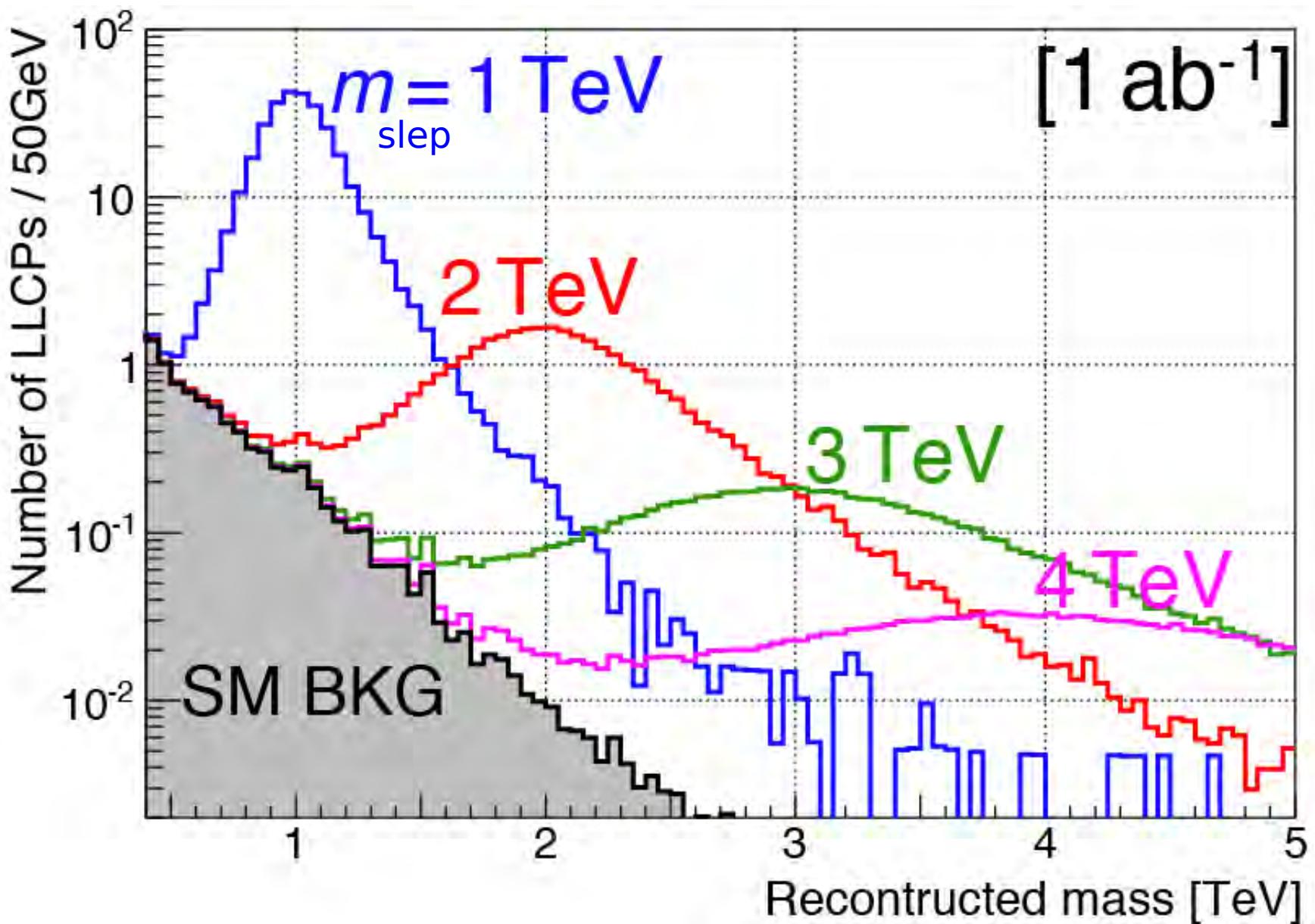
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reconstructed “muon” w.

- $p_T > 500 \text{ GeV}$
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- $E_{\text{loss}} < 30 \text{ GeV}$

**■ Event selection**

- two  $\tilde{l}$ -candidates



LLCP selection flow ( $\int L = 1 \text{ ab}^{-1}$ )

	signal		SM	BKG
	$\tilde{l} = 1 \text{ TeV}$	$3 \text{ TeV}$		
total	2570	31.8	—	
$p_T$ & $\eta$	1840	28.5	$9.19 \times 10^6$	
$\beta$	1230	24.6	$3.41 \times 10^5$	
$E_{\text{loss}}$	1230	24.6	$2.78 \times 10^5$	
$\epsilon_{\text{acc}} \epsilon_{\text{eff}}$	48%	77%	—	

Event categorization ( $\int L = 1 \text{ ab}^{-1}$ )

	1 TeV	3 TeV	BKG
$N_{\text{LLCP}} = 0$	483	1.34	(a lot)
$N_{\text{LLCP}} = 1$	378	4.46	$2.78 \times 10^5$
$N_{\text{LLCP}} = 2$	424	10.1	34.6

SR

■  $\tilde{l}$ -selection flow

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$E_{\text{loss}}$  reduces **34%** of BKG  
( $\because 0.82^2 = 0.66$ )

