



# SUSY (with explaining $(g - 2)_\mu$ ) at the LHC

Sho IWAMOTO (岩本 祥)

Kavli IPMU, the University of Tokyo

1 May 2013  
ACP Seminar @ Kavli IPMU

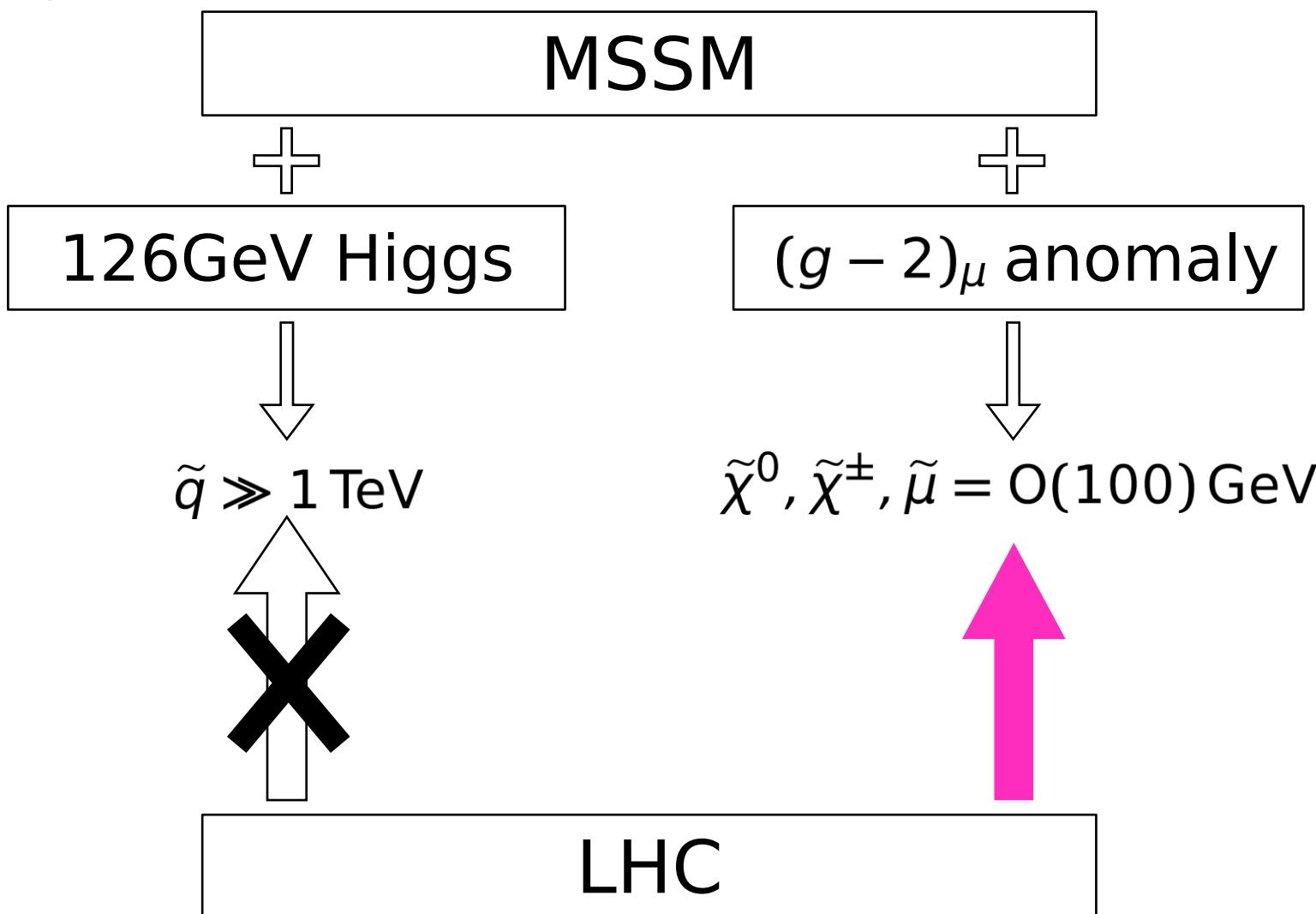
## References

Endo, Hamaguchi, SI, Yoshinaga [[1203.4256](#)].

Endo, Hamaguchi, SI, Yokozaki [[1108.3071](#)][[1112.5653](#)][[1202.2751](#)];  
Endo, Hamaguchi, Ishikawa, SI, Yokozaki [[1212.3935](#)].

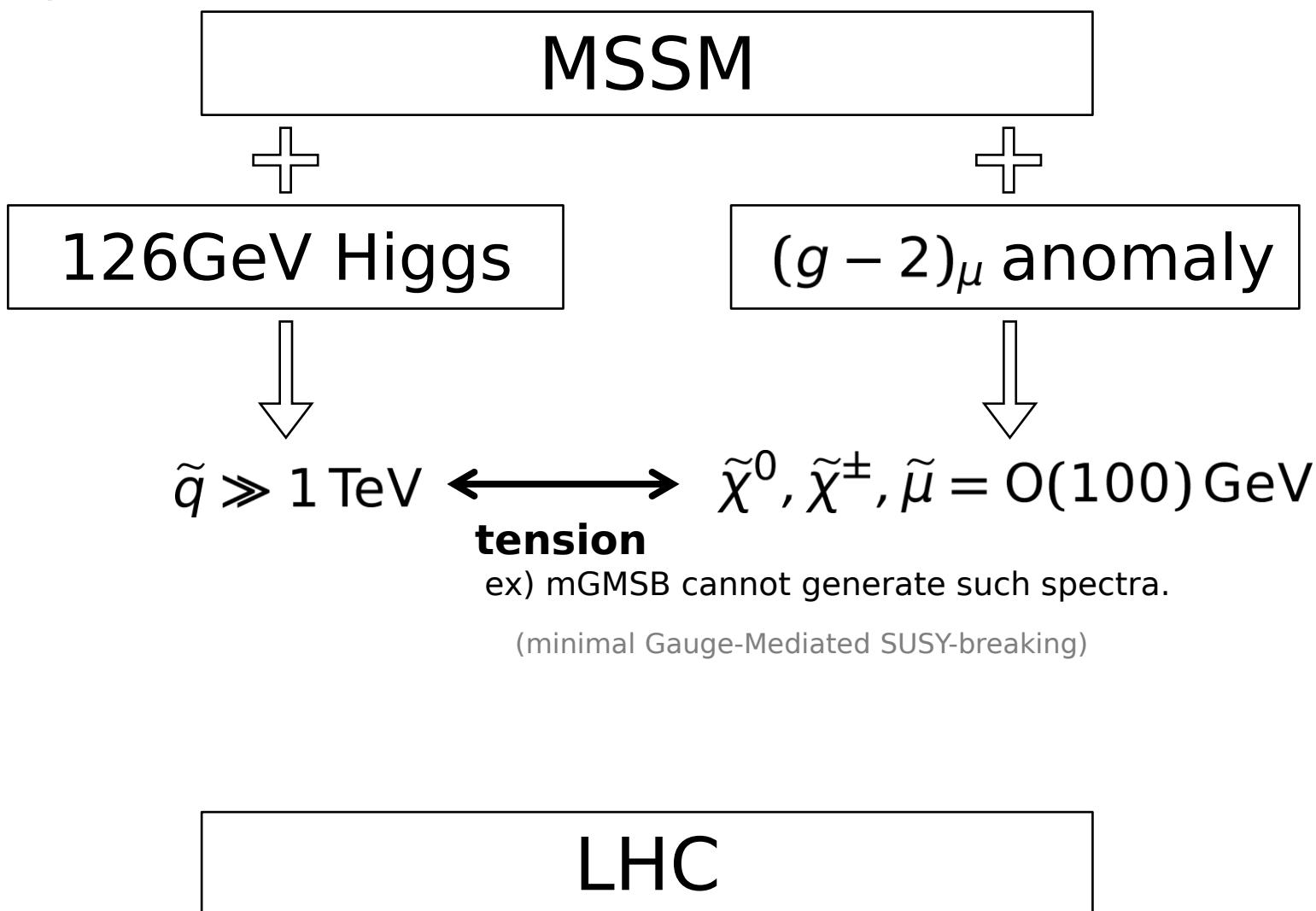
## ● Topic 1.

(Minimal SUSY Standard Model)



## ① Topic 2.

(Minimal SUSY Standard Model)



## ● Topic 2.

(Minimal SUSY Standard Model)

**MSSM + vector-like quarks**

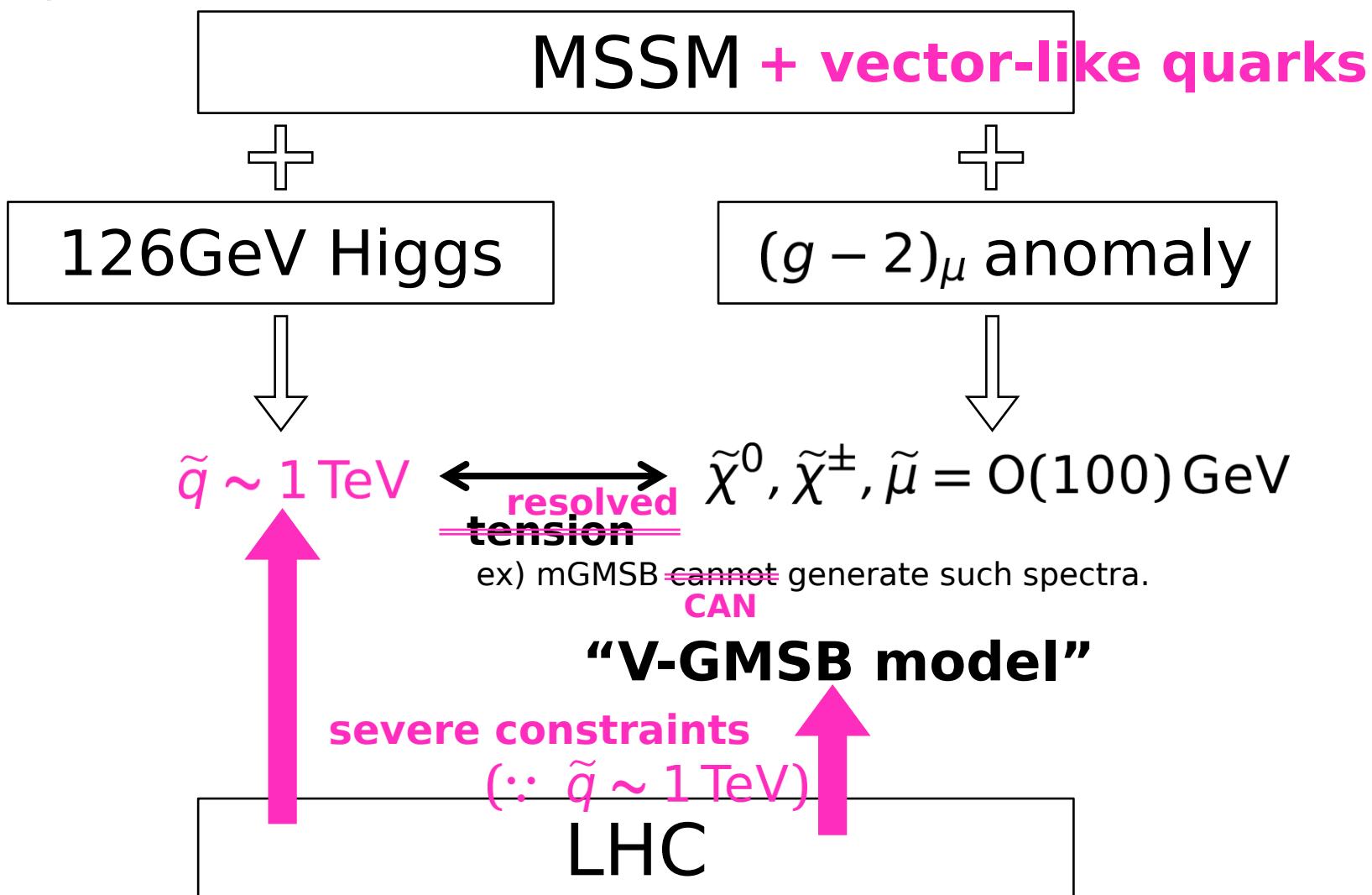
126GeV Higgs

 $(g - 2)_\mu$  anomaly $\tilde{q} \sim 1 \text{ TeV}$   $\longleftrightarrow$   $\tilde{\chi}^0, \tilde{\chi}^\pm, \tilde{\mu} = \mathcal{O}(100) \text{ GeV}$ resolved tensionex) mGMSB ~~cannot~~ CAN generate such spectra.**“V-GMSB model”**

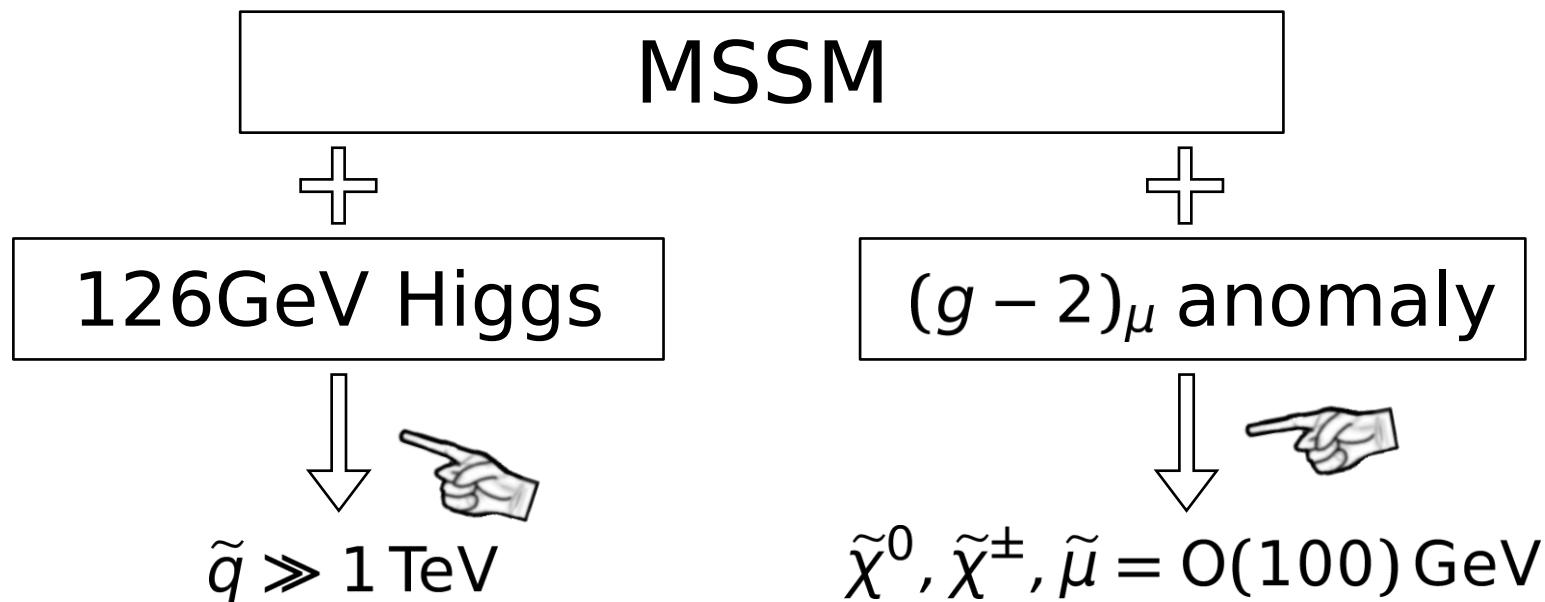
LHC

## ● Topic 2.

(Minimal SUSY Standard Model)



## 1. Foundation



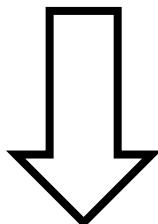
## 2. Topic 1) $\tilde{\chi}^0, \tilde{\chi}^\pm, \tilde{\mu}$ direct-search

## 3. Topic 2) V-GMSB model

[ (MSSM + vector-like quarks) + GMSB]

# Standard Model Now Completed!

- Problems
  - Hierarchy Problem, muon  $g - 2$  anomaly, ...
- Anxiety towards ultimate theory



**Supersymmetry (SUSY)**

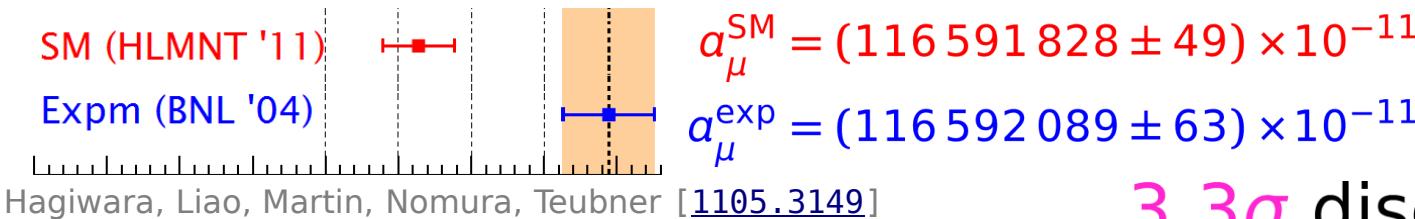
## MSSM (Minimal SUSY Standard Model)

- hierarchy : solved. (or relaxed.)
- $(g - 2)_\mu$  anomaly : explained.
- gauge coupling unification : improved.

