

#### Cosmological Constraints on *R*-Parity violating SUSY under Lepton Flavor Violation

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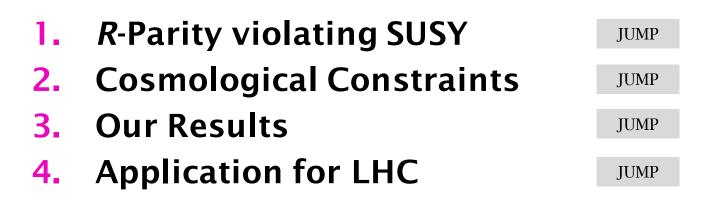
The University of **T**okyo

2010/02/20 KEK-PH 2010 @ KEK/筑波 [Tsukuba]

along the paper

M. Endo, K. Hamaguchi and SI. *Cosmological Constraints on R-parity violation.* arXiv: 0912.0585 [hep-ph] (2009).

# Outline



along the paper M. Endo, K. Hamaguchi and SI. *Cosmological Constraints on R-parity violation.* arXiv: 0912.0585 [hep-ph] (2009).

(about to be published)

# 1. *R*-parity violating SUSY

"To avoid the Proton Decay in the MSSM, we usually impose the *R*-parity. But actually, we have other two choices."

# MSSM and *R*-parity

# MSSM

(Minimal Supersymmetric Standard Model)

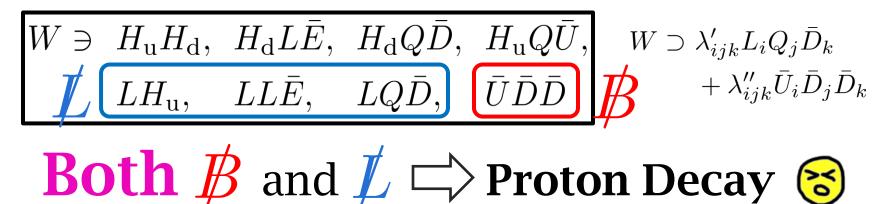
#### $\bigcirc$ Hierarchy problem $\rightarrow$ solved!

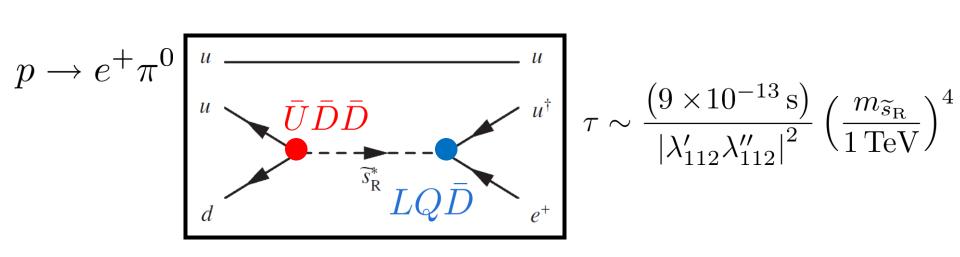
😸 Proton decay problem

Why does Proton decay?