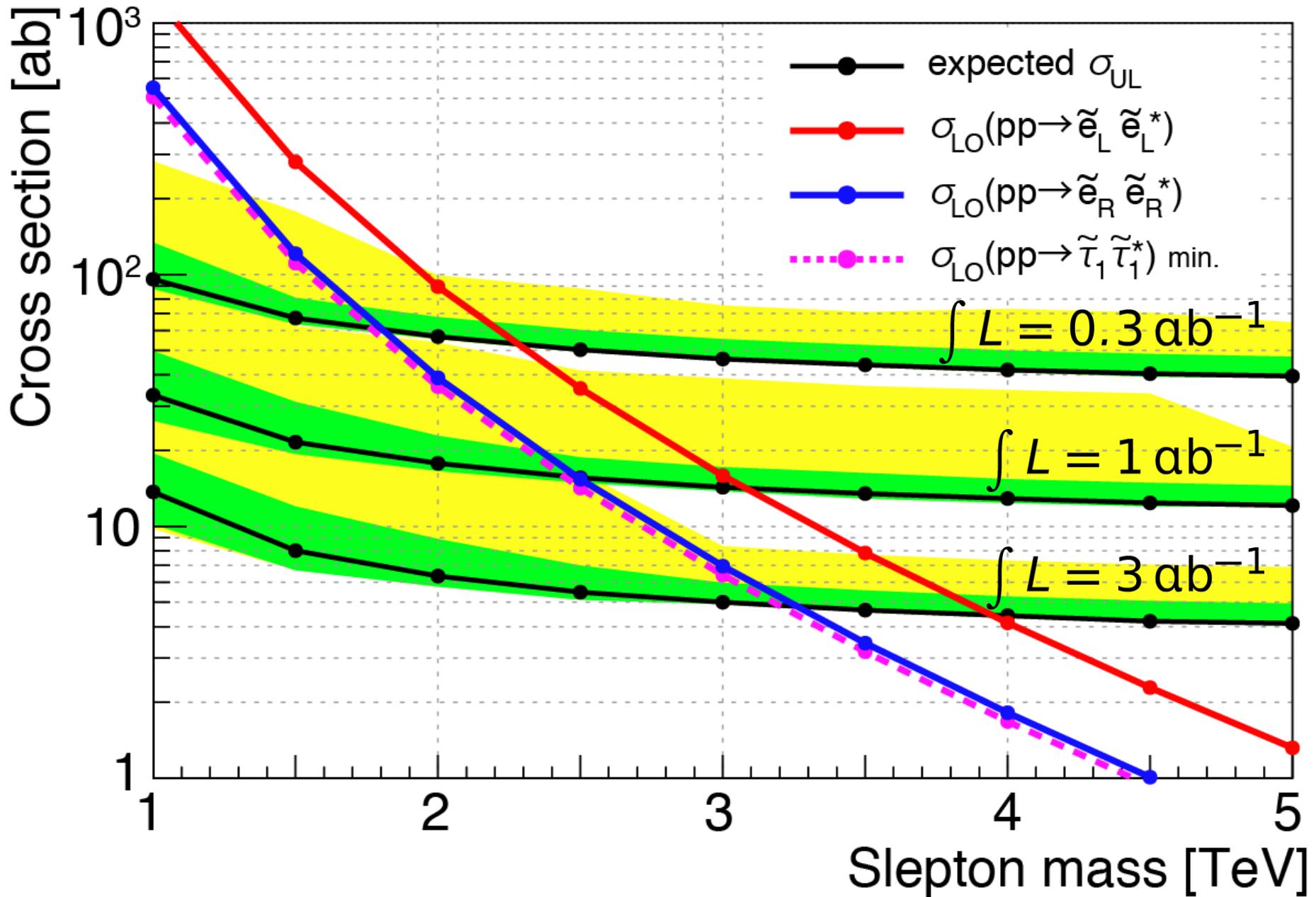
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- $\times 0.82$
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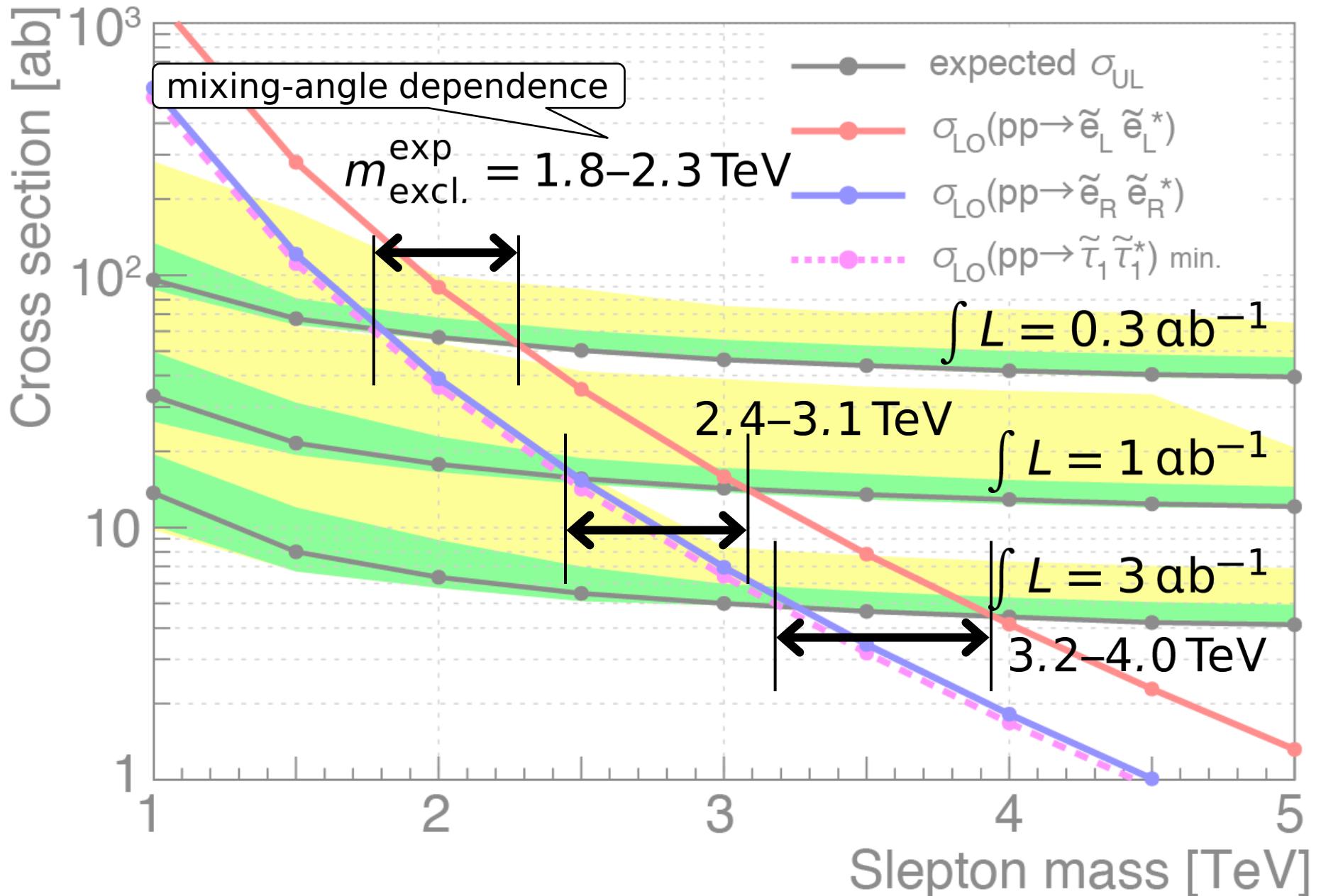
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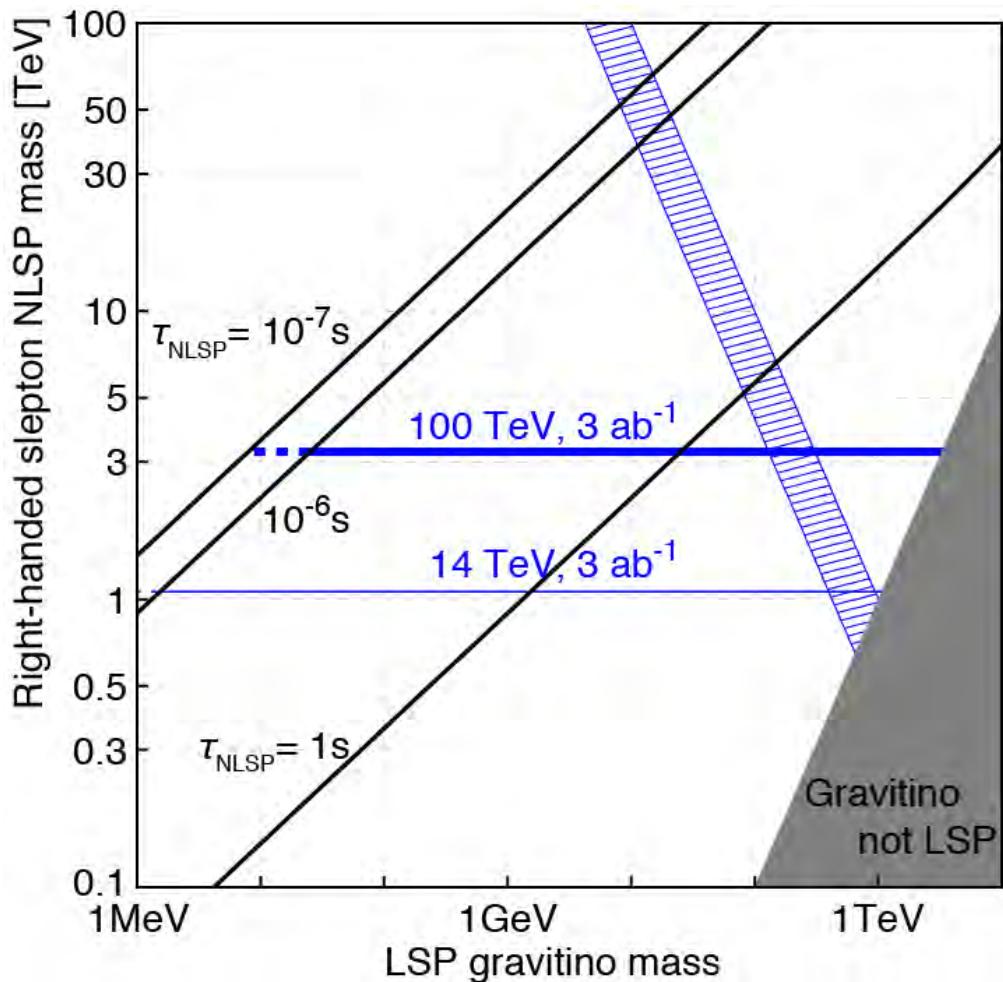
- Event selection
  - two  $\tilde{l}$ -candidates





## Implication to Cosmology

- SuperWIMP scenario



- $\tilde{B}-\tilde{l}$  co-annihilation  
...  $m_{\tilde{l}} \lesssim 600 \text{ GeV}$

covered @ LHC

## Conclusion

### $\tilde{t}$ -selection flow

reconstructed “muon” w.