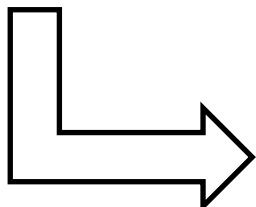
## Muon $g-2$ Problem

### • $(g-2)_\mu$ anomaly

$$\left( a_\mu := \frac{g_\mu - 2}{2} \right)$$



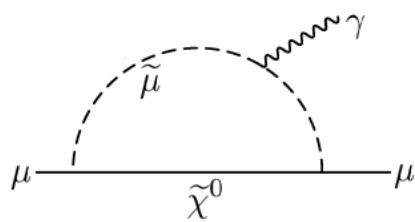
3.3 $\sigma$  discrepancy



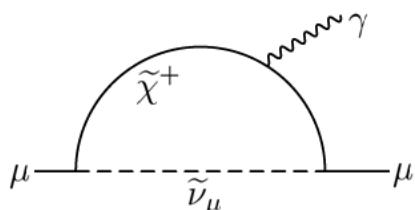
can be explained with **MSSM**

if  $\mu$ -term > 0,  $\tan \beta \gtrsim 10$ ,

and  $m(\tilde{\chi}^0, \tilde{\chi}^\pm, \tilde{\mu}, \tilde{\nu}_\mu) \sim O(100) \text{ GeV}$ .



$$\Delta a_\mu (\tilde{\chi}^0, \tilde{\mu}) \approx \frac{g_Y^2}{(4\pi)^2} \frac{m_\mu^2}{m_{\text{soft}}^2} \text{sgn}(\mu) \tan \beta + \dots,$$



$$\Delta a_\mu (\tilde{\chi}^\pm, \tilde{\nu}) \approx \frac{g_2^2}{(4\pi)^2} \frac{m_\mu^2}{m_{\text{soft}}^2} \text{sgn}(\mu) \tan \beta.$$

Lopez, Nanopoulos, Wang [[ph/9308336](#)]  
 Chattopadhyay, Nath [[ph/9507386](#)]  
 Moroi [[ph/9512396](#)]

$W \ni \mu H_u H_d$  (Higgsino mass term),       $\tan \beta = \frac{\langle H_u \rangle}{\langle H_d \rangle}$ ,

$m_{\text{soft}}$  : SUSY-particle mass-scale,       $g_i$  : Gauge couplings.

tree
one-loop level (top-stop)

$$m_h^2 \approx m_Z^2 + \frac{3g_W^2 m_t^4}{8\pi^2 m_W^2} \left[ \ln \frac{m_{\tilde{t}}^2}{m_t^2} - \frac{(\alpha^2 - 6)^2}{12} + 3 \right]$$

where  $\alpha := A_t/m_{\tilde{t}}$ .  
(stop mixing parameter)

heavier  $m_h \iff$

- $\tilde{t}$  should be *heavy*  
and/or
- stop mixing parameter  $\alpha$  at sweet spot ( $\sim \pm \sqrt{6}$ ).

tree
one-loop level (top-stop)

$$m_h^2 \approx m_Z^2 + \frac{3g_W^2 m_t^4}{8\pi^2 m_W^2} \left[ \ln \frac{m_{\tilde{t}}^2}{m_t^2} - \frac{(\alpha^2 - 6)^2}{12} + 3 \right]$$

where  $\alpha := A_t/m_{\tilde{t}}$ .  
 (stop mixing parameter)

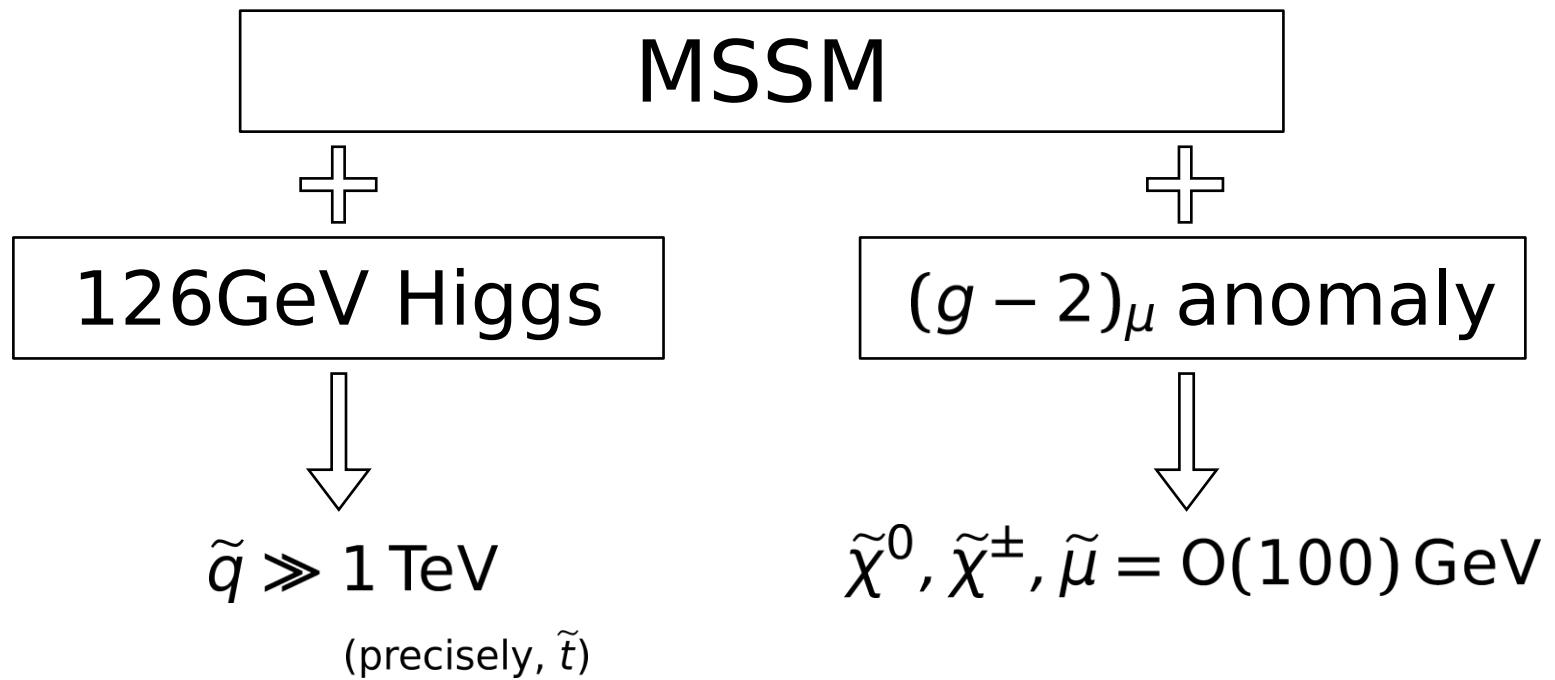
heavier  $m_h \iff m_{\tilde{t}} \sim \begin{cases} 1-2 \text{ TeV} & (\alpha \sim \pm \sqrt{6}) \\ 0(10) \text{ TeV} & (\alpha \sim 0) \end{cases}$

- $\tilde{t}$  should be heavy

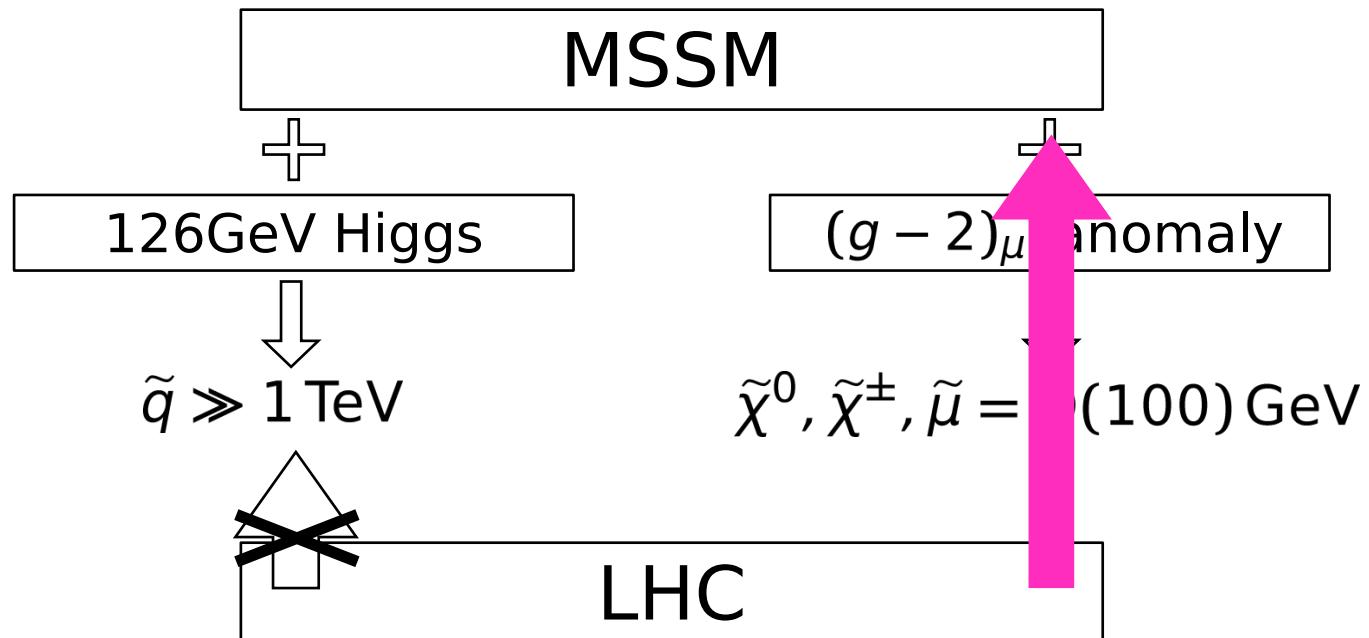
and/or

- stop mixing parameter  $\alpha$  at sweet spot ( $\sim \pm \sqrt{6}$ ).

Ibe, Yanagida [[1112.2462](#)]  
 Draper, Meade, Reece, Shih [[1112.3068](#)]



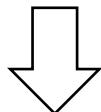
# Topic 1 : SUSY search respecting $(g - 2)_\mu$



# Where's SUSY?

- $m_h = 126 \text{ GeV} \rightarrow m_{\tilde{t}} = \mathcal{O}(1-10) \text{ TeV} ?$
- Nothing@LHC  $\rightarrow m(\tilde{q}, \tilde{g}) \gtrsim 1 \text{ TeV}.$

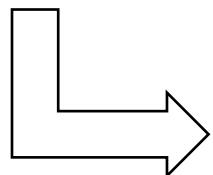
Colored = Heavy !?



## Non-colored Search!!!

Many params :  $\mu, \tan \beta, m_A; M_1, M_2, m_L^2, m_{\bar{E}}^2, \dots$

Various targets :  $\tilde{e}, \tilde{\mu}, \tilde{\tau}, \tilde{W}^\pm, \dots$



Use  $(g - 2)_\mu$  as a guide.

**$(g - 2)_\mu$ -motivated MSSM**

- squarks & stau ( $\tilde{\tau}, \tilde{\nu}_\tau$ ): **HEAVY**

↑(to simplify LHC analyses)

- sleptons &  $\tilde{\chi}^0, \tilde{\chi}^\pm \sim O(100) \text{ GeV}$

➤ sleptons:  $(\tilde{e}, \tilde{\nu}_e) = (\tilde{\mu}, \tilde{\nu}_\mu) \ll (\tilde{\tau}, \tilde{\nu}_\tau)$

➤ gauginos:  $M_1 : M_2 : M_3 = 1 : 2 : 6.$   
(approximate GUT relation)

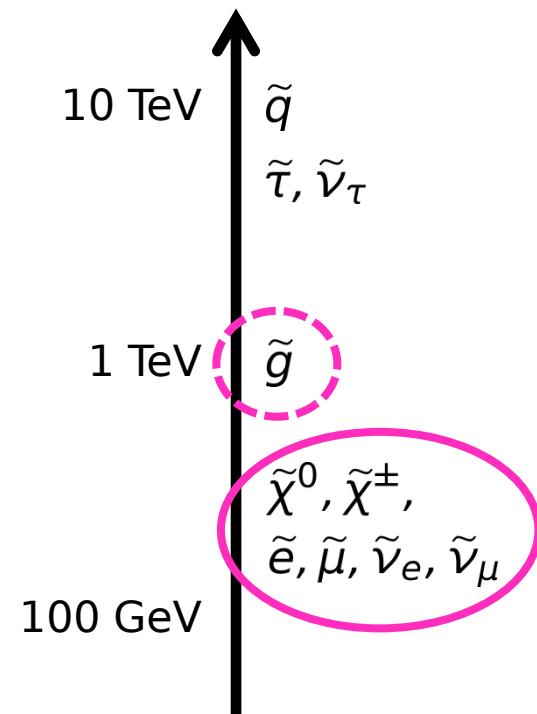
- A-terms = 0
- $\tan\beta = 40$
- $m_A = 1500 \text{ GeV}$  ( $B_s \rightarrow \mu\mu$  constr. satisfied.)
- $m_h = 126 \text{ GeV}$  is assumed. ( $\because \tilde{q}$  are decoupled.)
- R-parity conserved.

**Rest Params:**  $(m_L^2, m_{\tilde{E}}^2)$  : slepton soft-masses  
 $(M_2, \mu)$  : gaugino/Higgsino mass

All params are  
input @ TeV-scale.  
(PMSSM)

↓

**MODEL INDEPENDENT!!**



**Rest Params:**  $(m_L^2, m_{\tilde{E}}^2)$  : slepton soft-masses  
 $(M_2, \mu)$  : gaugino/Higgsino mass

### **Two extreme cases**

◎  $\tilde{\mu}_R$ -decoupled case  
 $(m_{\tilde{E}}^2 = (3 \text{ TeV})^2)$

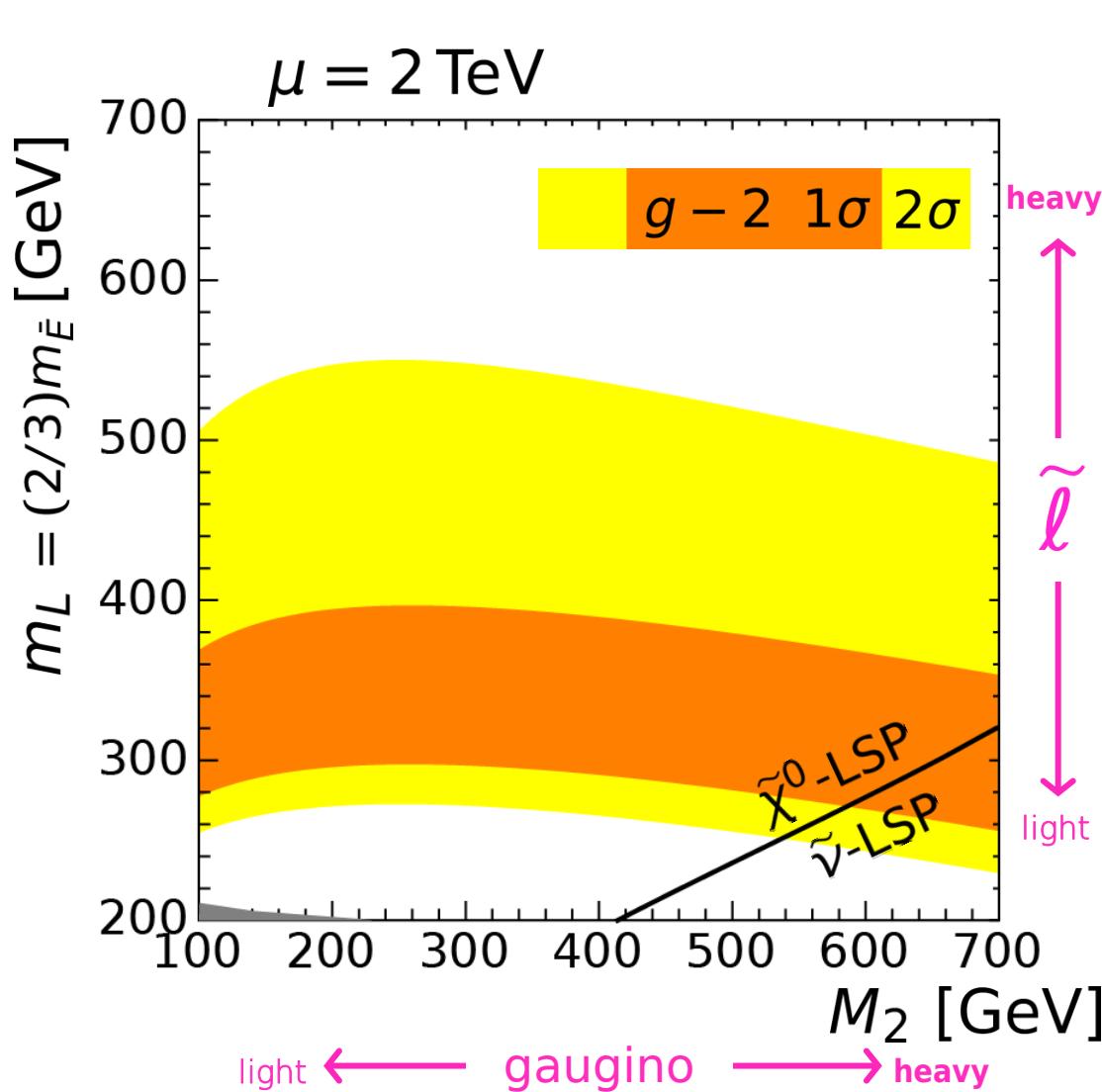
◎  $\tilde{h}$ -decoupled case  
 $(\mu = 2 \text{ TeV})$