# Proton Decay Problem

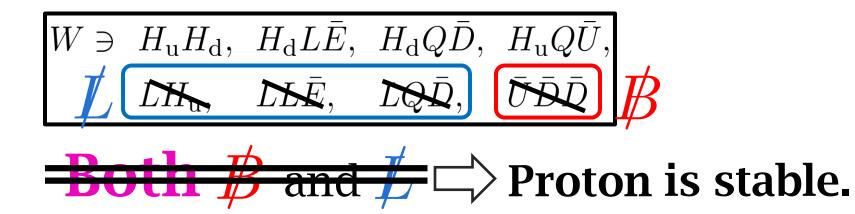
• Superpotential of the MSSM

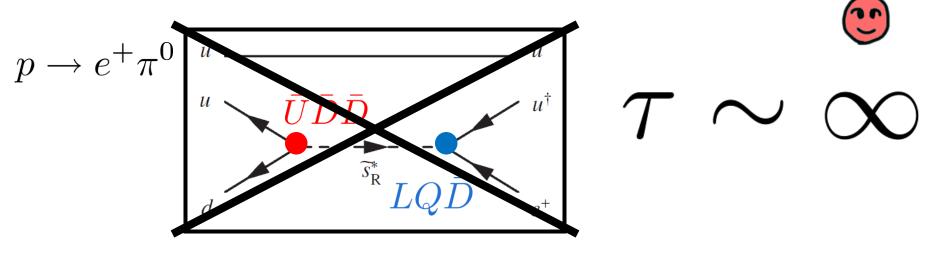




# **R-parity** $P_R := (-1)^{3B-L+2s} (s: spin)$

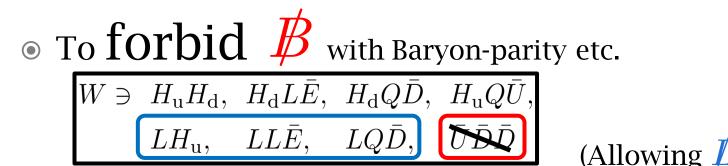
• Superpotential of the MSSM with *R*-Parity conservation





# SUSY without *R*-parity

#### However, since proton decay needs both $\cancel{B}$ and $\cancel{L}$ , we have other two possibilities!



(Allowing  $\mathbf{L}$ )

• To forbid  $\not L$  with Lepton-parity etc.

with assuming  $m_{\text{LSP}} > m_{\text{proton}}$ .

$$W \ni H_{\rm u}H_{\rm d}, H_{\rm d}L\bar{E}, H_{\rm d}Q\bar{D}, H_{\rm u}Q\bar{U}$$

(Allowing  $\cancel{B}$ )

# SUSY without R-parity

That is, we can install RpV interactions additionally.

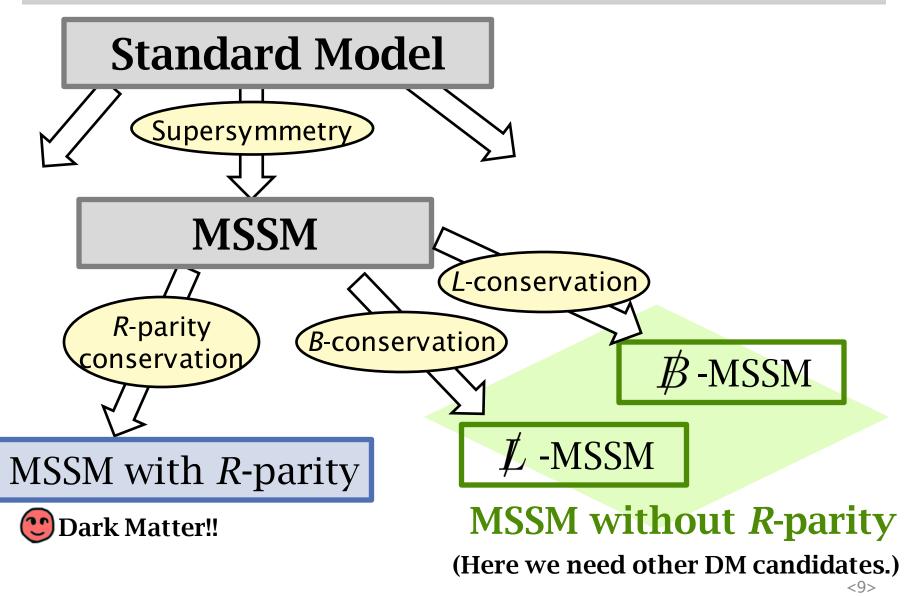
• MSSM with *R*-parity  $\rightarrow W = W_{RPC}$ 

$$W_{\rm RPC} = \mu H_{\rm u} H_{\rm d} + y_{{\rm u}ij} H_{\rm u} Q_i \bar{U}_j + y_{{\rm d}ij} H_{\rm d} Q_i \bar{D}_j + y_{{\rm e}ij} H_{\rm d} L_i \bar{E}_j$$