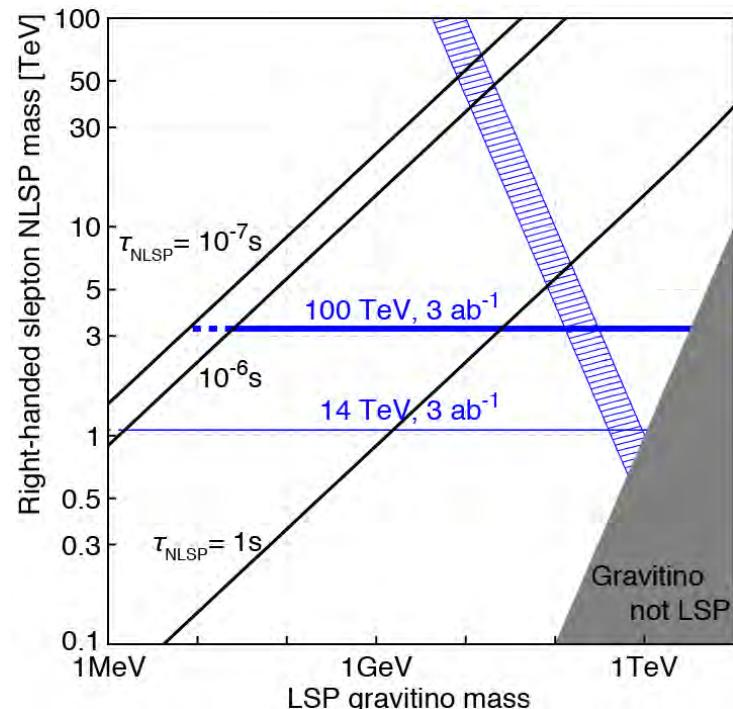
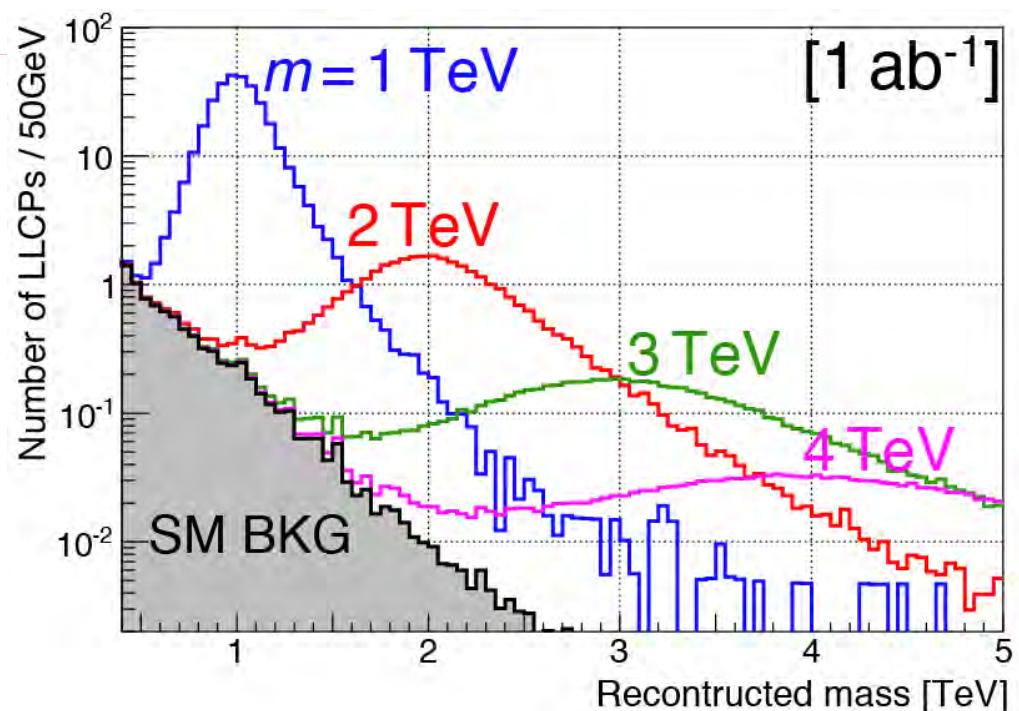
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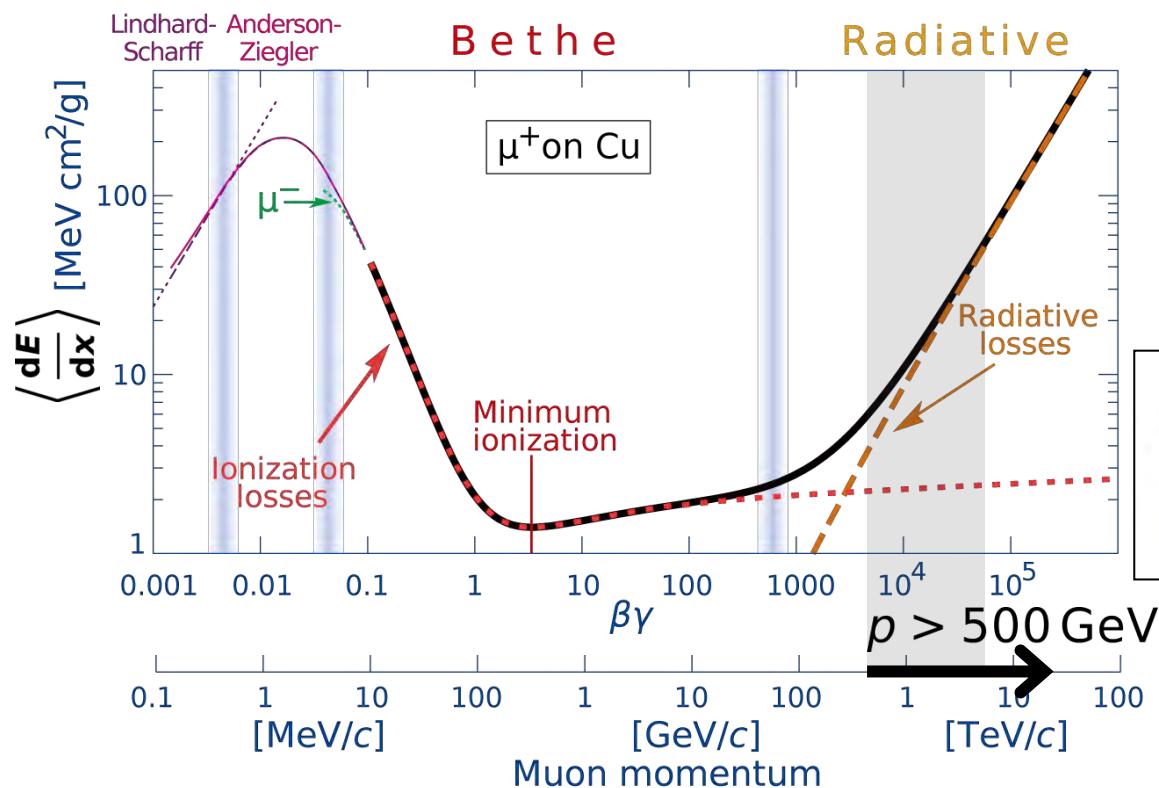


SR

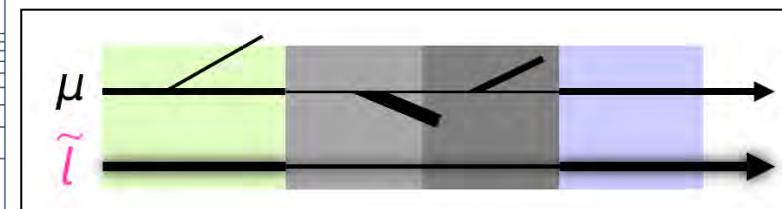
■ Expected exclusion reach @100 TeV

$$m_{\text{excl.}}^{\text{exp}} = \begin{cases} 1.8\text{--}2.3 \text{ TeV} & (0.3 \text{ ab}^{-1}) \\ 2.4\text{--}3.1 \text{ TeV} & (1.0 \text{ ab}^{-1}) \\ 3.2\text{--}4.0 \text{ TeV} & (3.0 \text{ ab}^{-1}) \end{cases}$$

■ “Muon radiative energy loss”



- Bremsstrahlung
- Photonuclear interaction
- $e^+e^-$  pair-production



→ 34% of BKG reduction



# Appendix: LHC Run 2

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# 1. How searched at the LHC?

## 2. at 100 TeV collider?

- Muon radiative energy loss for BKG reduction

## 3. Our simulation

- Expected reach:  $m_{\tilde{l}}$

### A. Note on momentum resolution

### B. 14 TeV LHC

## ■ Detector

- similar to ATLAS/CMS
- $\beta$ -resolution same as ATLAS  
(resolution: 2.4%)