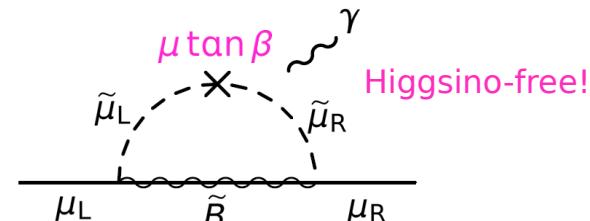
- Current Limit
- Future Prospects

## Result: $g-2$ v.s. LHC current status

An extreme case:  $\mu = 2 \text{ TeV}$ ,  $m_L^2 : m_{\tilde{E}}^2 = 1 : (1.5)^2$



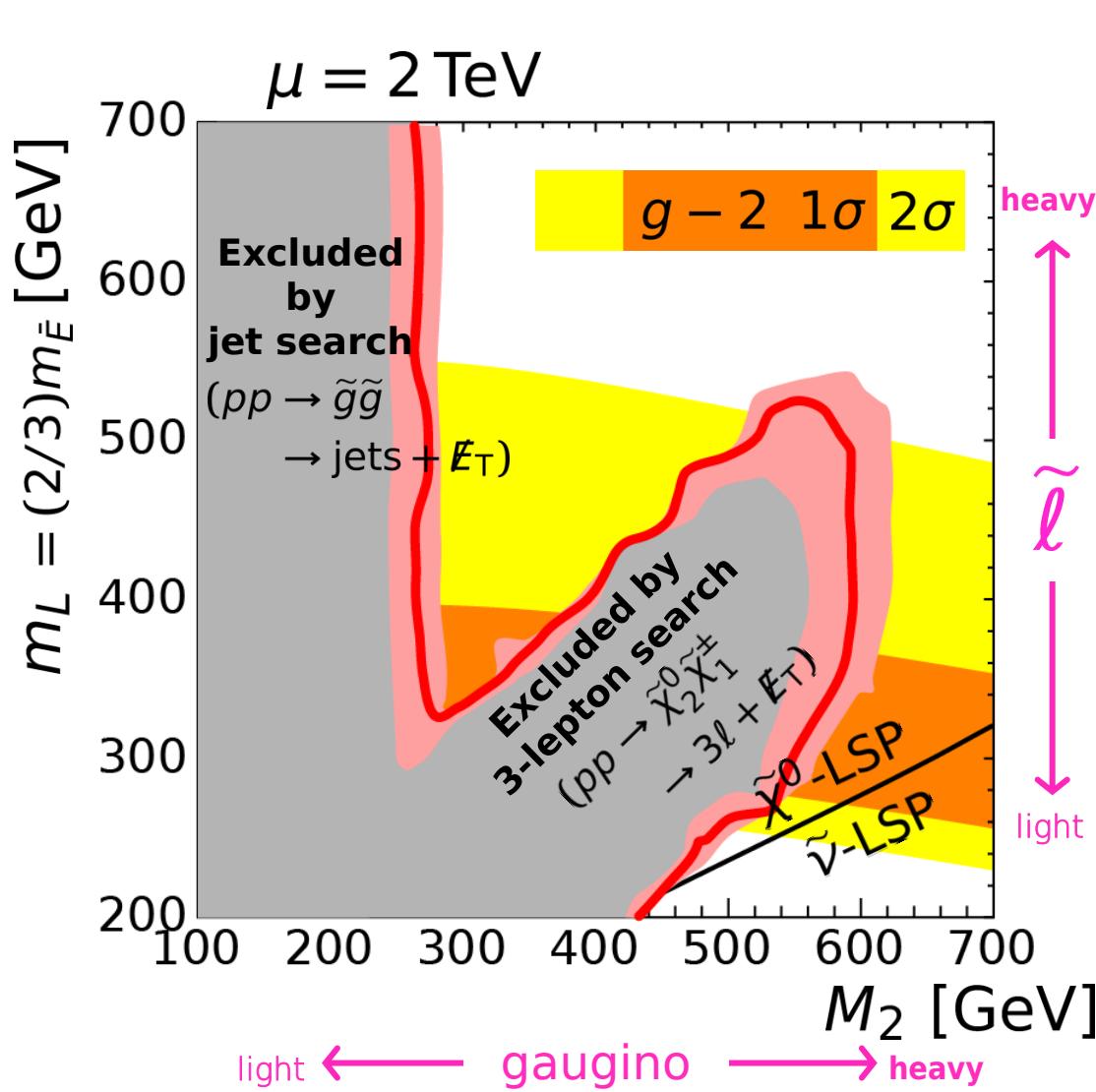
- $(g - 2)_\mu$  dominant source:



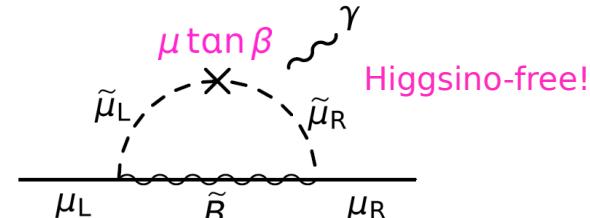
- Parameters:
  - $M_1 : M_2 : M_3 = 1 : 2 : 6$
  - $\mu = 2 \text{ TeV}$
  - $m_L^2 : m_{\tilde{E}}^2 = 1 : (1.5)^2$
  - $(\tan \beta, m_A) = (40, 1.5 \text{ TeV})$
- Soft-params set @ 7 TeV ( $= m_{\tilde{t}}$ ).
- $R$ -parity conserved.
- LSP is long-lived.
- squark/stau decoupled.
- slepton 1st-gen = 2nd-gen.
- $A$ -terms = 0.

## Result: $g-2$ v.s. LHC current status

An extreme case:  $\mu = 2 \text{ TeV}$ ,  $m_L^2 : m_{\tilde{E}}^2 = 1 : (1.5)^2$



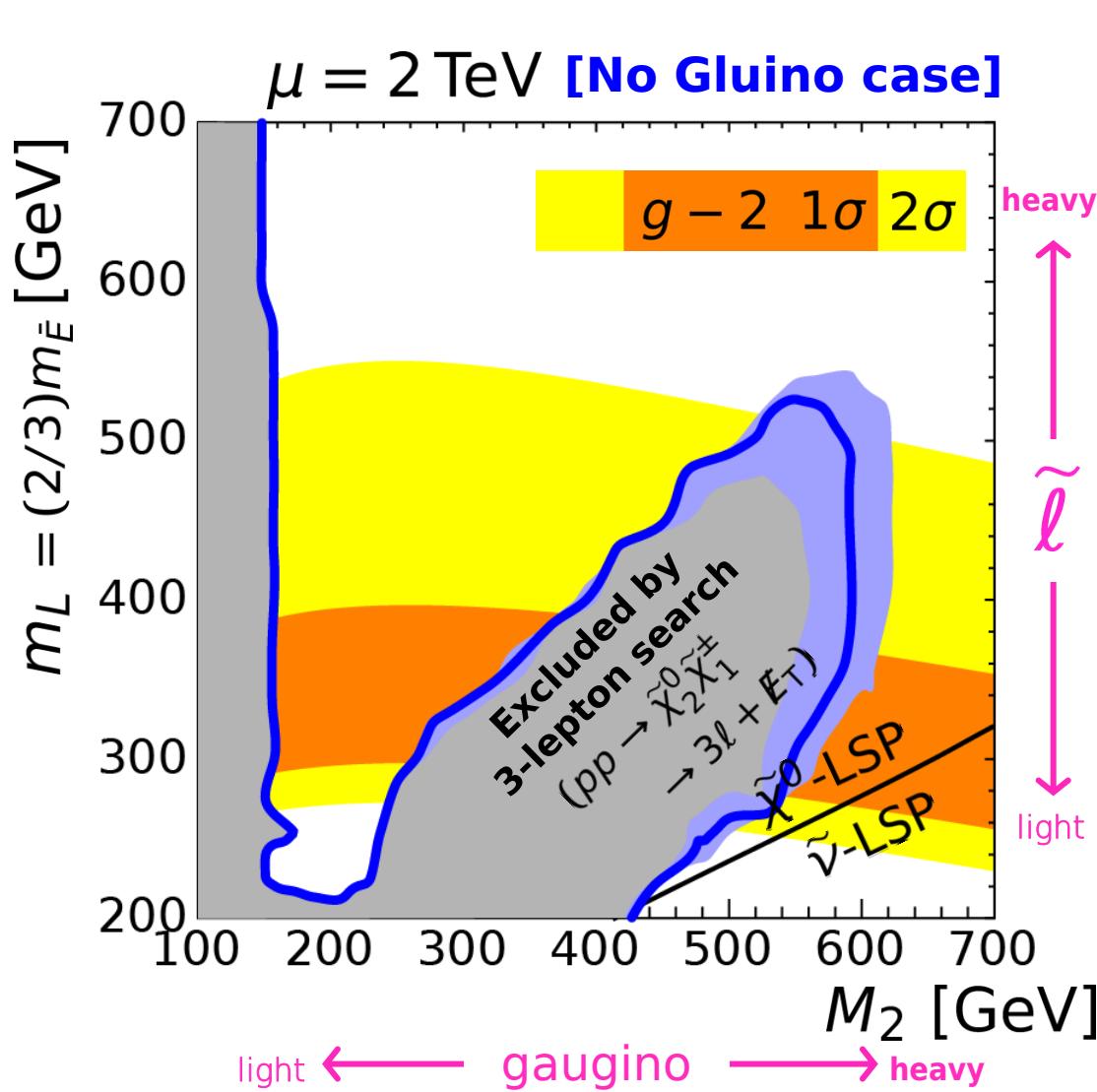
- $(g-2)_\mu$  dominant source:



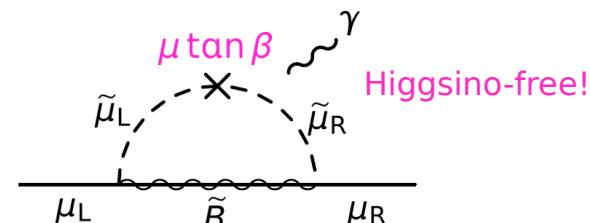
- Parameters:
  - $M_1 : M_2 : M_3 = 1 : 2 : 6$
  - $\mu = 2 \text{ TeV}$
  - $m_L^2 : m_{\tilde{E}}^2 = 1 : (1.5)^2$
  - $(\tan \beta, m_A) = (40, 1.5 \text{ TeV})$
- Soft-params set @ 7 TeV ( $= m_{\tilde{t}}$ ).
- R-parity conserved.
- LSP is long-lived.
- squark/stau decoupled.
- slepton 1st-gen = 2nd-gen.
- A-terms = 0.

## Result: $g-2$ v.s. LHC current status

An extreme case:  $\mu = 2 \text{ TeV}$ ,  $m_L^2 : m_{\tilde{E}}^2 = 1 : (1.5)^2$



- $(g - 2)_\mu$  dominant source:

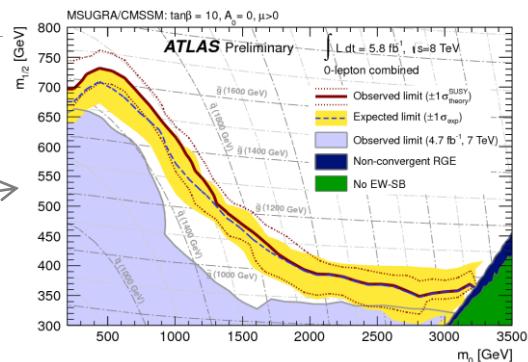


- Parameters:
  - $M_1 : M_2 : M_3 = 1 : 2 : 3$
  - $\mu = 2 \text{ TeV}$
  - $m_L^2 : m_{\tilde{E}}^2 = 1 : (1.5)^2$
  - $(\tan \beta, m_A) = (40, 1.5 \text{ TeV})$
- Soft-params set @ 7 TeV ( $= m_{\tilde{t}}$ ).
- $R$ -parity conserved.
- LSP is long-lived.
- squark/stau decoupled.
- slepton 1st-gen = 2nd-gen.
- $A$ -terms = 0.

## Details of Analyses

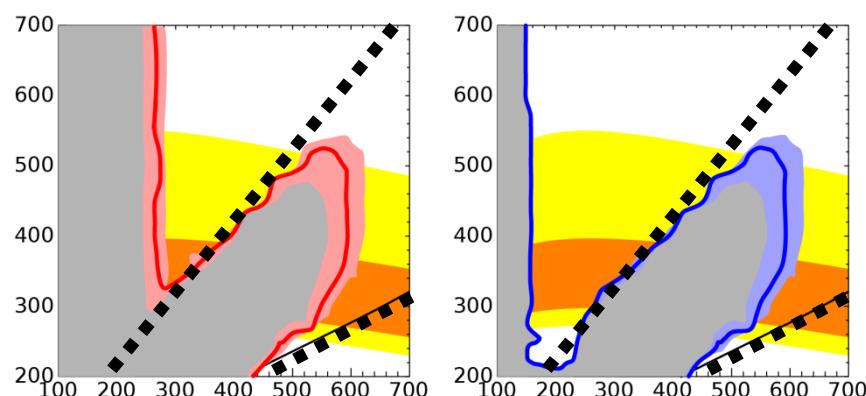
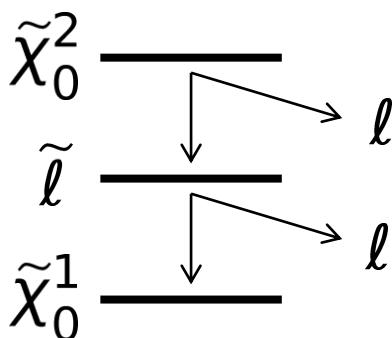
### ● jet search ( $pp \rightarrow \tilde{g}\tilde{g} \rightarrow \text{jets} + \cancel{E}_T$ )

- ATLAS 8TeV  $5.8\text{fb}^{-1}$  [[ATLAS-CONF-2012-109](#)]
- 2-6 hard jets + no lepton +  $\cancel{E}_T$
- Original bound :  $\tilde{g} \gtrsim 950\text{ GeV}$  (CMSSM,  $\tilde{q} \gg \tilde{g}$ )
 
$$\implies M_2 \gtrsim 300\text{ GeV} \text{ in our model}$$



### ● 3-lepton search ( $pp \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^\pm \rightarrow 3\ell + \cancel{E}_T$ )

- ATLAS 8TeV  $13\text{fb}^{-1}$  [[ATLAS-CONF-2012-154 \(obsolete\)](#)]
- Exact 3 leptons +  $\cancel{E}_T$  + vetoing SM-like signal  
(no  $b$ -jets, no lepton pairs near  $M_Z$ , etc...)
- Degenerated regions  
are not excluded.  
(near the dotted lines)