• 
$$\mathcal{L}$$
-MSSM  $\rightarrow$   
 $W_{\mathcal{L}} = W_{\text{RPC}} + \lambda_{ijk} L_i L_j \bar{E}_k + \lambda'_{ijk} L_i Q_j \bar{D}_k + \kappa_i L_i H_u$   
•  $\mathcal{B}$ -MSSM  $\rightarrow$   
 $W_{\mathcal{B}} = W_{\text{RPC}} + \lambda''_{ijk} \bar{U}_i \bar{D}_j \bar{D}_k$ 

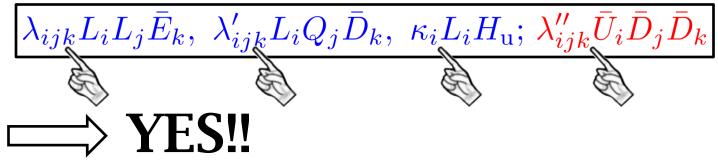
MSSM without *R*-parity

# Introductive Diagram



# What I studied

Can we **CONStraint** such **exotic** couplings?



• **Collider** experiments  $\rightarrow$  various constraints of order  $10^{-(1-2)}$ .

• We analyzed **cosmological** constraints  $\rightarrow$  much more **stringent!** 

(as we will see later...)

# 2. Cosmological Constraints

"The violation of *R*-parity may spoil the current Baryon Asymmetry of the Universe."

## Baryon Asymmetry of the Universe

Current universe:

# There's **Baryon**,

and no anti-baryon.

Baryon

## Baryon Asymmetry of the Universe

Note:

Today we assume that

# Current Baryon Asym. is generated before EWPT. $\widehat{\}$ $T \gtrsim 100 \, \text{GeV}$

## Baryon Asymmetry of the Universe

Current universe:

# There's **Baryon**,

and no anti-baryon.

Baryon



However, if we have  $W \ni \lambda'' \overline{U} \overline{D} \overline{D}$  interaction,

$$\widetilde{q} \rightleftharpoons \overline{q} \overline{q}, \quad \widetilde{q}^* \rightleftharpoons qq$$
  
in the early universe.

And if frequently enough,  $\rightarrow$  achieve **Equilibrium** : B = 0.

→ No Baryon Asymmetry! "WASH-OUT" 🔂

 $\rightarrow \lambda''$  must be **small enough!** 

Bouquet and Salati, 1987

# Wash-out with B-viol.



# That is, if LARGE , then "WASH-OUT" occurs!! (S)

But this is a bit **naïve** view... We have to consider **"sphaleron."**  Manton, 1983; Klinkhamer and Manton, 1984; 't Hooft, 1976

Kuzmin, Rubakov, Shaposhnikov, 1985; Ringwald, 1988

# Sphaleron

$$\mathcal{O}_{\rm sph} = \prod_{i} (udd\nu)_{i} \\ \Delta L = 1 \quad 1 \quad 1 \\ = uddcsstbb\nu_{e}\nu_{\mu}\nu_{\tau} \\ \Delta B = \frac{1}{3}\frac{1}{3}\frac{1}{3}\frac{1}{3}\frac{1}{3}\frac{1}{3}\frac{1}{3}\frac{1}{3}\frac{1}{3}\frac{1}{3}\frac{1}{3}} \\ \Delta B = 3, \Delta L = 3; \ \Delta (B - L) = 0$$

In the early universe (temperature  $T \gtrsim 100 \,\mathrm{GeV}$ )

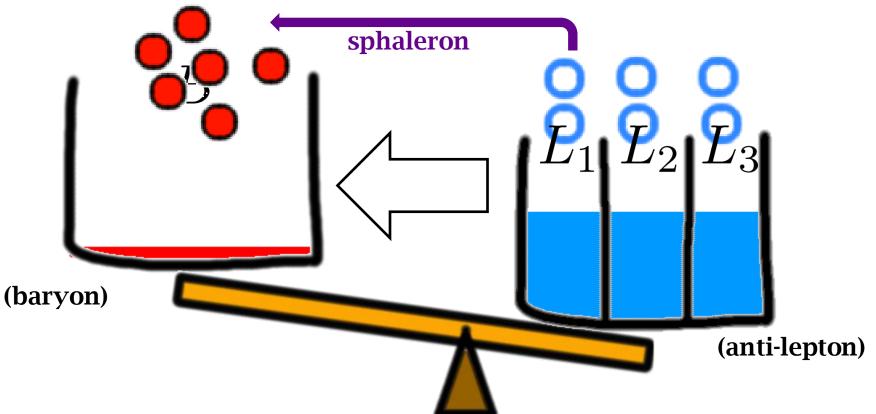
 $\rightarrow$  the **sphaleron** process is **frequent**. (by thermal effects) Sphaleron converts