## ■ Signal: Madgraph5 + Pythia6 + Delphes3 (calculated at the LO)

## ■ BKG: “Snowmass 2013” BKG set for 14 TeV (publicly available)

## ■ Pile-up not considered

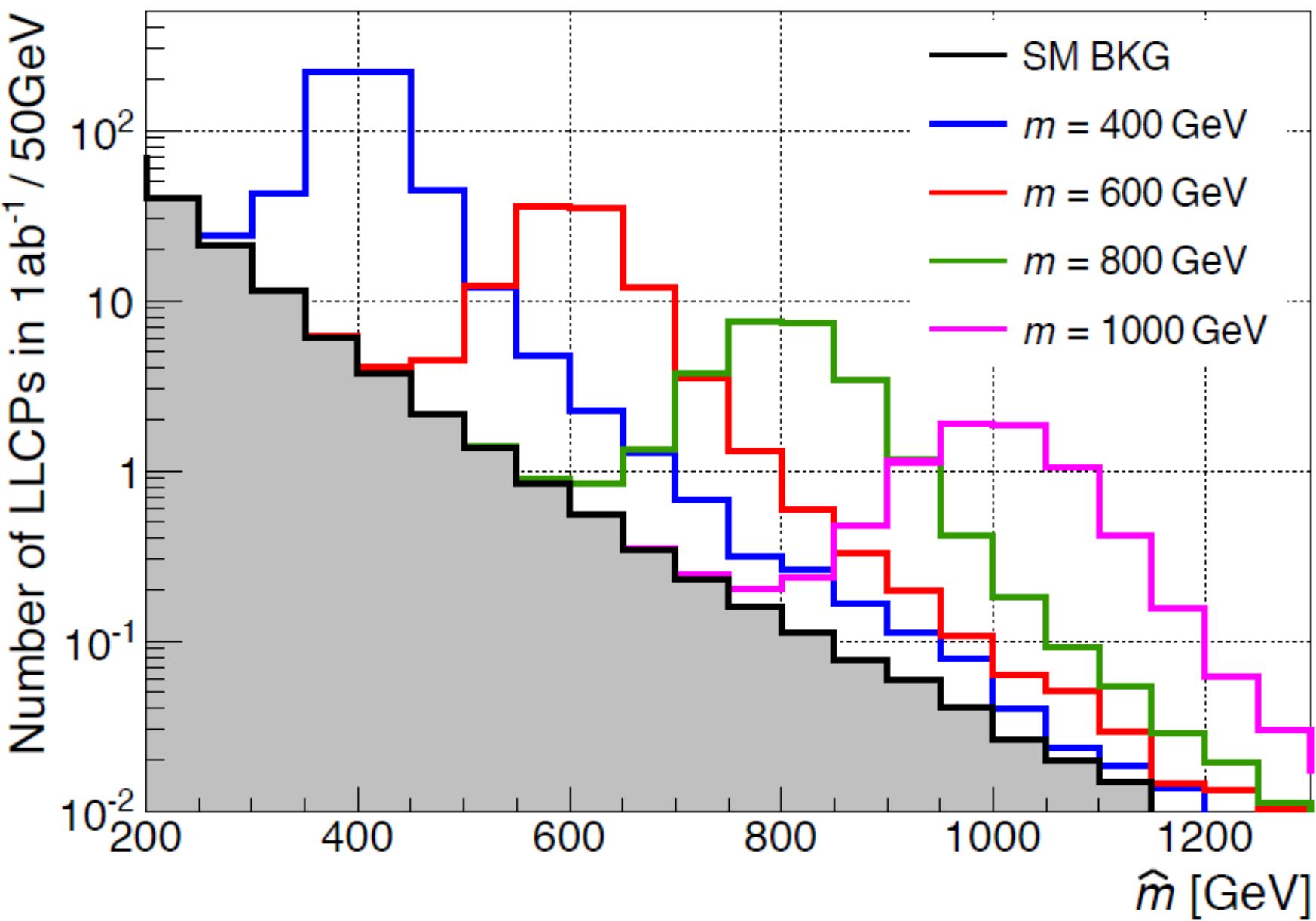
## ■ $\tilde{l}$ -selection flow

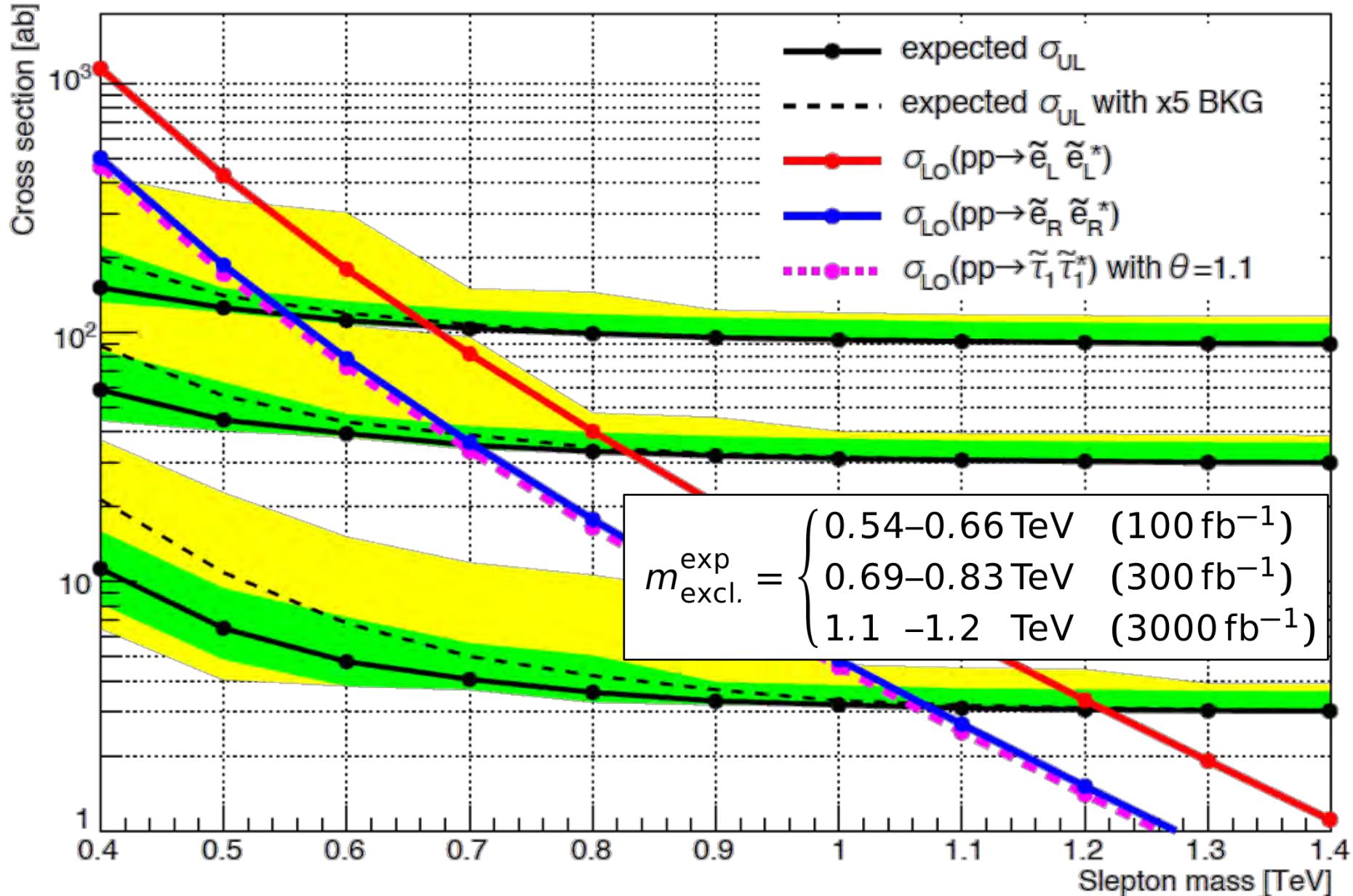
reconstructed “muon” w.

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- $|\eta| < 2.4$
- $0.3 < \hat{\beta} < 0.95$
- ~~$E_{\text{loss}} < 30 \text{ GeV}$~~

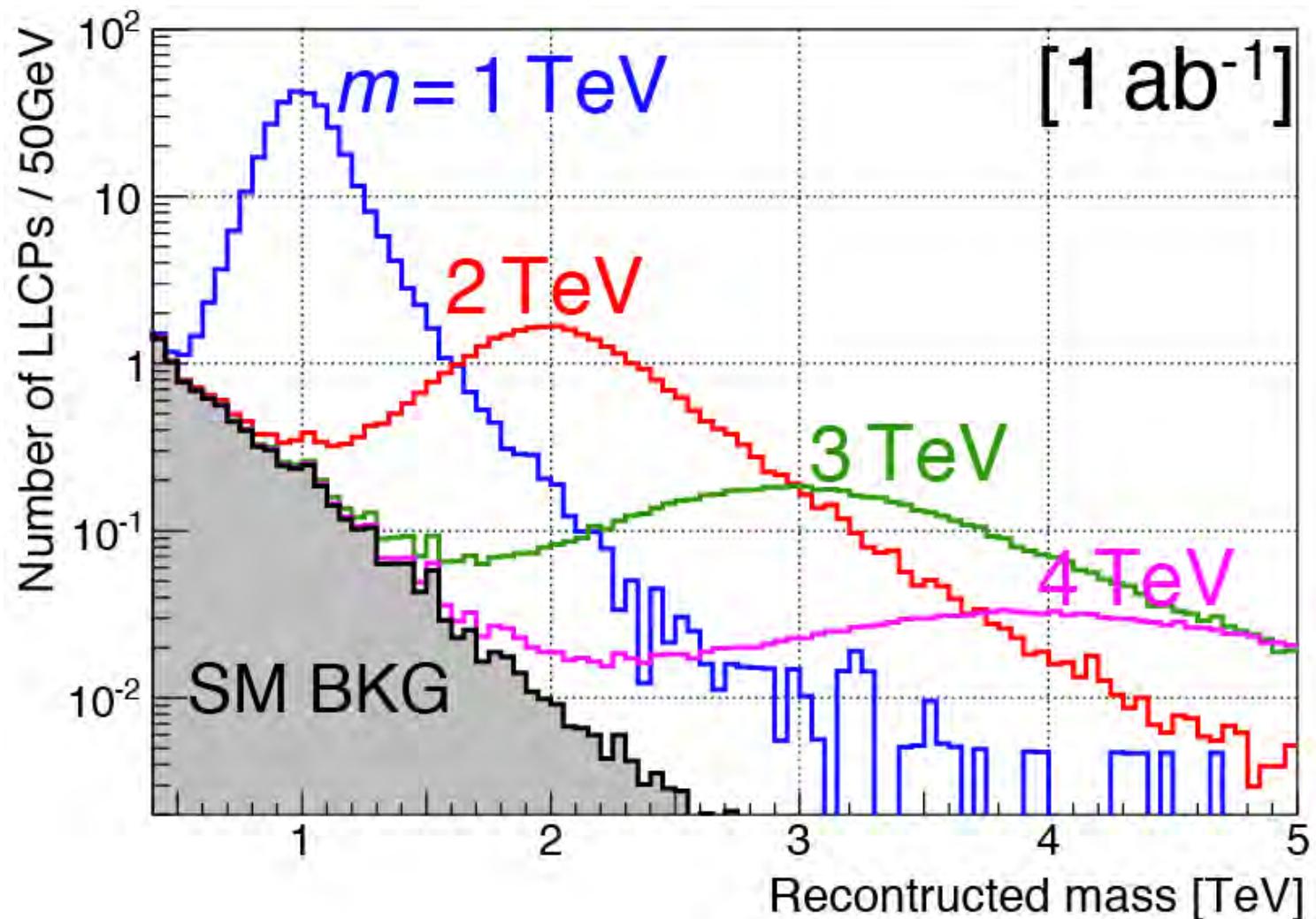
## ■ Event selection

- two  $\tilde{l}$ -candidates





The mass resolution is very bad?