**Rest Params:**  $(m_L^2, m_{\tilde{E}}^2)$  : slepton soft-masses  
 $(M_2, \mu)$  : gaugino/Higgsino mass

### **Two extreme cases**

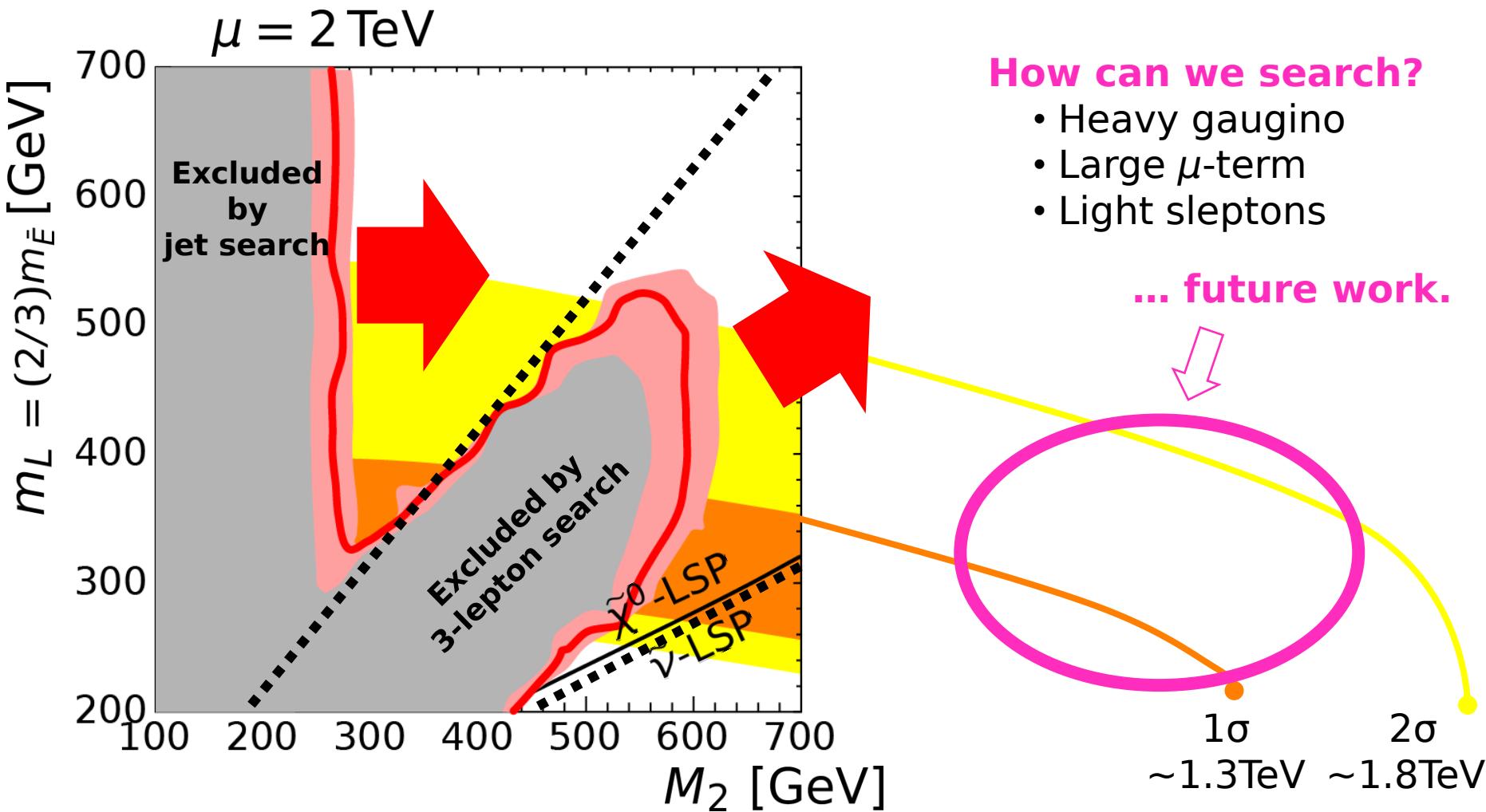
◎  $\tilde{\mu}_R$ -decoupled case  
 $(m_{\tilde{E}}^2 = (3 \text{ TeV})^2)$

◎  $\tilde{h}$ -decoupled case  
 $(\mu = 2 \text{ TeV})$



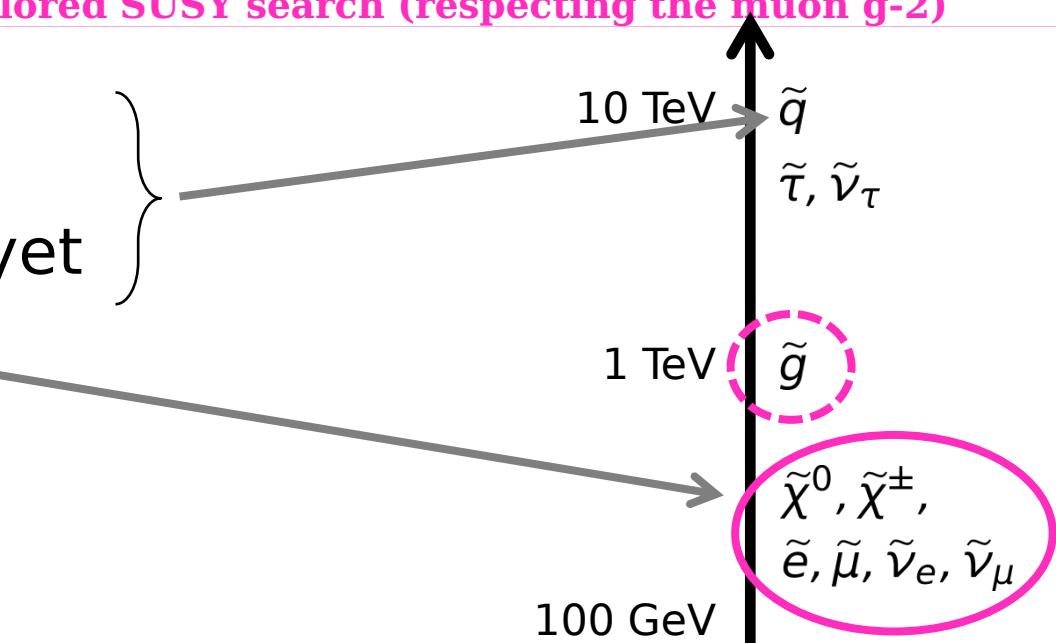
- Current Limit
- Future Prospects

An extreme case:  $\mu = 2 \text{ TeV}$ ,  $m_L^2 : m_{\tilde{E}}^2 = 1 : (1.5)^2$



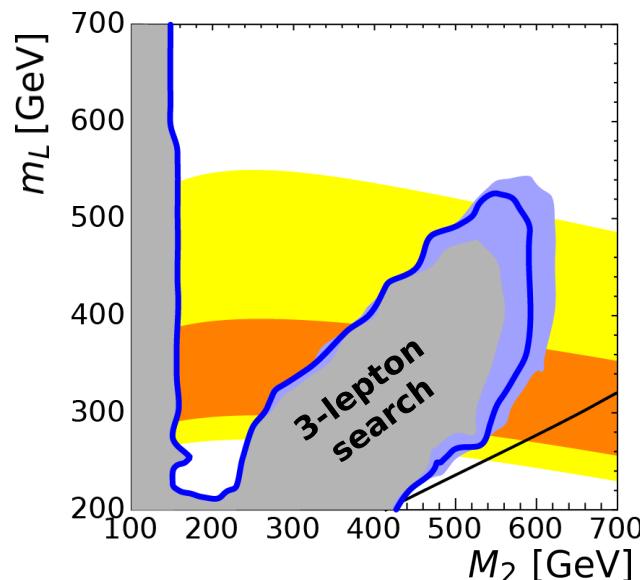
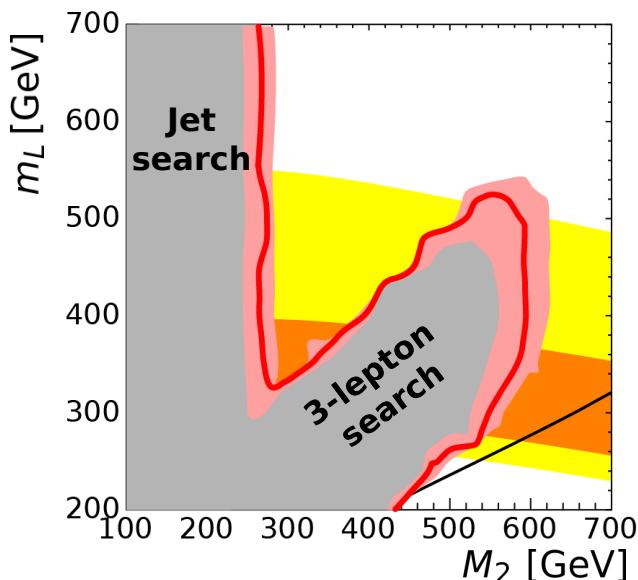
## Summary of Topic 1 : Non-colored SUSY search (respecting the muon g-2)

- 126 GeV Higgs
- SUSY Not Found yet
- $(g - 2)_\mu$  anomaly



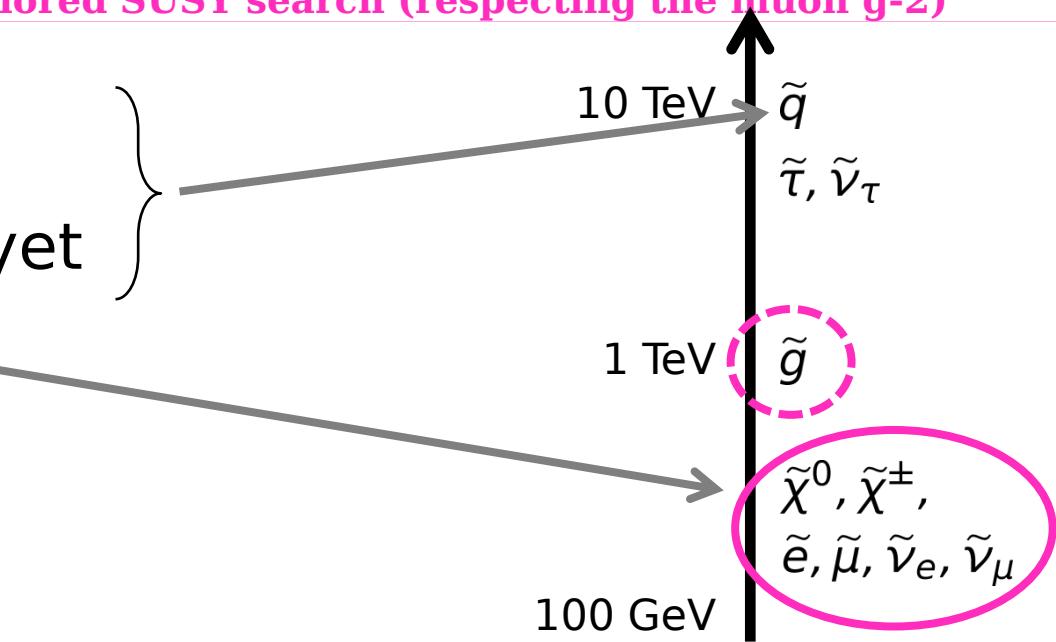
An extreme case:  $\mu = 2 \text{ TeV}$ ,  $m_L^2 : m_E^2 = 1 : (1.5)^2$

Jet: [ATLAS-CONF-2012-109](#)  
3L: [ATLAS-CONF-2012-154](#)



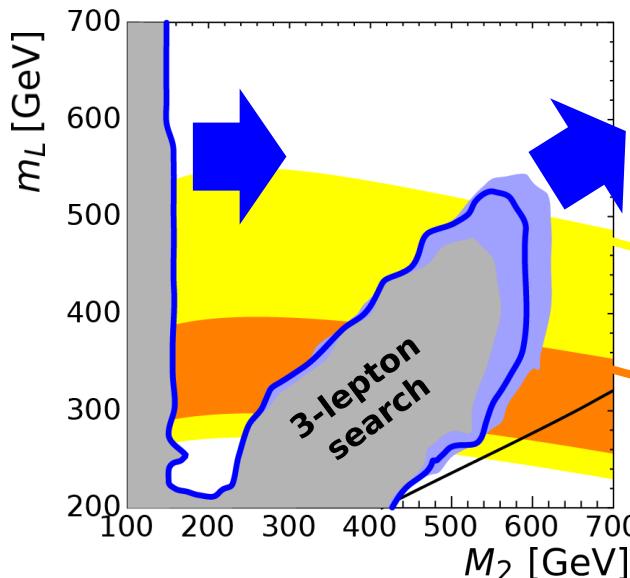
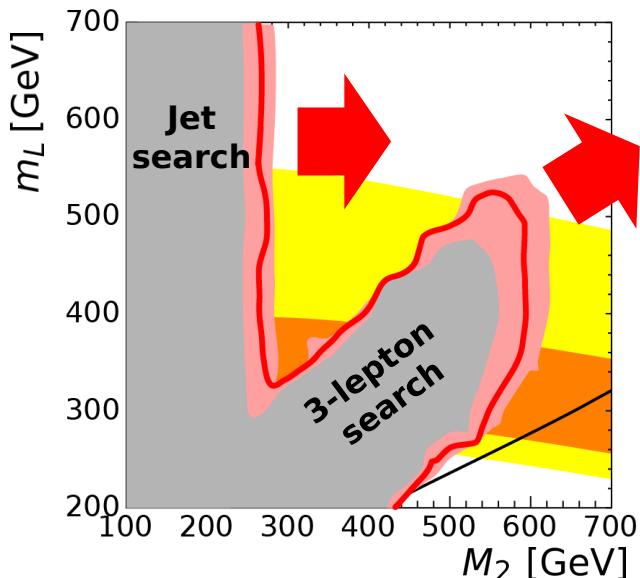
## Summary of Topic 1 : Non-colored SUSY search (respecting the muon g-2)

- 126 GeV Higgs
- SUSY Not Found yet
- $(g - 2)_\mu$  anomaly



An extreme case:  $\mu = 2 \text{ TeV}$ ,  $m_L^2 : m_E^2 = 1 : (1.5)^2$

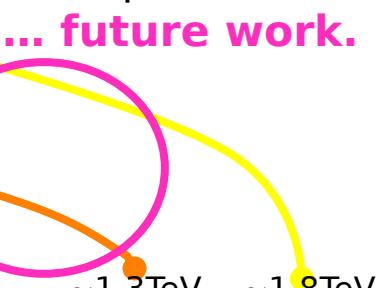
Jet: [ATLAS-CONF-2012-109](#)  
3L: [ATLAS-CONF-2012-154](#)