Baryon 
$$\rightleftharpoons$$
 Anti-lepton

 $\rightarrow$  Equilibrium.

If Baryon is short...

sphaleron works right to left

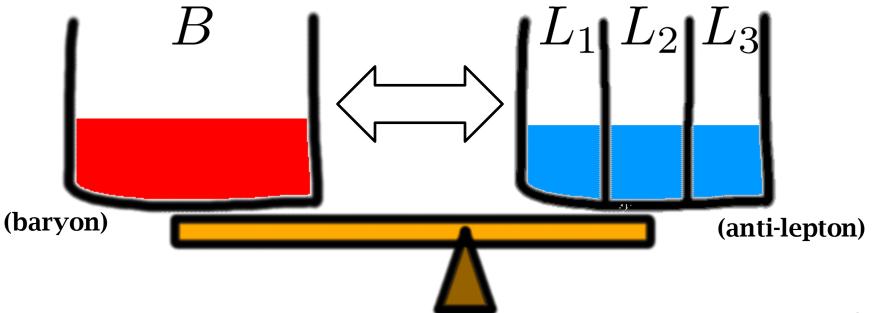


 $(\text{in } T \gtrsim 100 \,\text{GeV})$ 

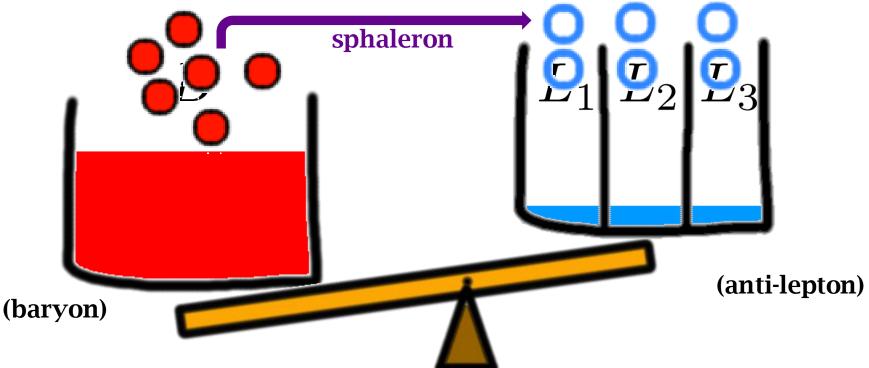
If Baryon is short...

(in  $T \gtrsim 100 \,\mathrm{GeV}$ )

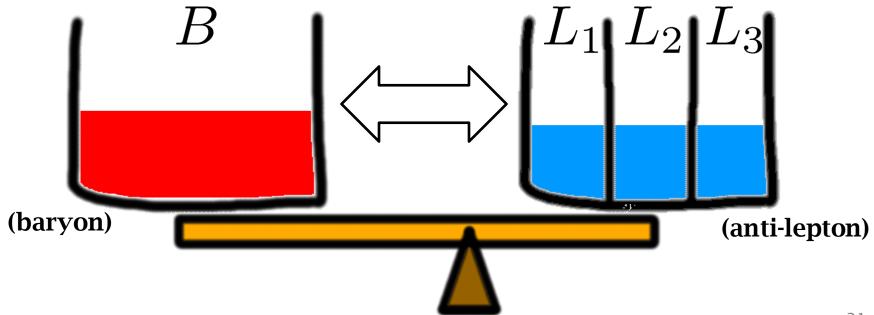
sphaleron works right to left and achieve Equilibrium.