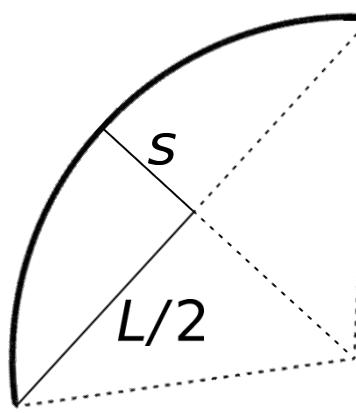


$$\left( = \frac{p}{\beta\gamma} = \frac{p_T \cosh \eta}{\beta\gamma} \right)$$

# Appendix: Momentum resolution @100TeV

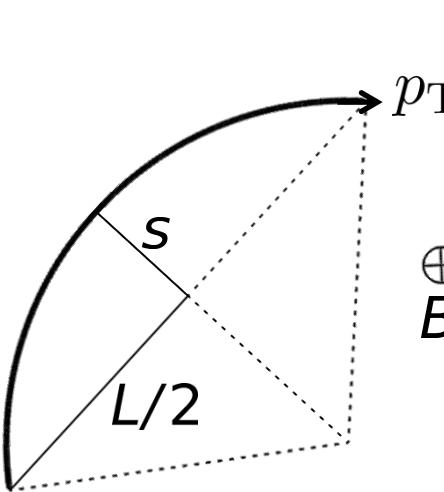
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## Momentum resolution for very-large $p_T$



The diagram shows a quarter-circle arc representing the path of a charged particle in a uniform magnetic field  $B$ . The radius of the arc is labeled  $L/2$ . A dashed line from the center to the arc is labeled  $s$ , representing the impact parameter. A curved arrow at the top indicates the direction of particle motion.

$$p_T = \frac{L^2}{8s} |q|B \quad \Rightarrow \quad \Delta p_T = \frac{L^2 |q|B}{8} \frac{\Delta s}{s^2}$$
$$= \frac{8\Delta s}{L^2 |q|B} \cdot p_T^2$$
$$\therefore \Delta p_T \propto p_T^2$$



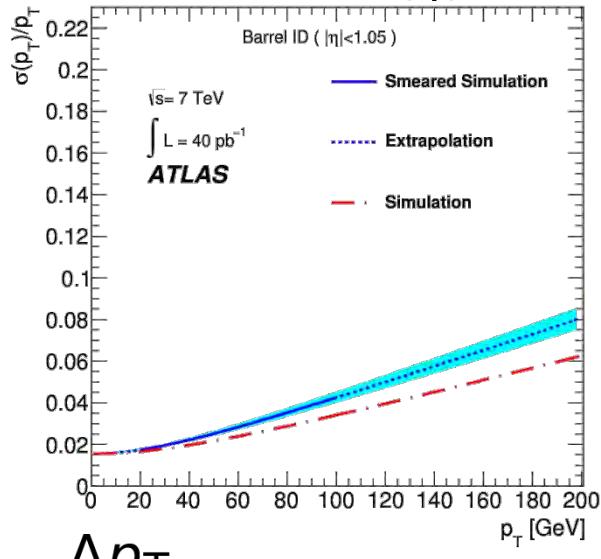
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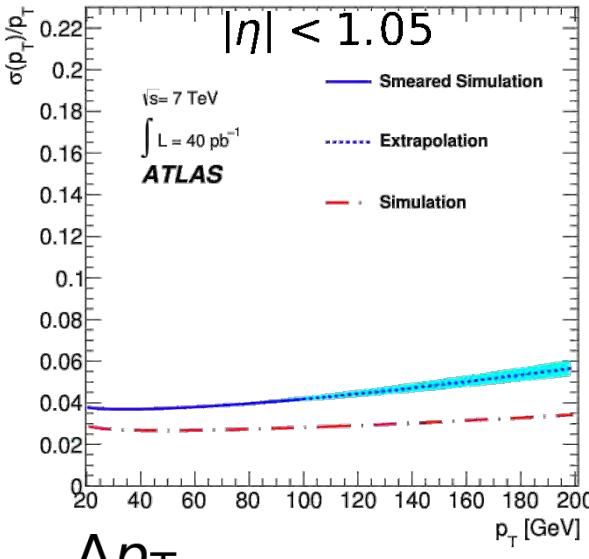
## ATLAS 7 TeV results on muon momentum resolution