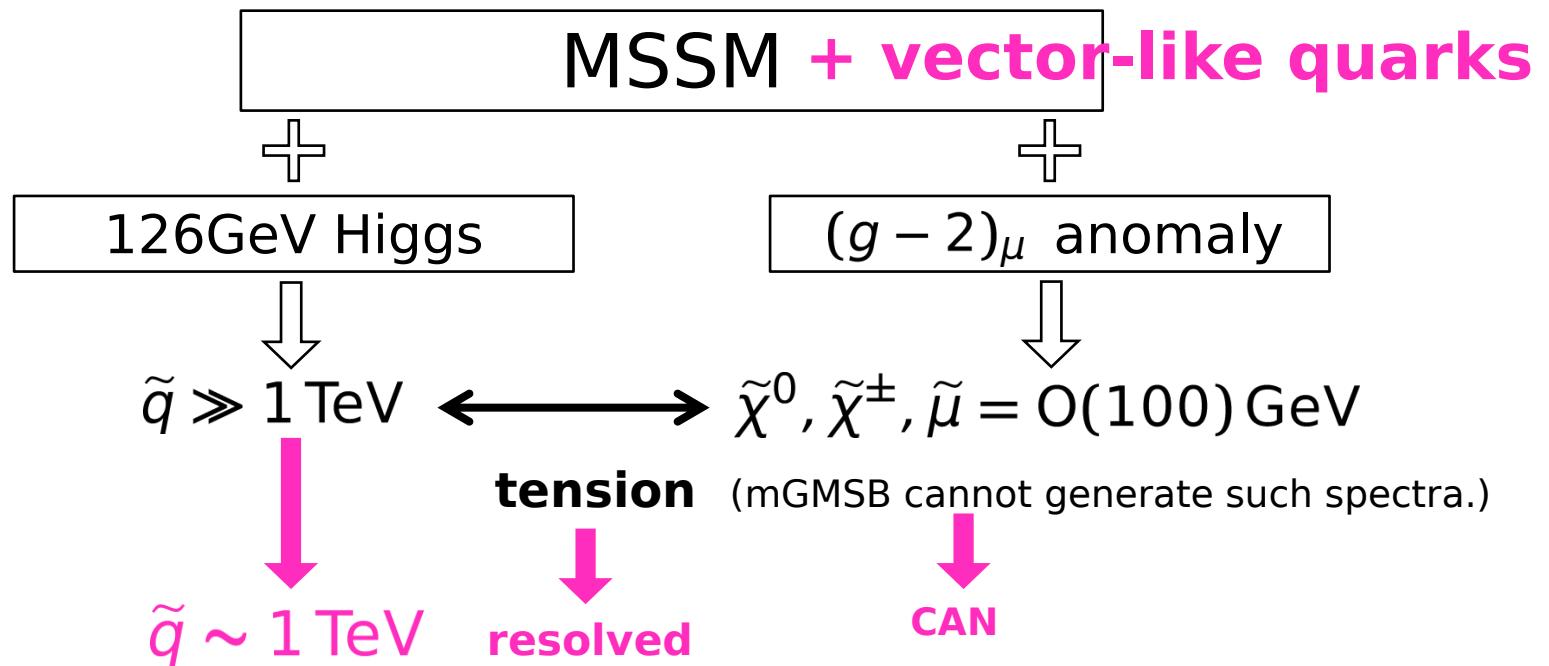
**How can we search?**

- Heavy gaugino
- Large  $\mu$ -term
- Light sleptons

**... future work.**

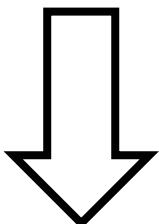


# Topic 2 : V-GMSB



**MSSM + GMSB (or mSUGRA)**

$\implies (g - 2)_\mu \text{ with } m_{\tilde{\chi}^\pm} = 126 \text{ GeV}$



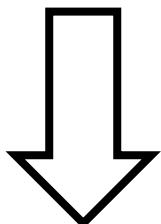
**MSSM + more complicated SUSY**

**or**

**Extended model + GMSB/mSUGRA**

**MSSM + GMSB (or mSUGRA)**

$\implies (g - 2)_\mu \text{ with } m_{\tilde{\chi}^0} = 126 \text{ GeV}$



**MSSM + more complicated SUSY**

**or**

**V-MSSM**

**+ GMSB/mSUGRA**

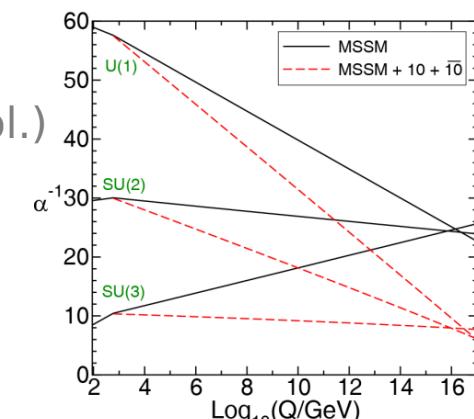
- V-MSSM = MSSM +  $(\mathbf{10} + \overline{\mathbf{10}})$ , i.e.  $\begin{cases} \mathbf{10} = (Q', \bar{U}', \bar{E}') \\ \overline{\mathbf{10}} = (\bar{Q}', U', E') \end{cases}$   
extra Vector-like matters

$$W_{\text{extra}} = Y' Q' H_u \bar{U}' + Y'' \bar{Q}' H_d U' \quad (\text{cf. } W_{\text{MSSM}} \ni Y_t Q H_u \bar{U})$$

$$+ M_V Q' \bar{Q}' + M_V U' \bar{U}' + M_V E' \bar{E}'$$

$$W_{\text{mix}} = \epsilon_i Q_i H_u U' + \epsilon'_i Q' H_u \bar{U}_i + \epsilon''_i Q' H_d \bar{D}_i + \epsilon^L_i L_i H_d \bar{E}'$$

- Vector-like  $\Rightarrow$  No gauge anomaly.
- Mixings : necessary (to avoid stable particles)  
but must be tiny. (to avoid large flav-viol.)
- $Y'$  : IR fixed to  $\sim 1.05 \Rightarrow m_h$  well increased.
- $Y''$  : reduces  $m_h \Rightarrow$  assumed small.



Martin [0910.2732]

# RESULT

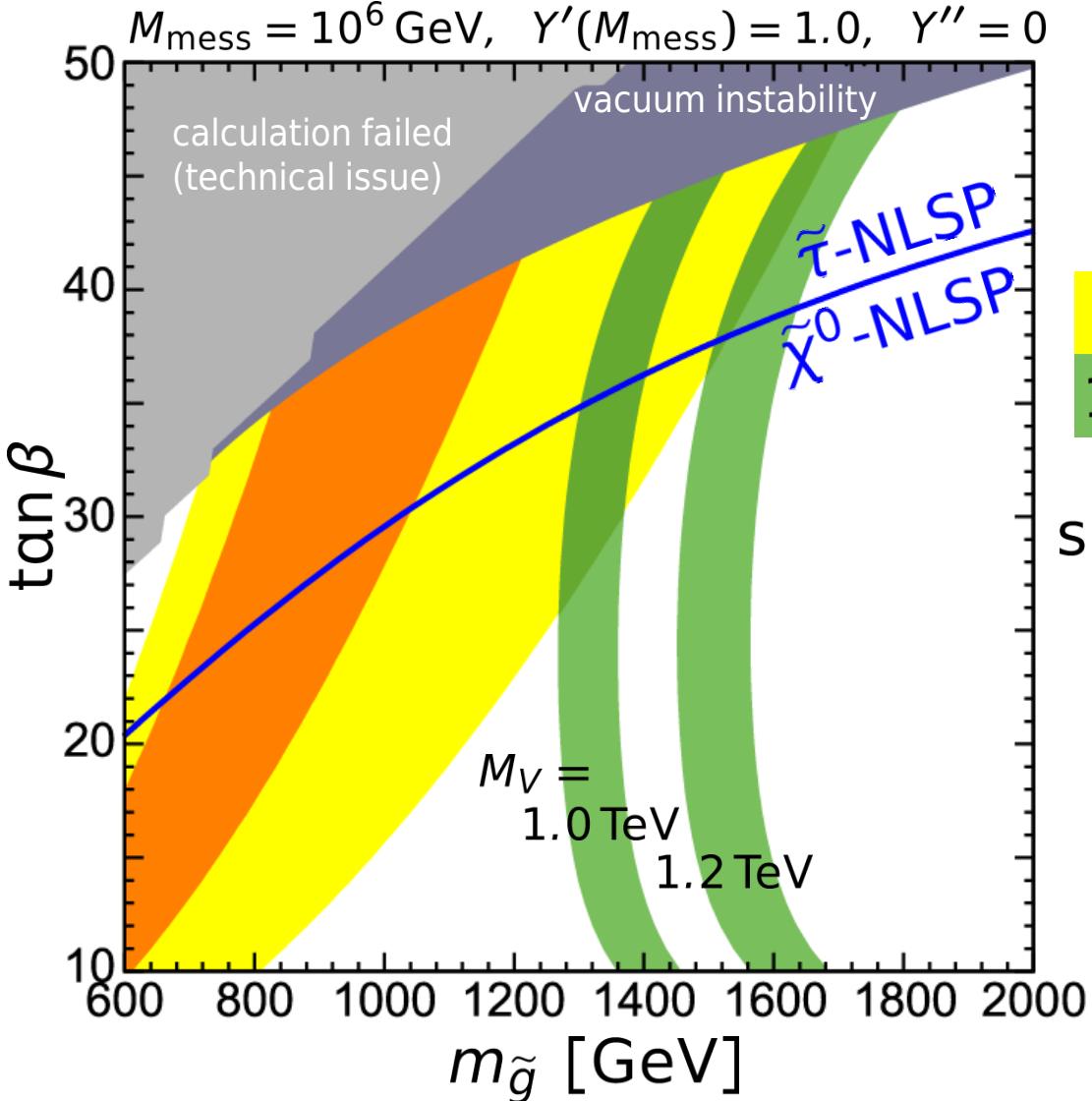
in this talk

with {

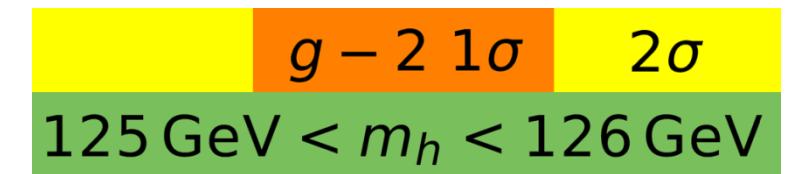
- GMSB framework
- mSUGRA framework  
→ See [[1112.5653](#)]

# VMSSM + GMSB explains muon g-2 anomaly under 126GeV Higgs

params: ( $\Lambda$ ,  $M_{\text{mess}}$ ,  $\tan \beta$ ,  $N_{\text{mess}}$ ,  $\text{sgn} \mu$ ;  $Y'$ ,  $M_V$ )



$$\begin{array}{c|c|c} \parallel & \parallel & \parallel \\ 1 & + & 1.0 \\ \hline \Delta(g-2) > 0 & (\text{IR fixed}) & \end{array}$$



simultaneous realization:

$$M_V \lesssim 1.2 \text{ TeV},$$

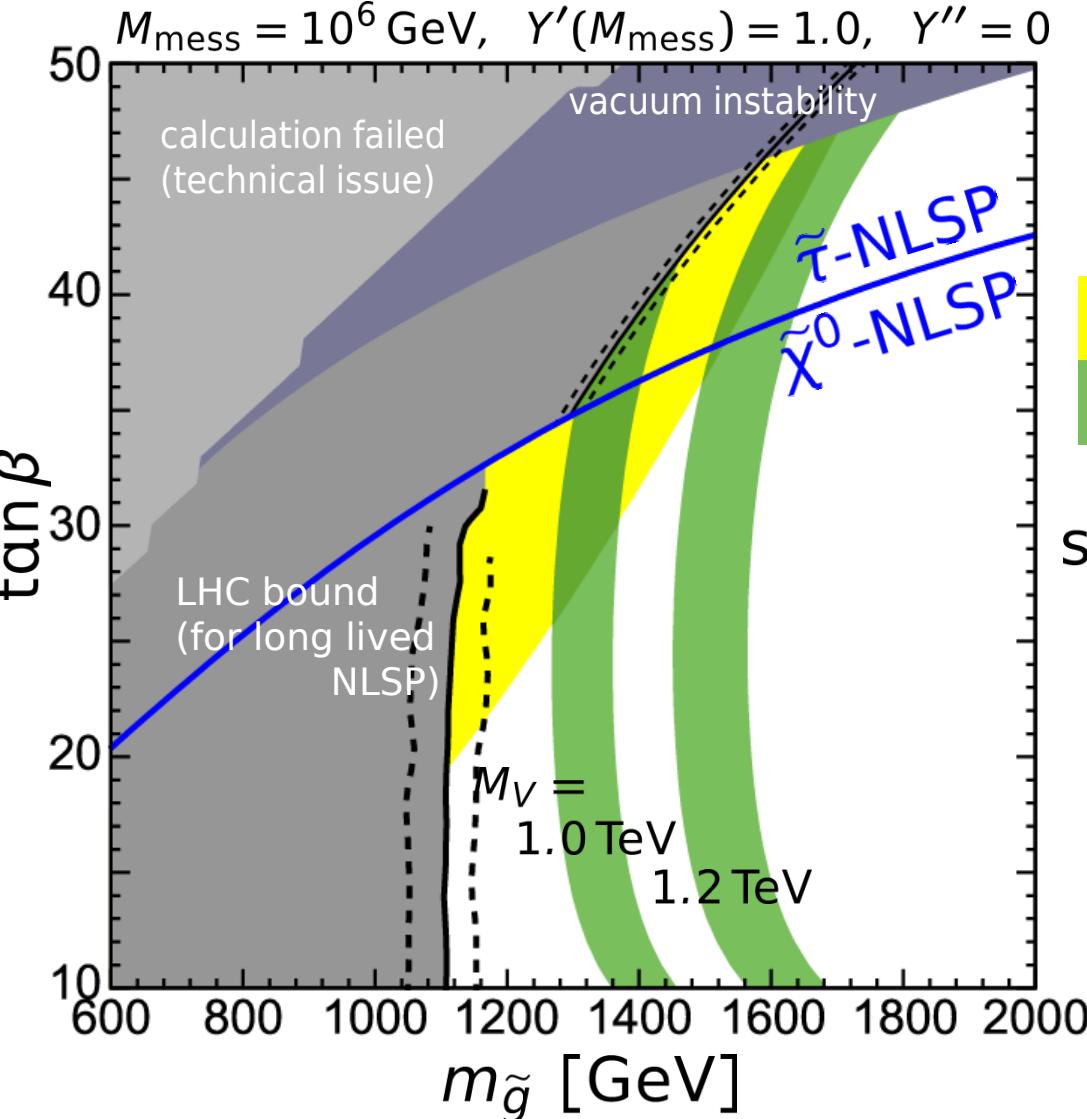
$$m_{\tilde{g}} \lesssim 1.6 \text{ TeV},$$

$$\tan \beta \sim \mathcal{O}(10)$$

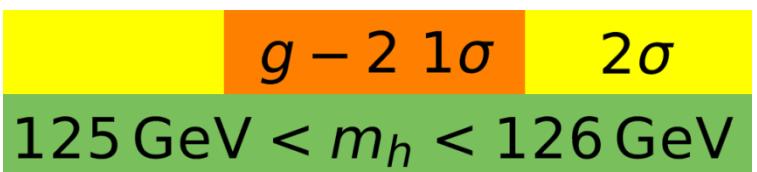
→ **LHC LIMIT!?**

# VMSSM + GMSB explains muon g-2 anomaly under 126GeV Higgs

params: ( $\Lambda$ ,  $M_{\text{mess}}$ ,  $\tan \beta$ ,  $N_{\text{mess}}$ ,  $\text{sgn} \mu$ ;  $Y'$ ,  $M_V$ )



||  
1  
+  
||  
 $\Delta(g-2) > 0$  (IR fixed)  
1.0



simultaneous realization:

$M_V \lesssim 1.2 \text{ TeV}$ ,  
 $m_{\tilde{g}} \lesssim 1.6 \text{ TeV}$ ,  
 $\tan \beta \sim \mathcal{O}(10)$

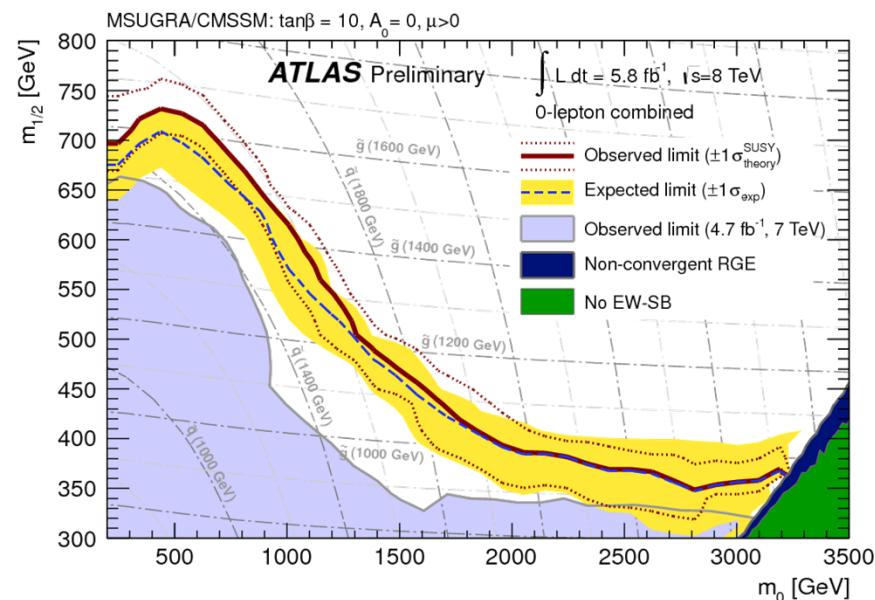
→ **LHC LIMIT!?**

NLSP	Long-lived NLSP	NLSP prompt decay
$\tilde{\chi}_1^0$	jet + $E_T$ ( $\tilde{\chi}_1^0 \tilde{\chi}_1^0$ ) (same as mSUGRA)	jet + $E_T$ and $2\gamma + E_T$ (from $\tilde{\chi}_1^0 \rightarrow \gamma \tilde{G}$ )
$\tilde{\tau}_1$	Long-lived stau	multi-tau