#### Also when (anti-)Lepton is short, $(in T \gtrsim 100 \,\text{GeV})$ sphaleron does left to right

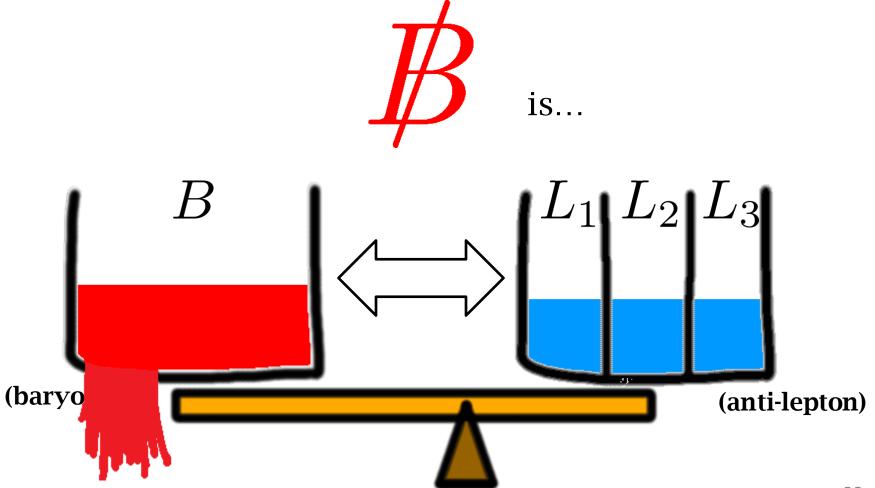


#### Also when (anti-)Lepton is short, sphaleron does left to right and achieve Equilibrium.



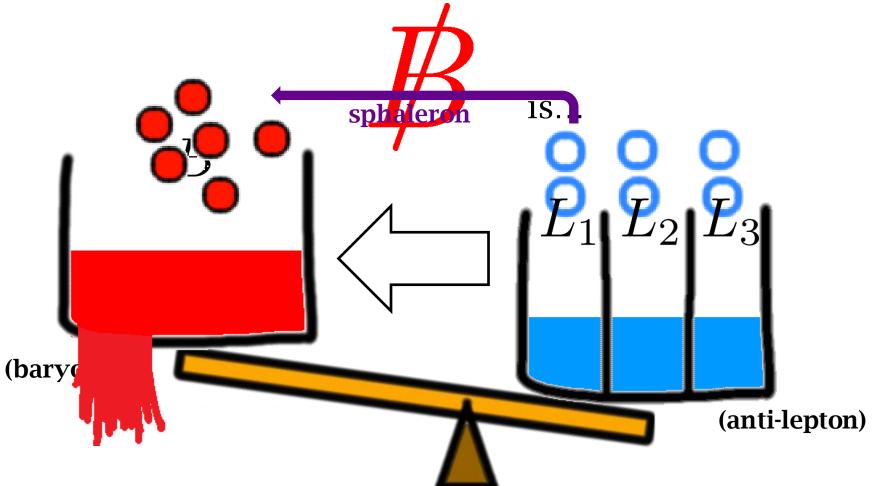