Inner Detector,  $|\eta| < 1.05$

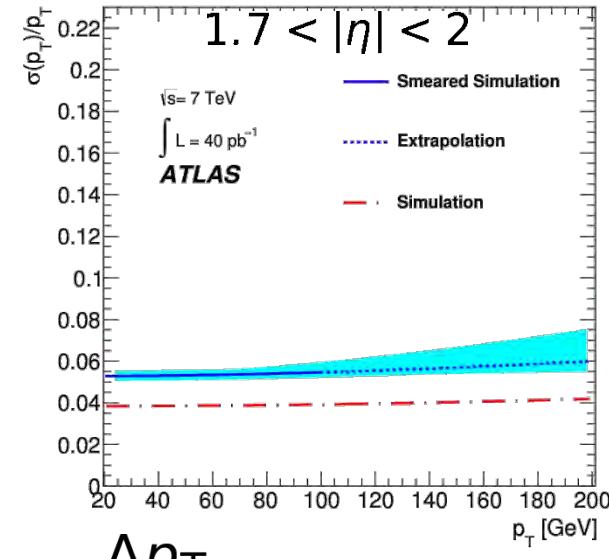


$$\frac{\Delta p_T}{p_T} \sim 0.38 p_T / \text{TeV}$$

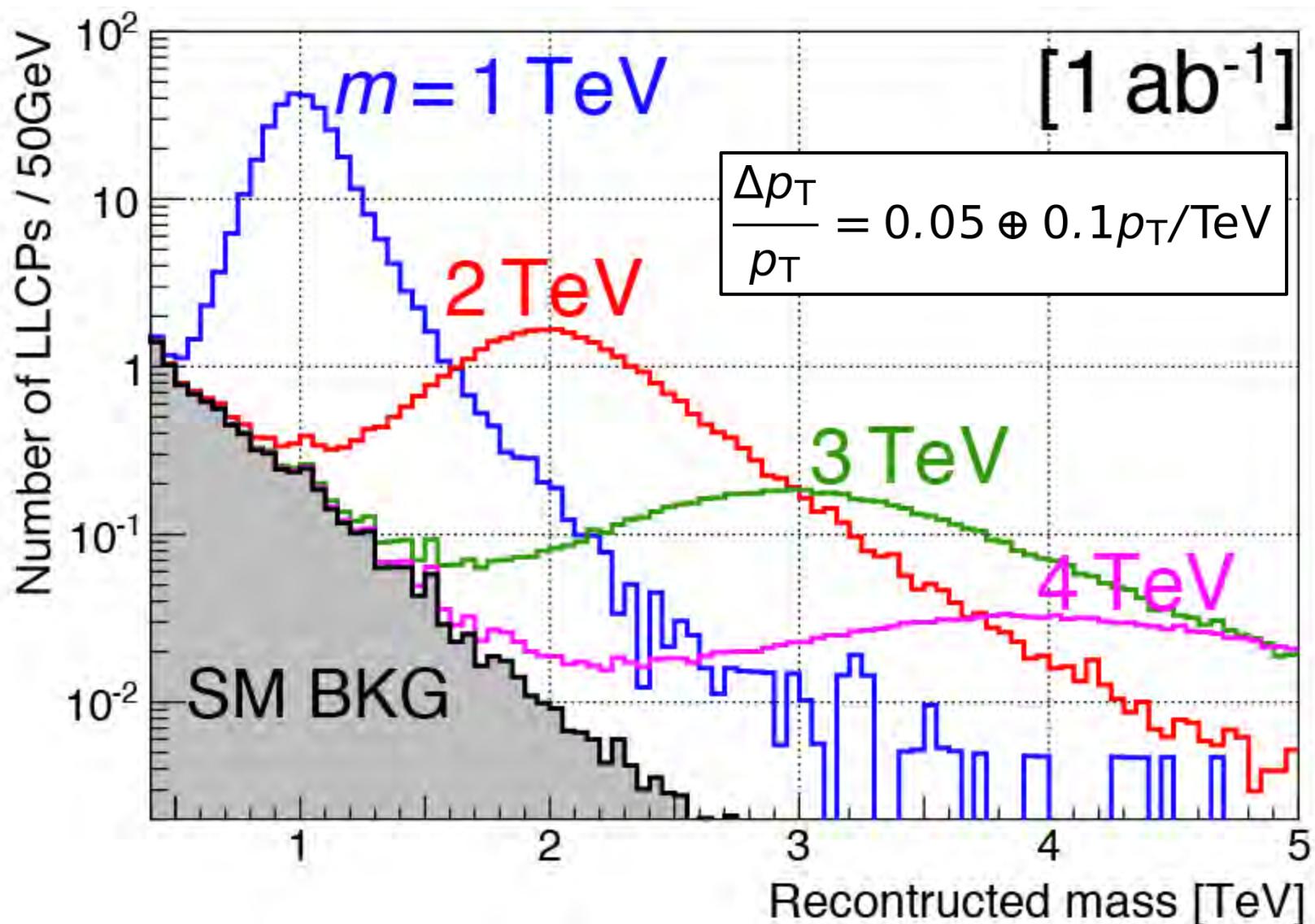
Muon spectrometer

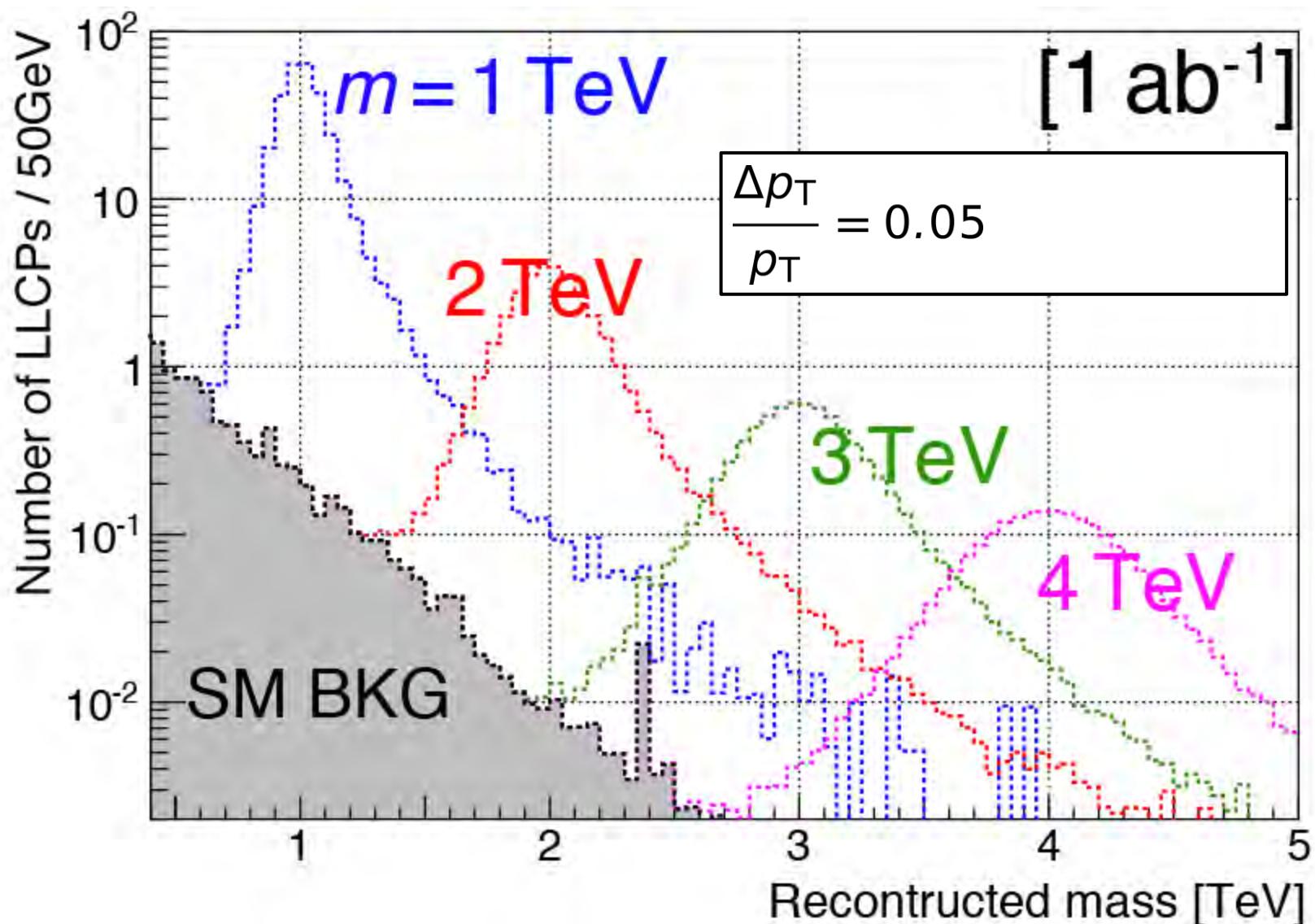


$$\frac{\Delta p_T}{p_T} \sim 0.14 p_T / \text{TeV}$$



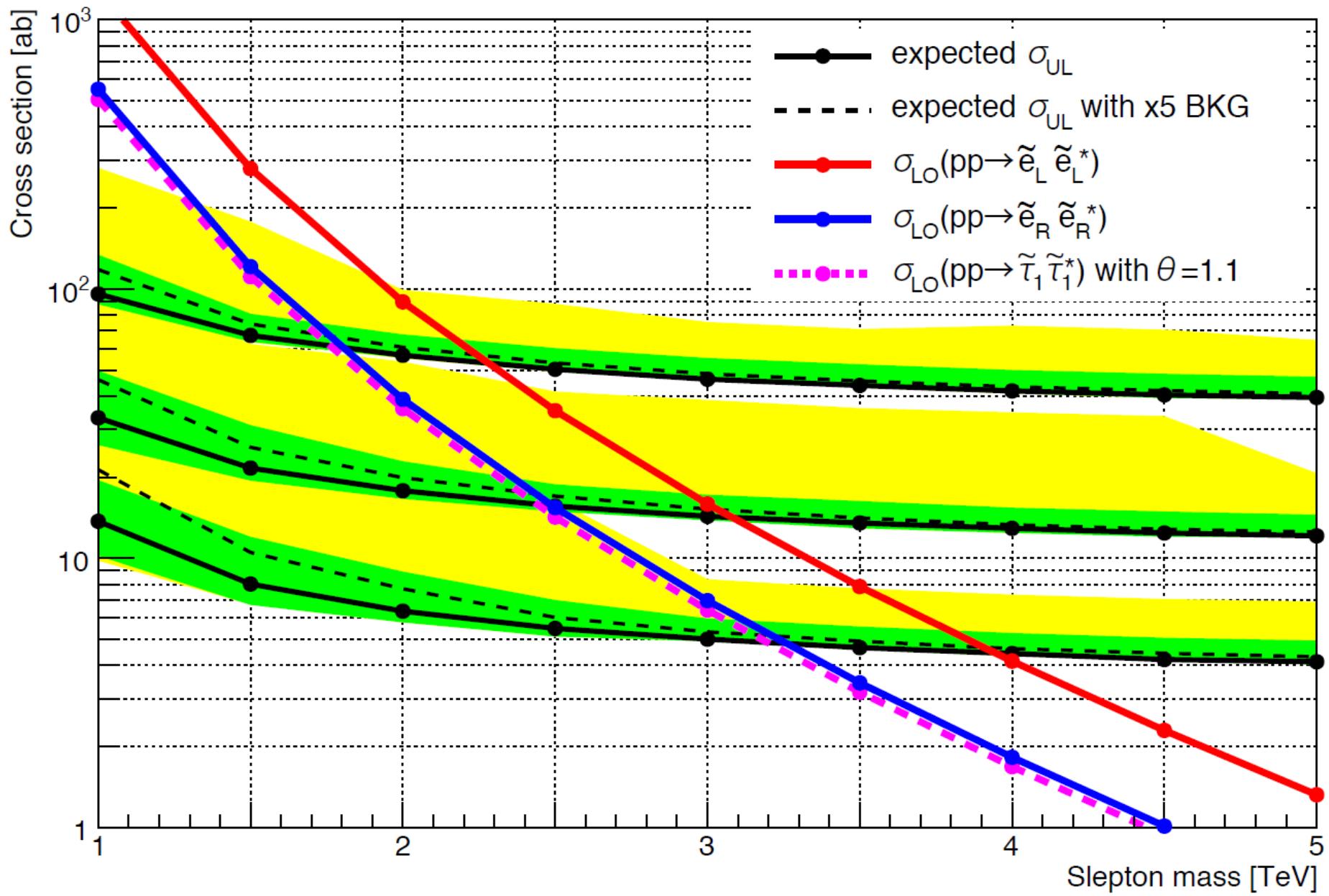
$$\frac{\Delta p_T}{p_T} \sim 0.06 p_T / \text{TeV}$$