## Our analysis

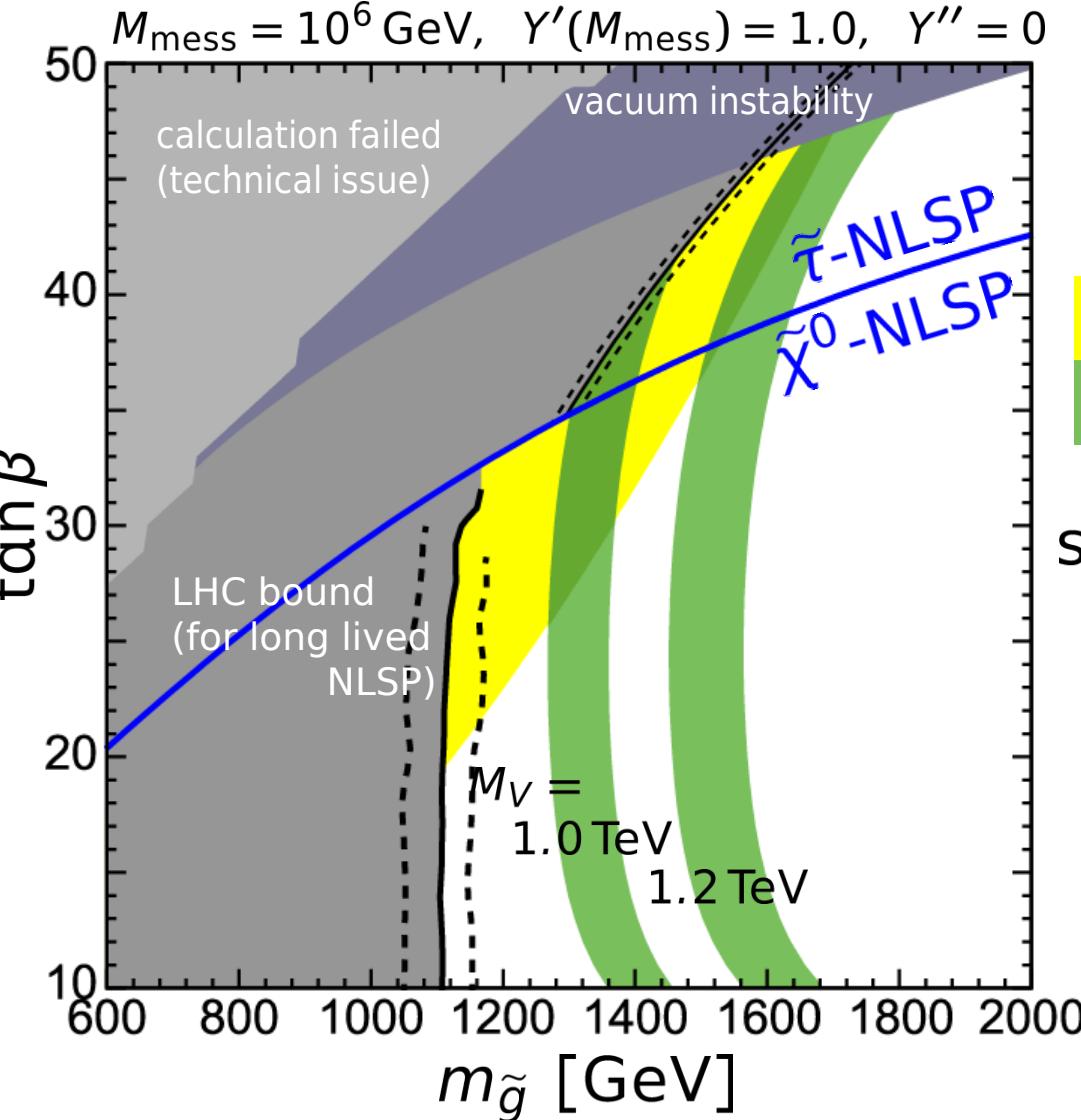
- Neutralino NLSP  
→ ATLAS 8 TeV- $5.8 \text{ fb}^{-1}$   
(2–6 jets +  $E_T$ )  
[ATL-C0NF-2012-109]

- Stau NLSP  
→ CMS 7 TeV- $5.0 \text{ fb}^{-1}$   
(assuming  $pp \rightarrow \tilde{\tau}_1 \tilde{\tau}_1^*$ )  
 $\rightsquigarrow m_{\tilde{\tau}_1} > 223 \text{ GeV}$  [1205.0272]

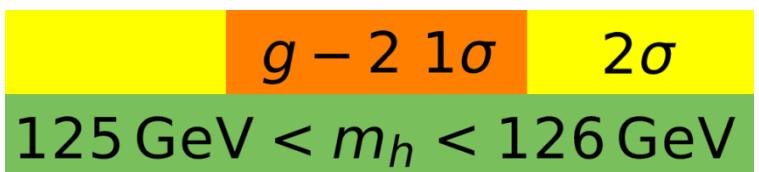


# VMSSM + GMSB explains muon g-2 anomaly under 126GeV Higgs

params: ( $\Lambda$ ,  $M_{\text{mess}}$ ,  $\tan \beta$ ,  $N_{\text{mess}}$ ,  $\text{sgn} \mu$ ;  $Y'$ ,  $M_V$ )



||  
1  
+  
||  
 $\Delta(g-2) > 0$  (IR fixed)  
1.0



simultaneous realization:

$M_V \lesssim 1.2 \text{ TeV}$ ,  
 $m_{\tilde{g}} \lesssim 1.6 \text{ TeV}$ ,  
 $\tan \beta \sim \mathcal{O}(10)$

# Appendix

LHC-constraints from  
extra-quark search.

MSSM+ $(\mathbf{10} + \overline{\mathbf{10}})$ , i.e.  $\begin{cases} \mathbf{10} = (Q', \bar{U}', \bar{E}') \\ \overline{\mathbf{10}} = (\bar{Q}', U', E') \end{cases}$

## Extra particles in the V-MSSM

- $(Q', \bar{U}', \bar{E}') + (\bar{Q}', U', E') \rightarrow (\tilde{t}'_{1,2,3,4}, \tilde{b}'_{1,2}, \tilde{\tau}'_{1,2})$

➤ Mass

$$m_{t'} \sim M_V \pm (174 \text{ GeV}/2),$$

$$m_{b'} = m_{\tau'} = M_V$$

&  $(t'_1, t'_2, b', \tau')$

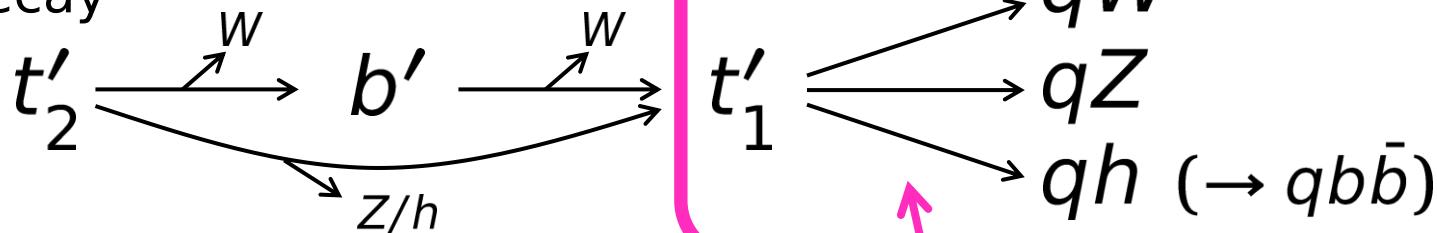
$$W_{\text{extra}} = Y' Q' H_u \bar{U}' + M_V Q' \bar{Q}' + M_V U' \bar{U}' + M_V E' \bar{E}'$$

$$W_{\text{mix}} = \epsilon_i Q_i H_u U' + \epsilon'_i Q' H_u \bar{U}_i + \epsilon''_i Q' H_d \bar{D}_i + \epsilon^L_i L_i H_d \bar{E}'$$

➤ Production

$$pp \rightarrow t'_1 \bar{t}'_1 \text{ etc. (pair production)}$$

➤ Decay

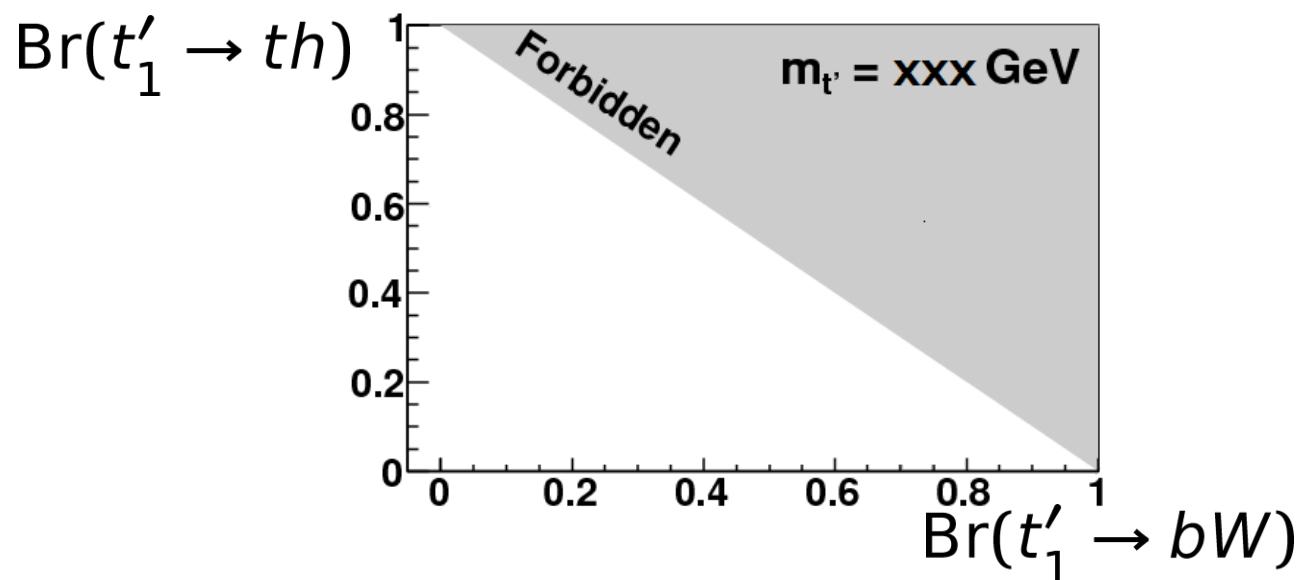
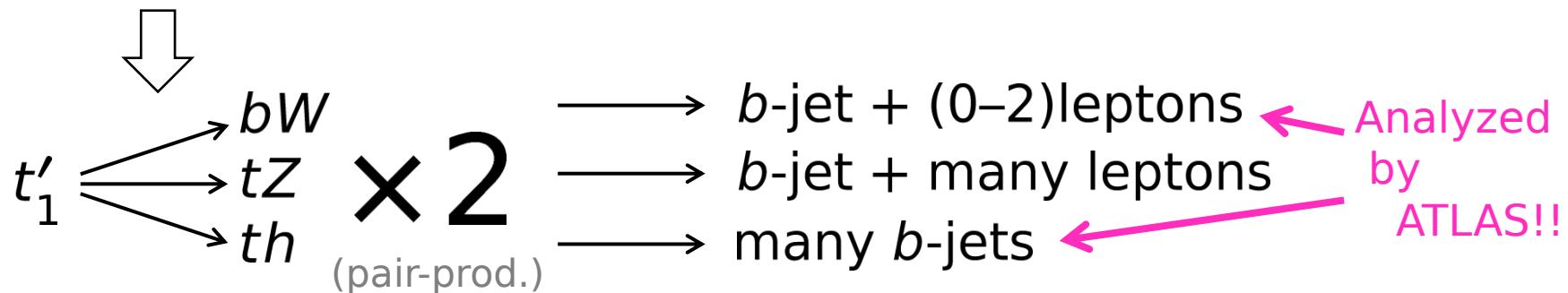


**depending on mixing**  
btw. vec-like/SM quarks.

## Extra particles in the V-MSSM

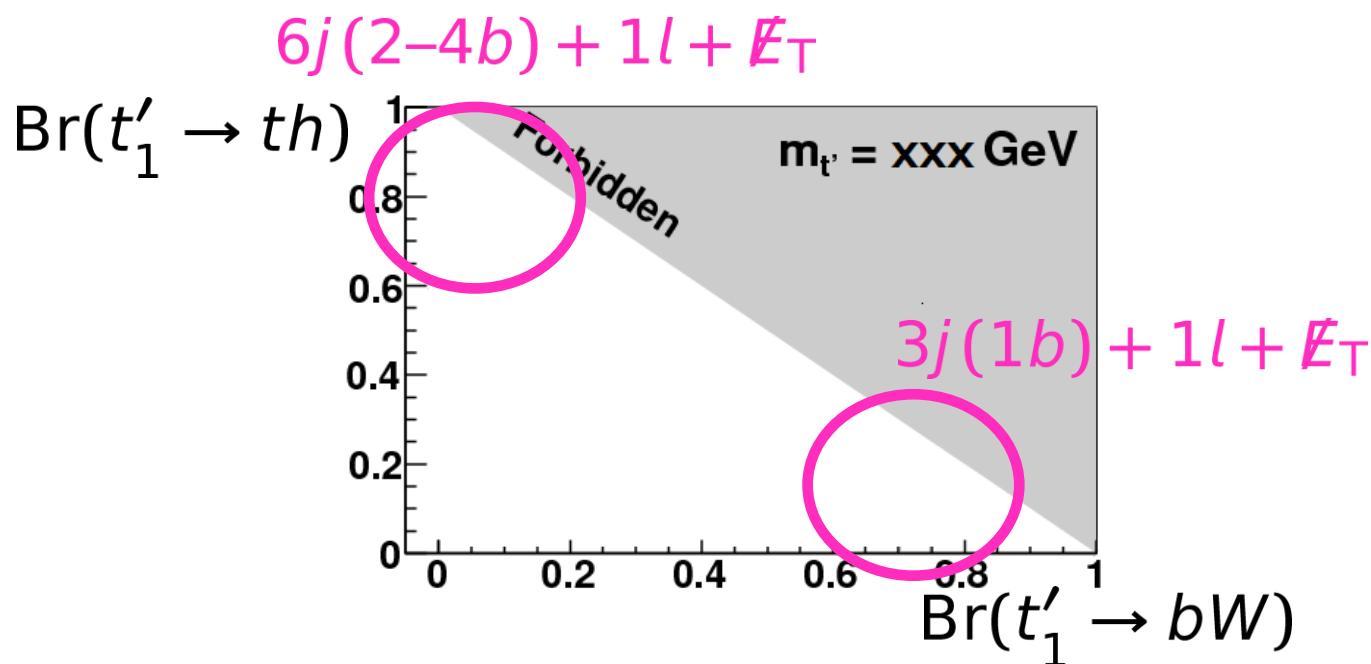
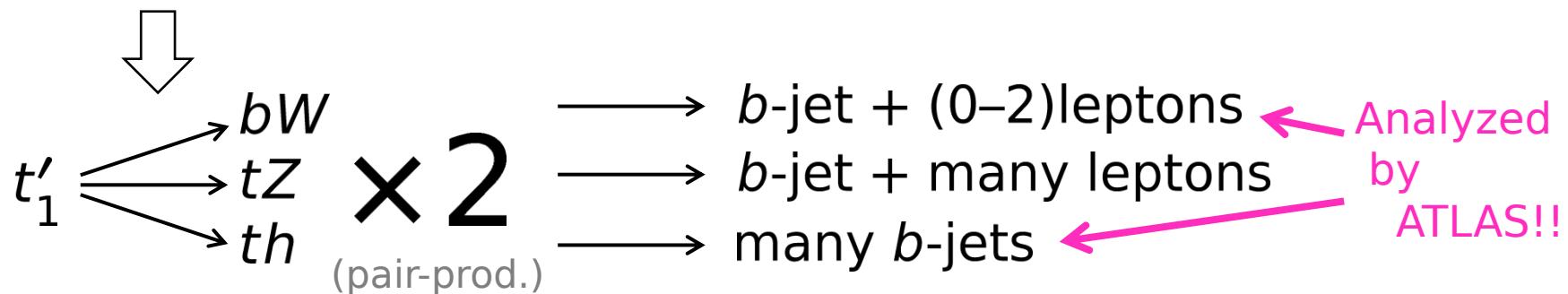
$$W_{\text{mix}} = \epsilon_i Q_i H_u U' + \epsilon'_i Q' H_u \bar{U}_i + \epsilon''_i Q' H_d \bar{D}_i + \epsilon^L_i L_i H_d \bar{E}'$$