Thus, actually the previous wash-out by



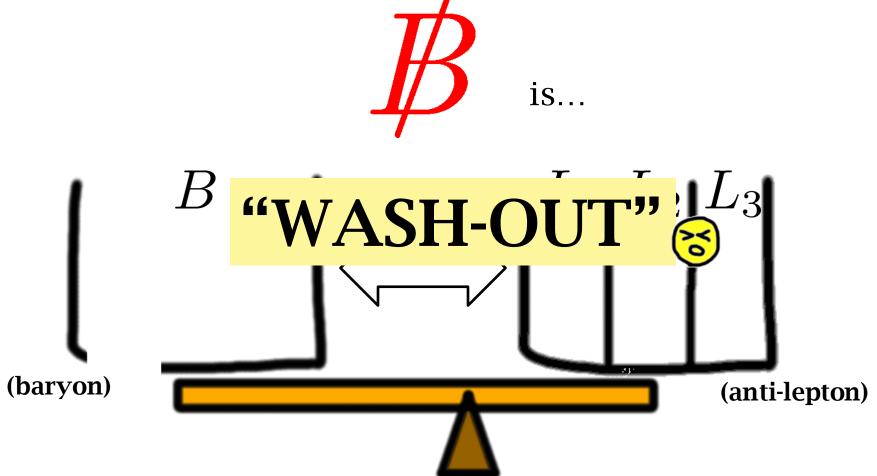


Thus, actually the previous wash-out by





Thus, actually the previous wash-out by

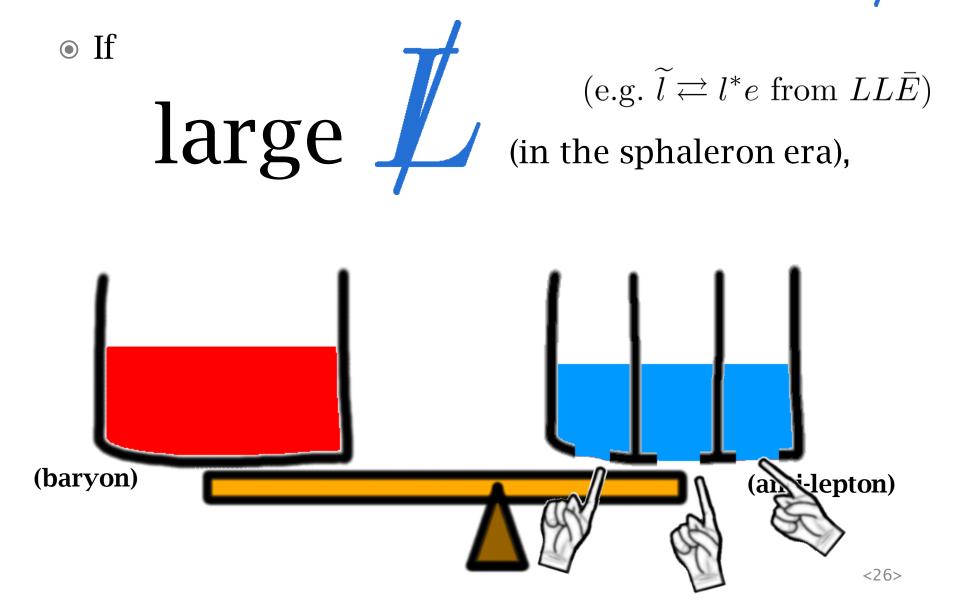


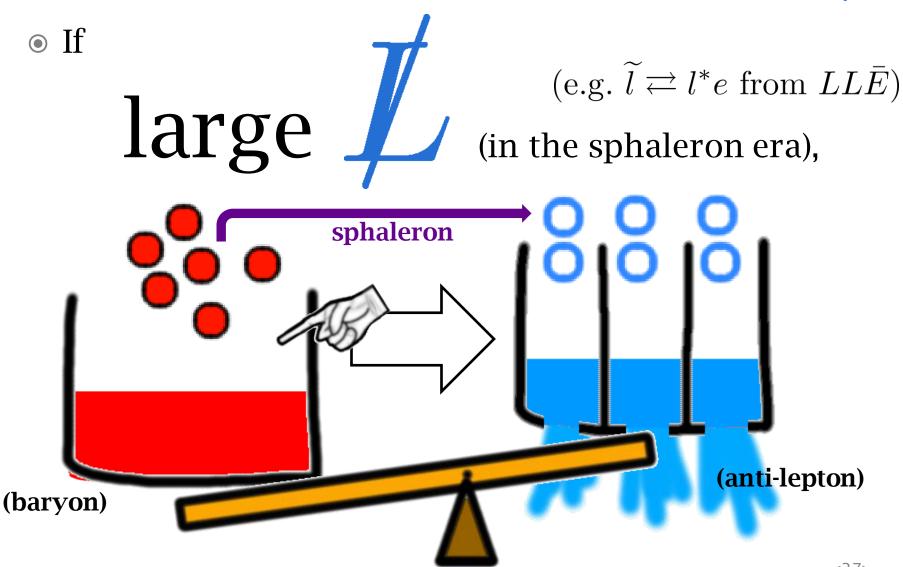