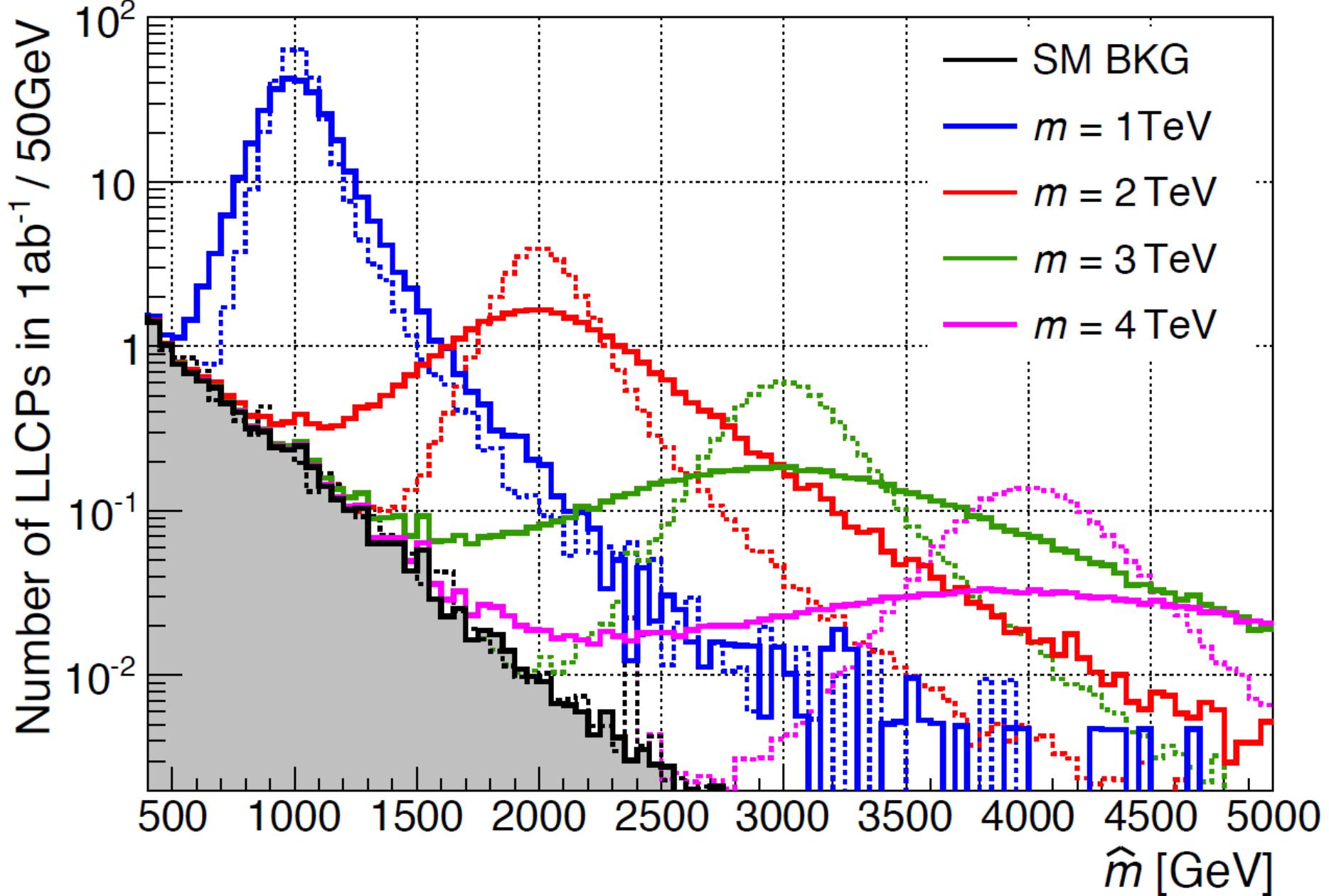


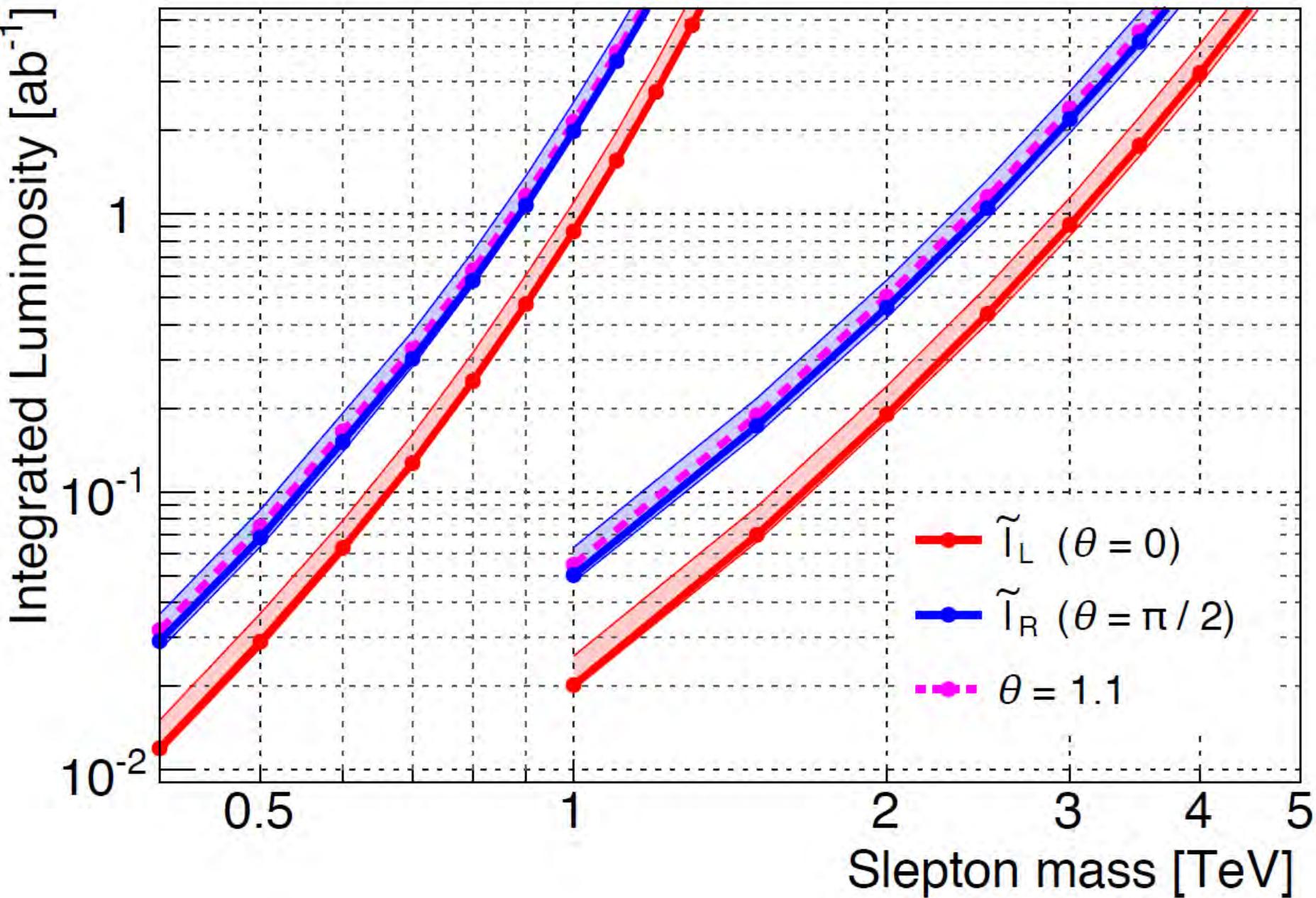


# Detailed Figures (100TeV)

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Why  $\beta > 0.4$ ? (slepton  $dE/dx$ )

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Lindhard-  
Scharff    Anderson-  
Ziegler