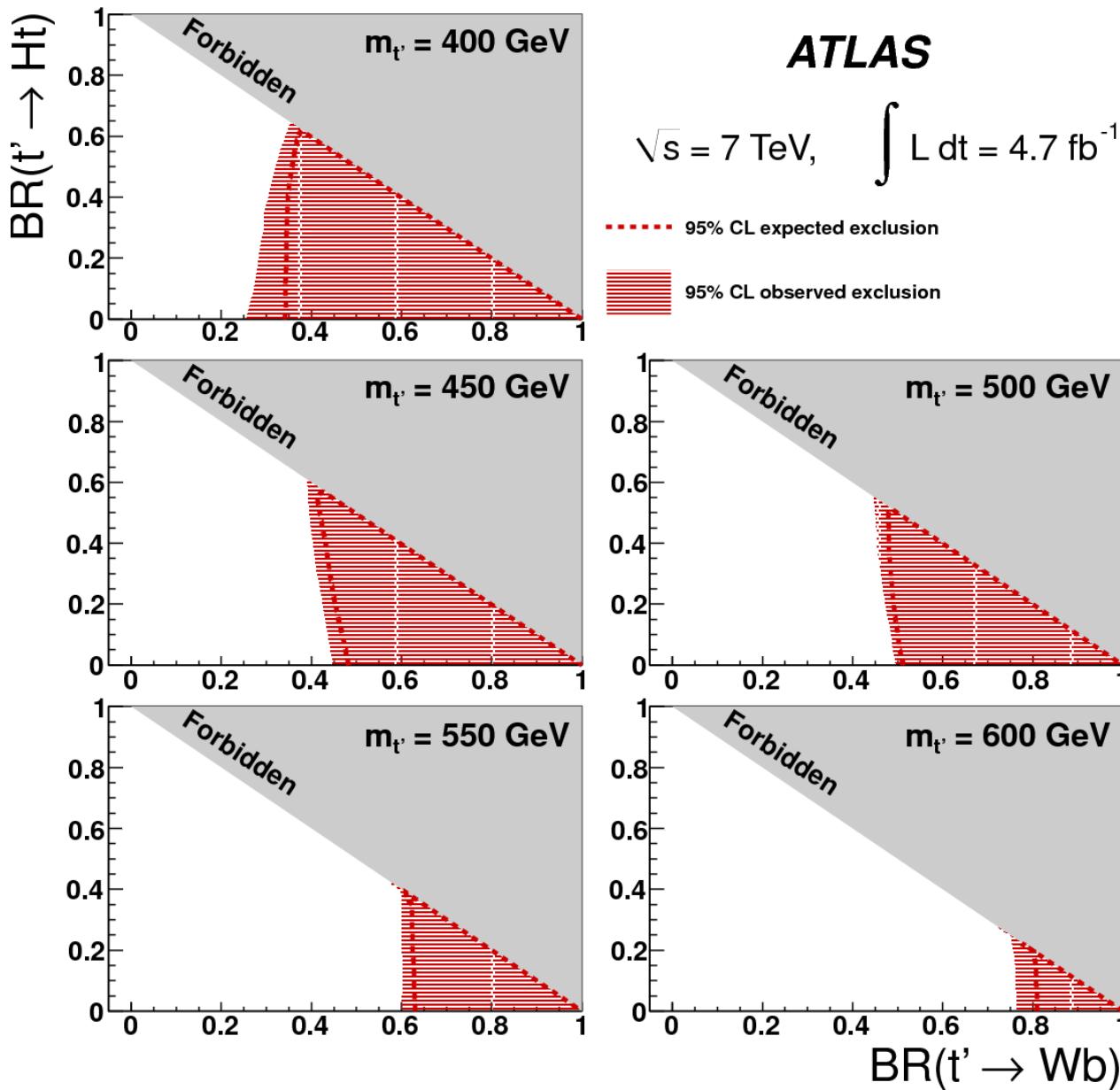
- Assumption: mixing with **3-gen.** only. ( $\epsilon_1 = \epsilon_2 = 0$ ) etc.

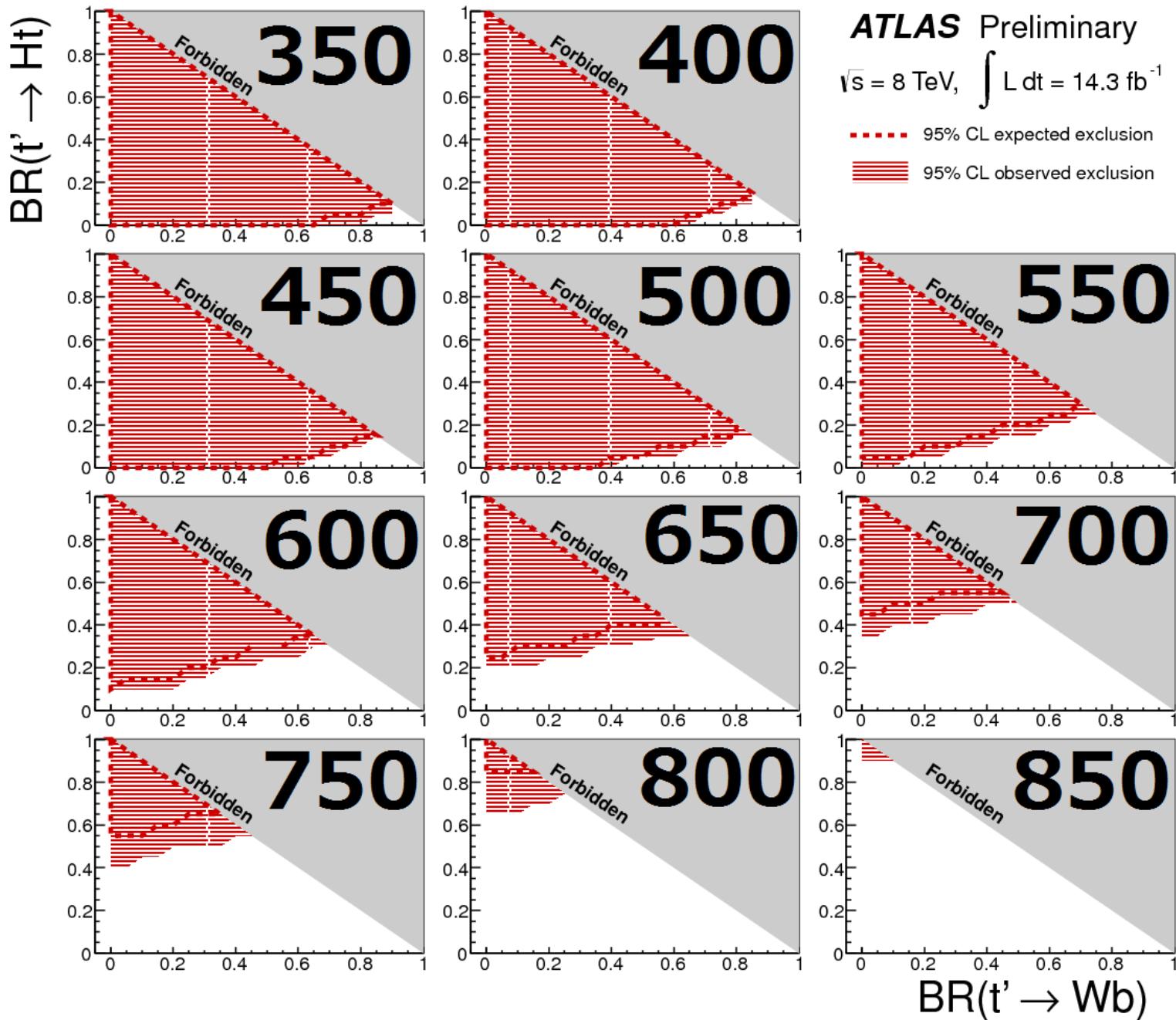


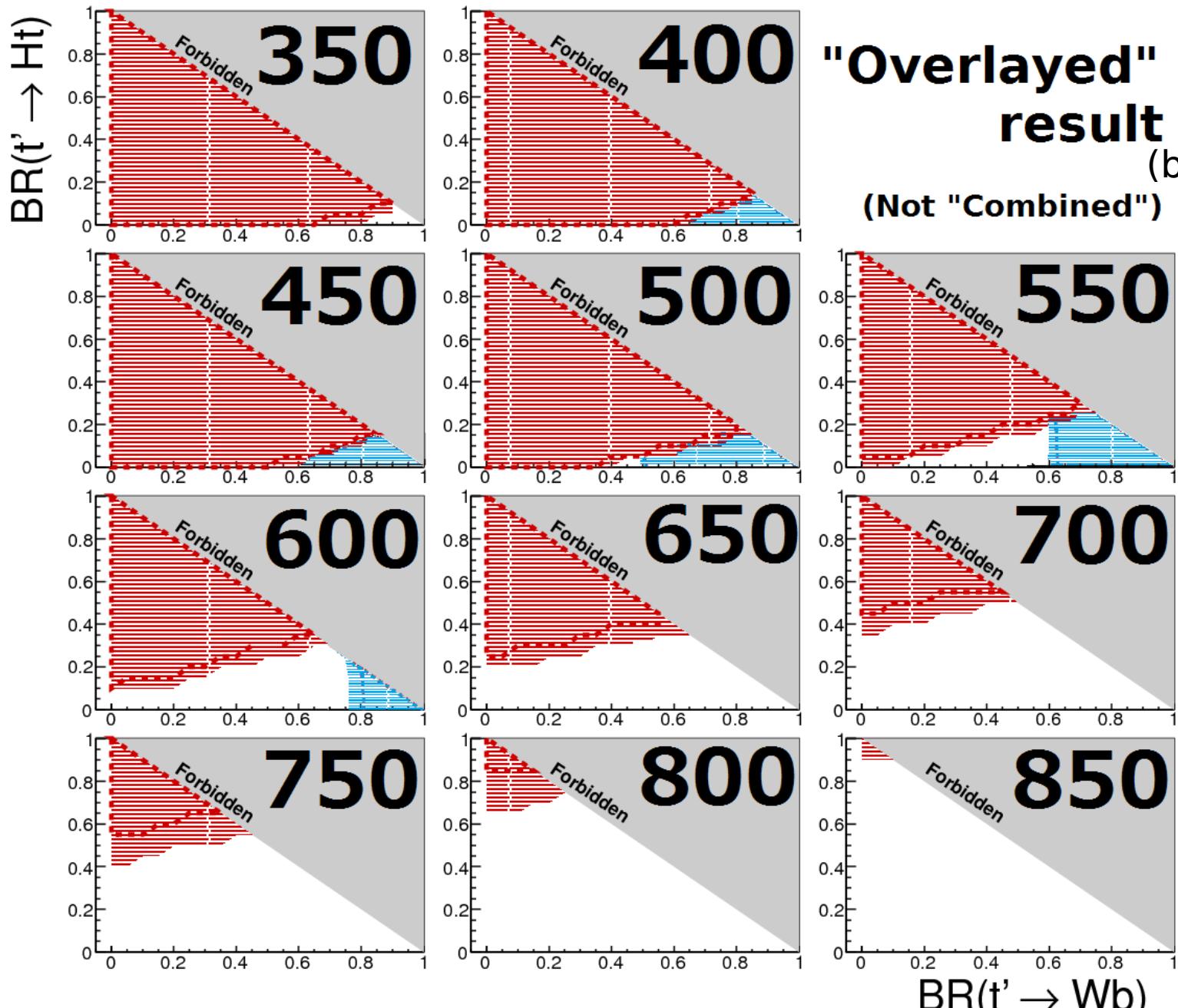
$$W_{\text{mix}} = \epsilon_i Q_i H_u U' + \epsilon'_i Q' H_u \bar{U}_i + \epsilon''_i Q' H_d \bar{D}_i + \epsilon^L_i L_i H_d \bar{E}'$$

- Assumption: mixing with **3-gen.** only. ( $\epsilon_1 = \epsilon_2 = 0$ ) etc.