# B e t h e

# Radiative

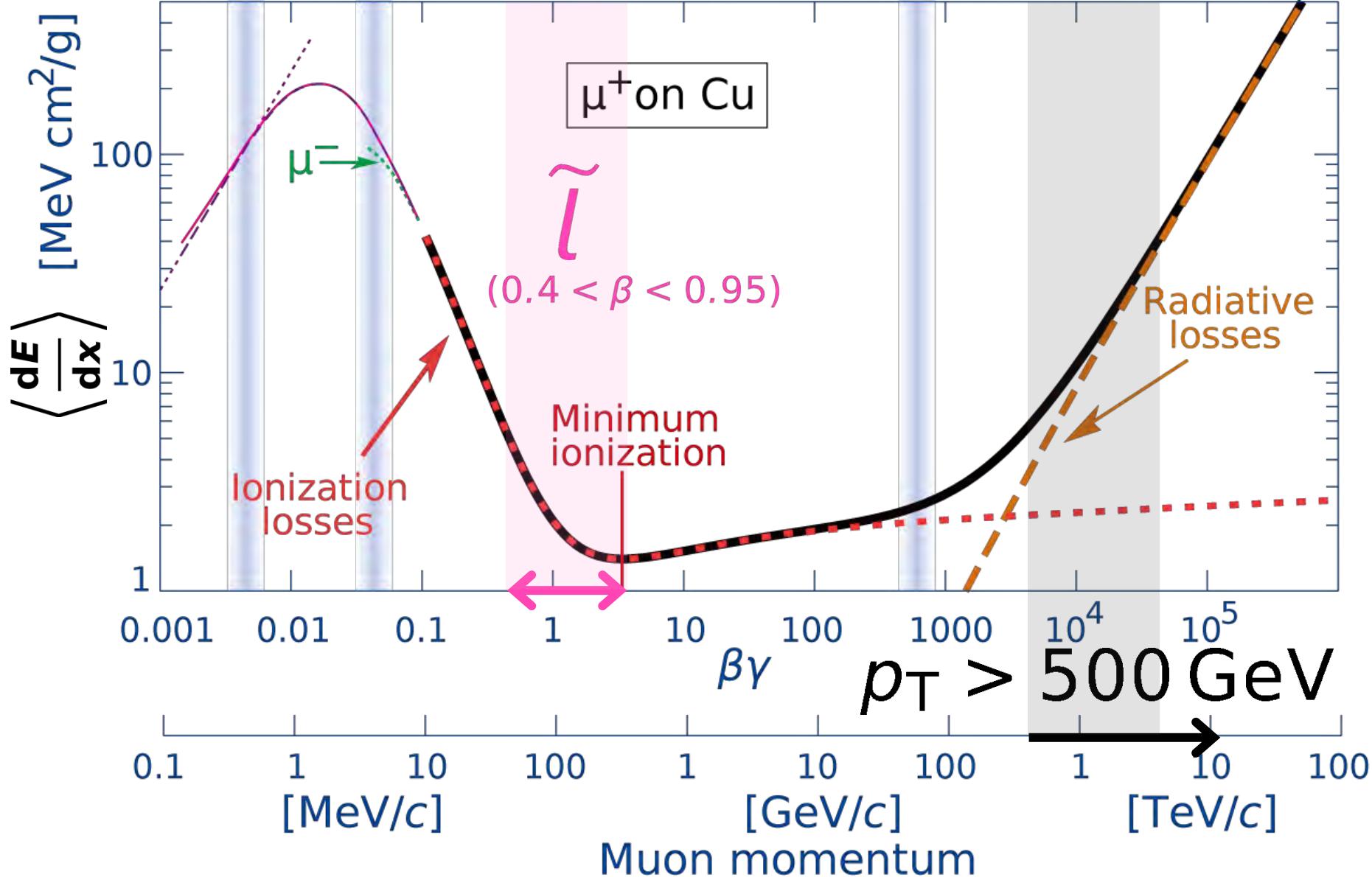
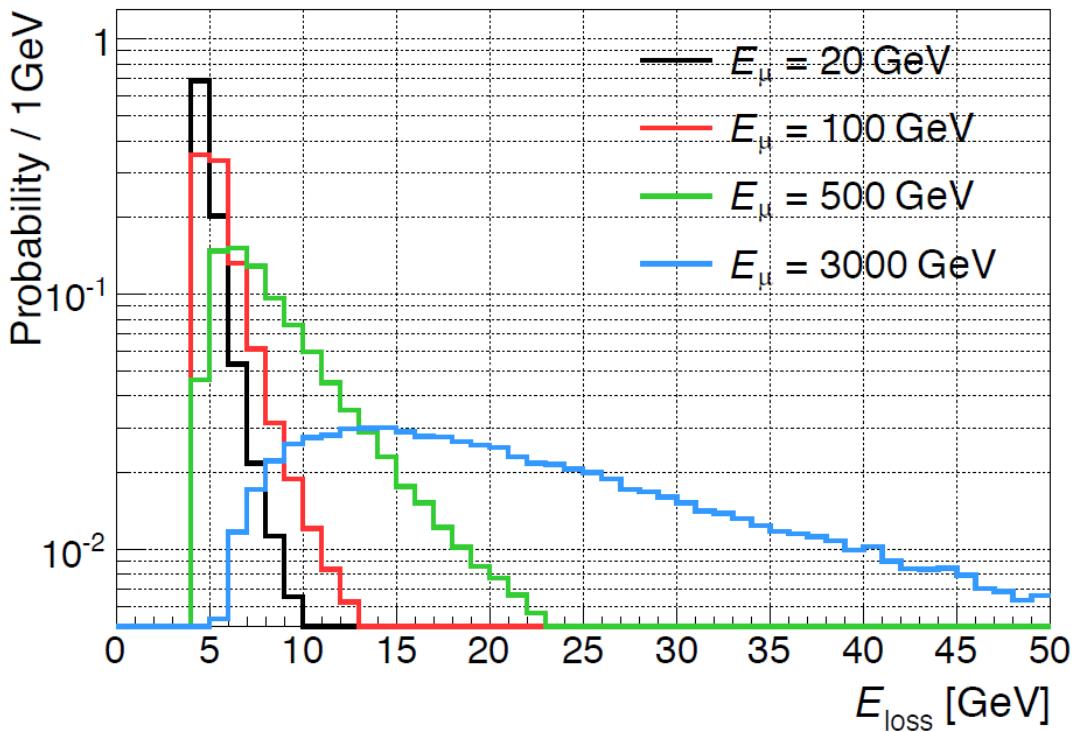
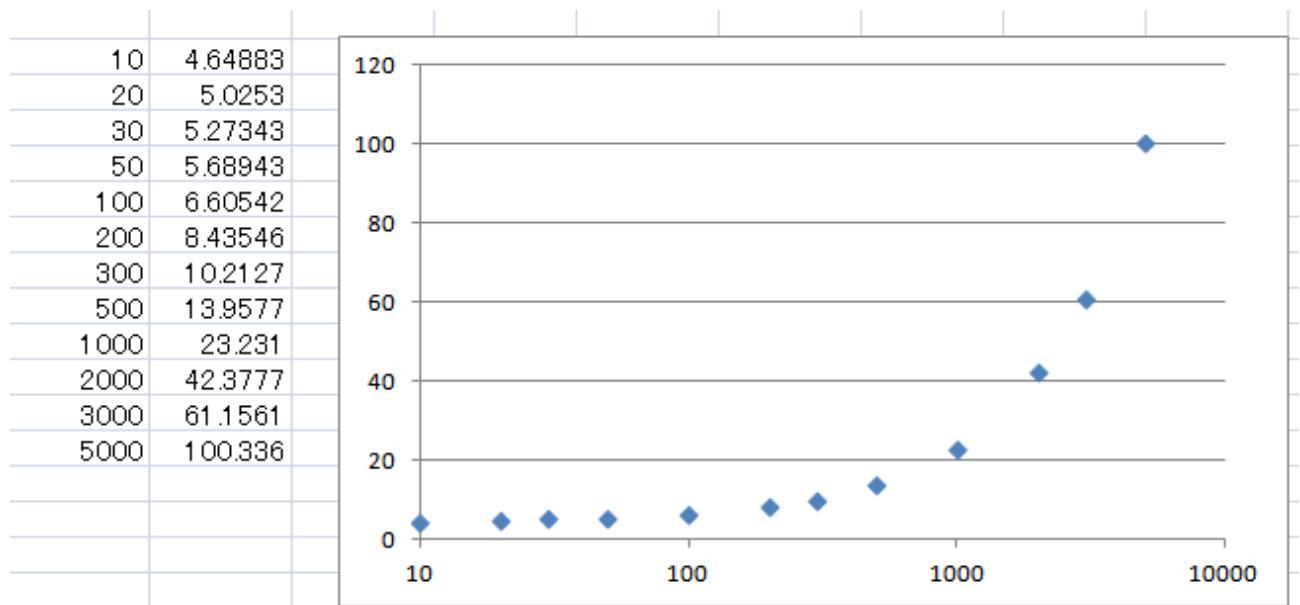


Figure from Groom, Mokhov, Striganov, [Atom. Nucl. Data Tab. 78](#) (2001) 183-356  
[also in PDG Review "Passage of particles through matter"]

Mean value of  $E_{\text{loss}}$ ?

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# Averaged muon energy loss in 3m iron (internal)



Note that the mean is much larger than the median because of its long long long tail.

$dE/dx$  to measure  $\beta$

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## Mass measurement = Measurement of velocity $\beta$

### ■ TOF : time-of-flight

$$\beta = \Delta L / \Delta t$$

### ■ $dE/dx$ : ionization energy loss