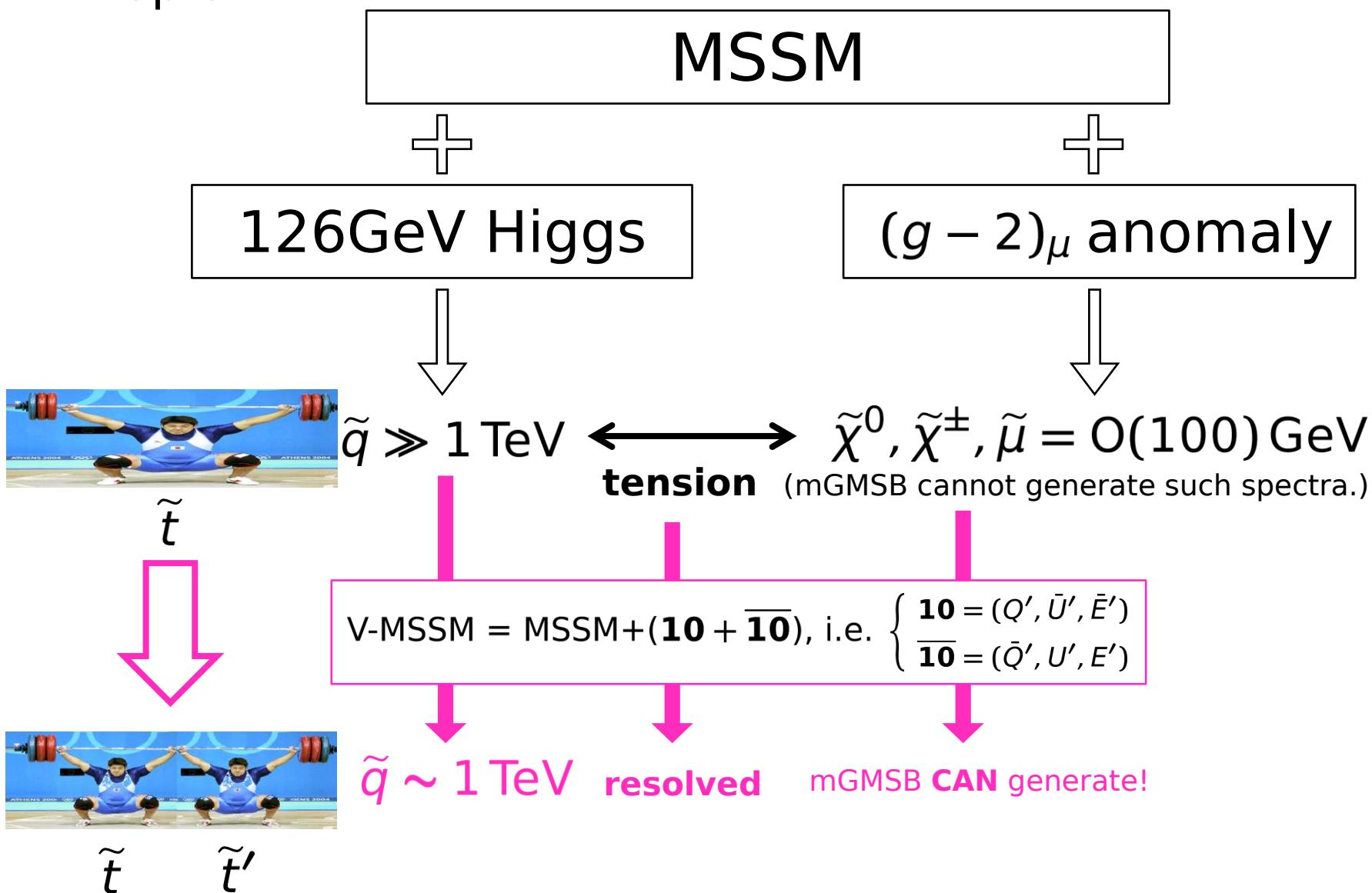


**ATLAS** $\sqrt{s} = 7 \text{ TeV}, \int L dt = 4.7 \text{ fb}^{-1}$

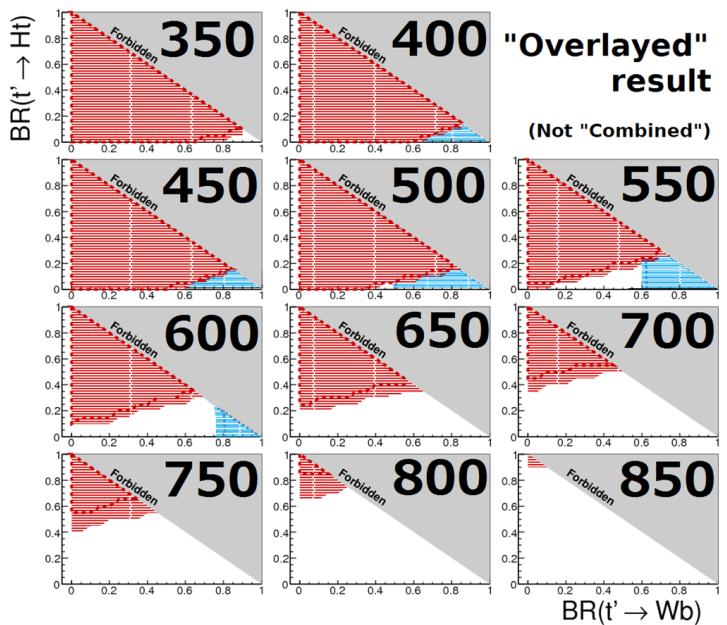
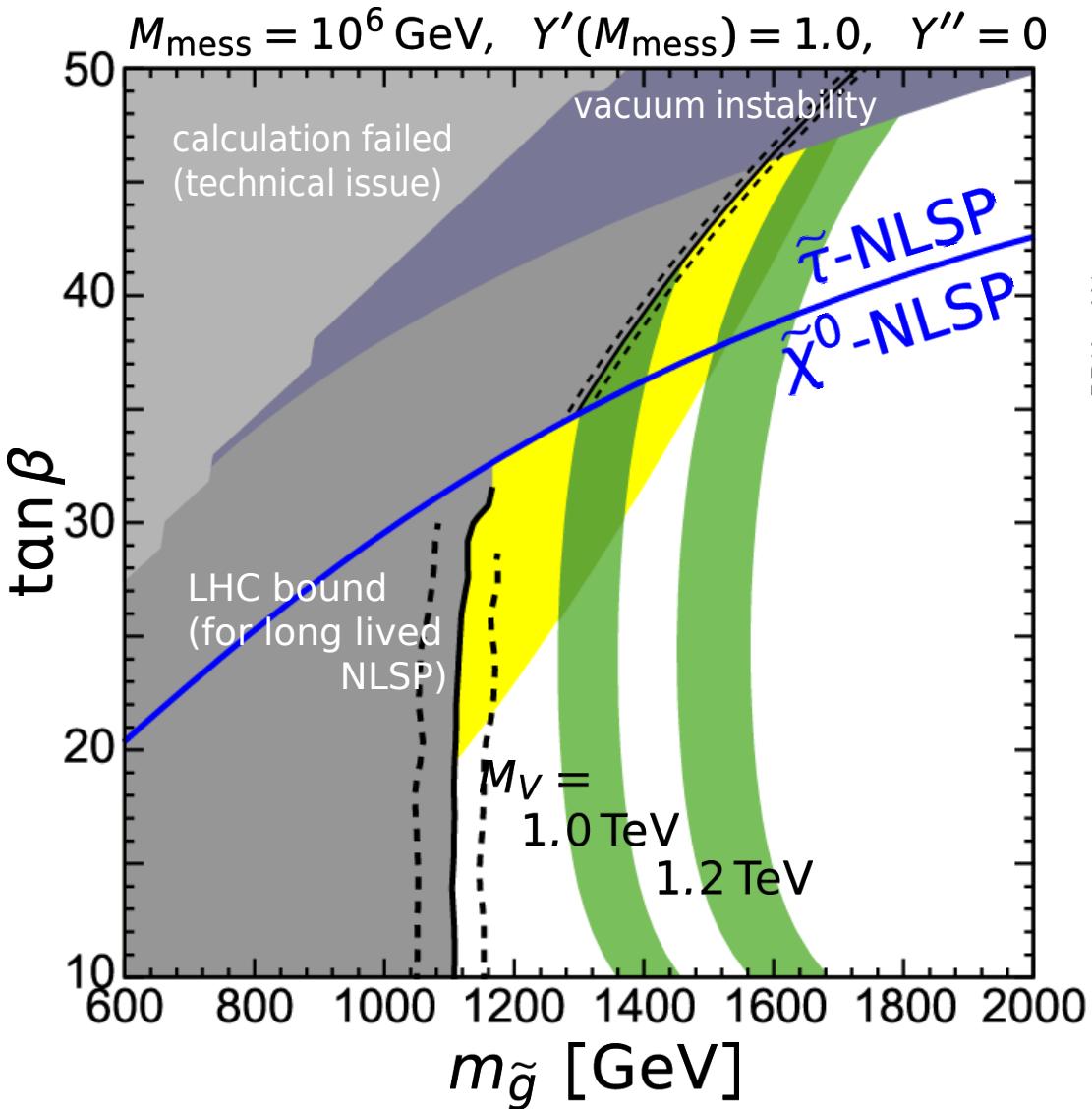
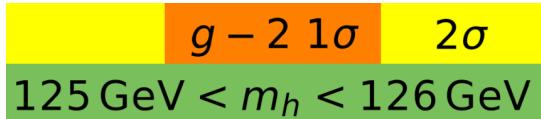




## ○ Topic 2.



# VMSSM + GMSB explains muon g-2 anomaly under 126GeV Higgs

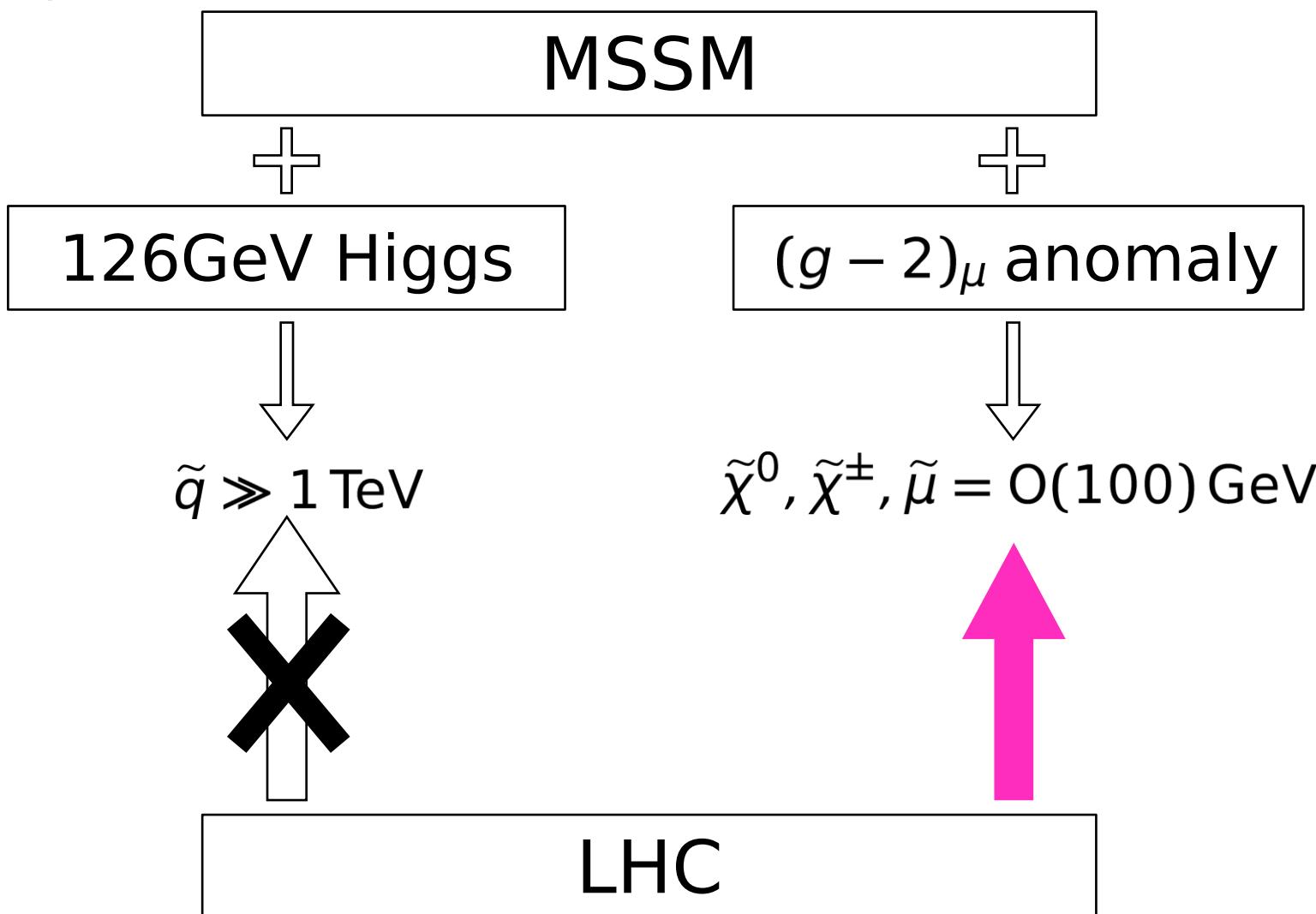


# **Summary?**

---

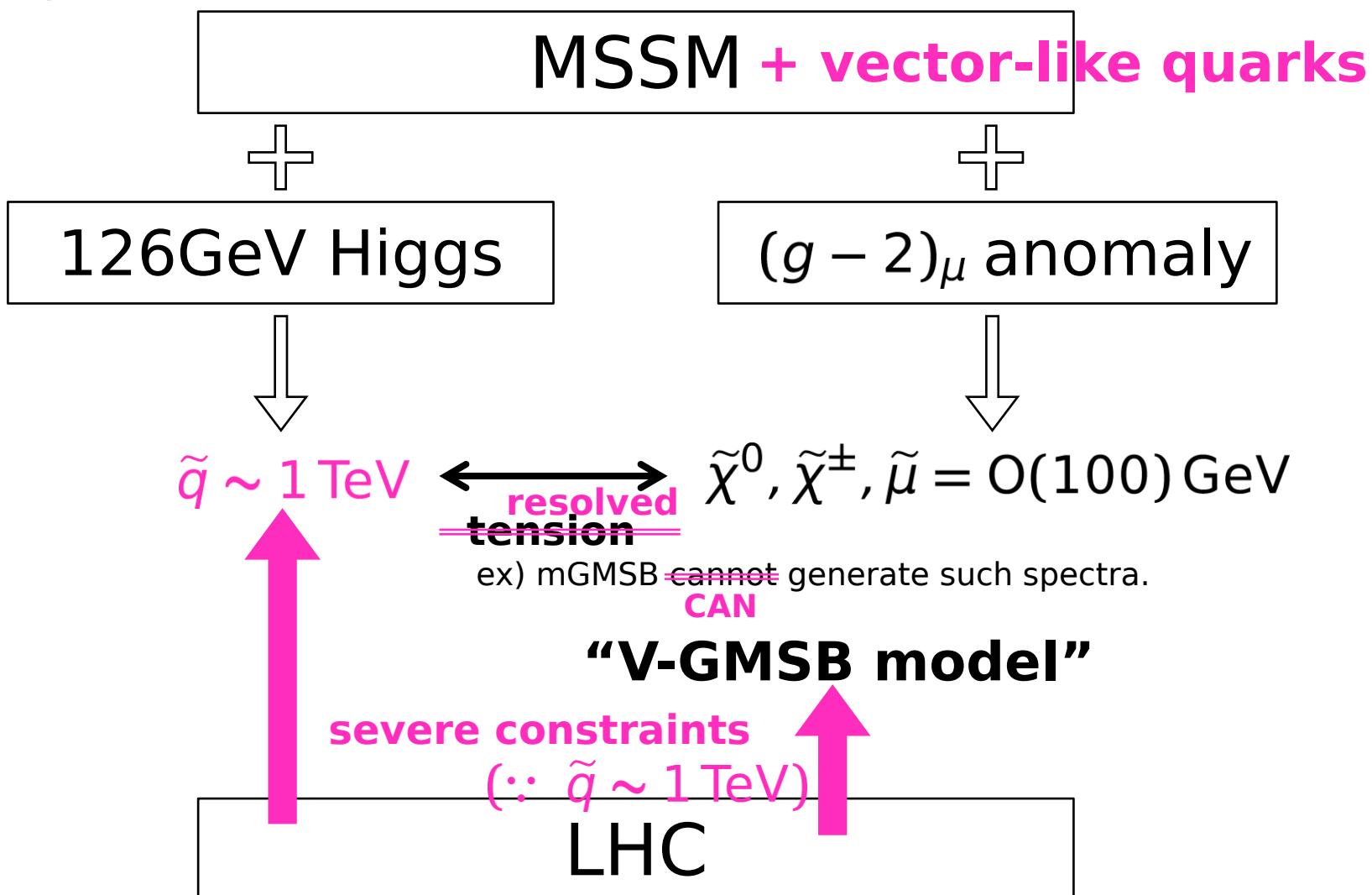
## ● Topic 1.

(Minimal SUSY Standard Model)



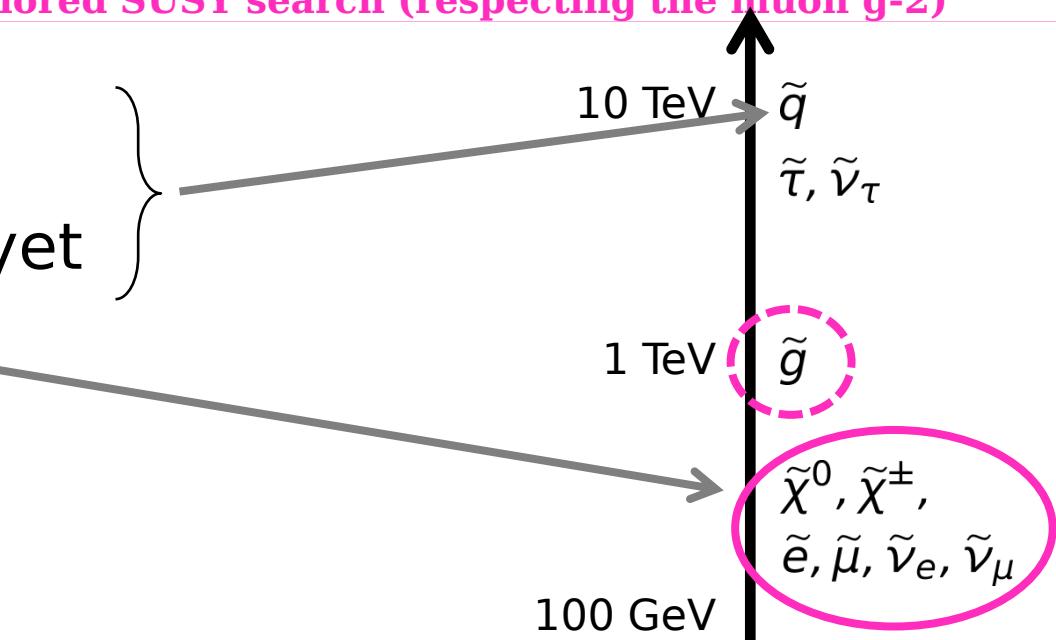
## ● Topic 2.

(Minimal SUSY Standard Model)



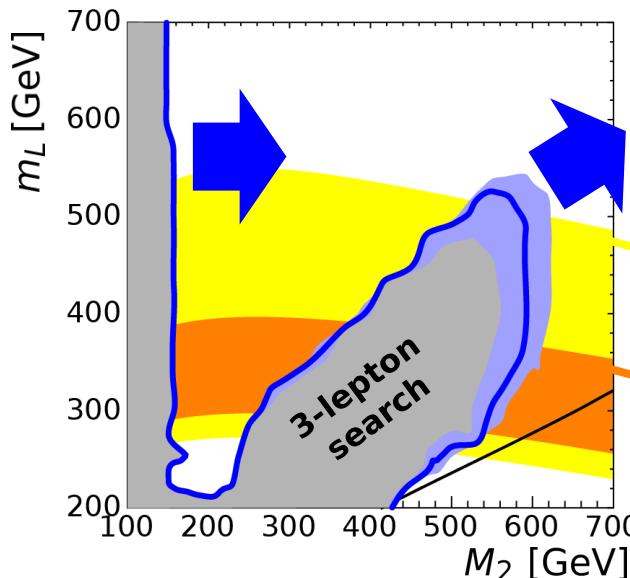
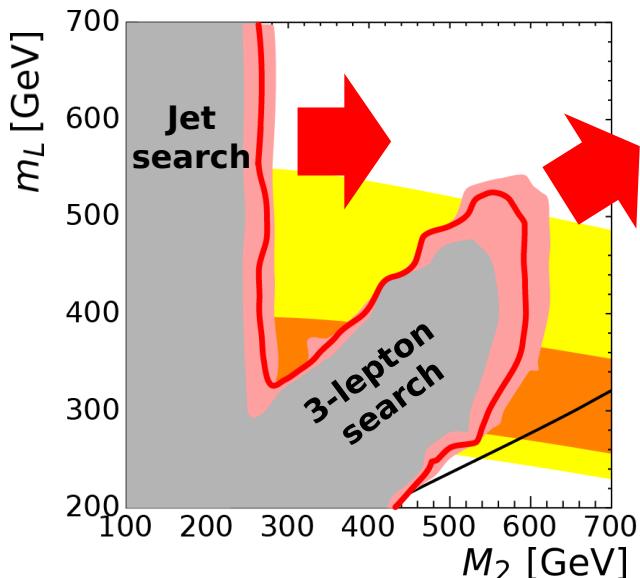
## Summary of Topic 1 : Non-colored SUSY search (respecting the muon g-2)

- 126 GeV Higgs
- SUSY Not Found yet
- $(g - 2)_\mu$  anomaly



An extreme case:  $\mu = 2 \text{ TeV}$ ,  $m_L^2 : m_E^2 = 1 : (1.5)^2$

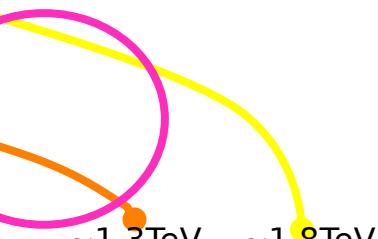
Jet: [ATLAS-CONF-2012-109](#)  
3L: [ATLAS-CONF-2012-154](#)



**How can we search?**

- Heavy gaugino
- Large  $\mu$ -term
- Light sleptons

**... future work.**



# VMSSM + GMSB explains muon g-2 anomaly under 126GeV Higgs