Kuzmin, Rubakov and Shaposhnikov, 1985

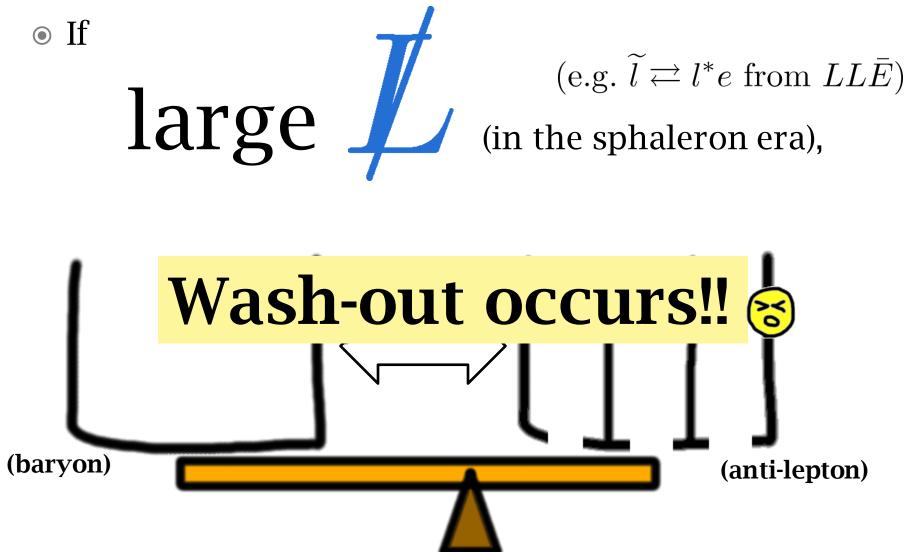
# Wash-out with L-viol.

# This story

# does not end here!

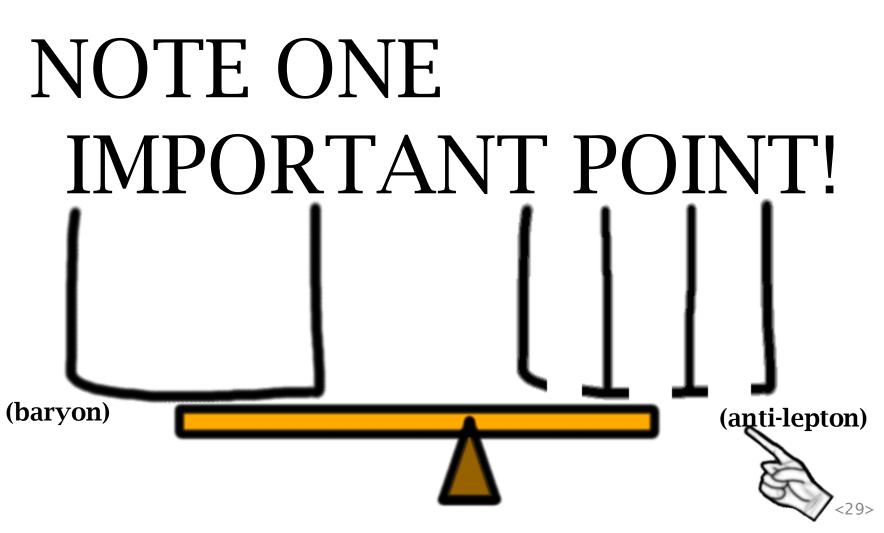






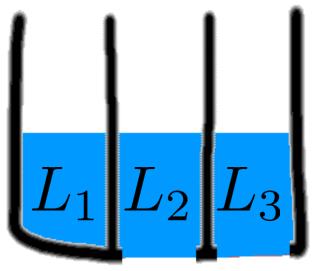
# Wash-out with L-viol.

But

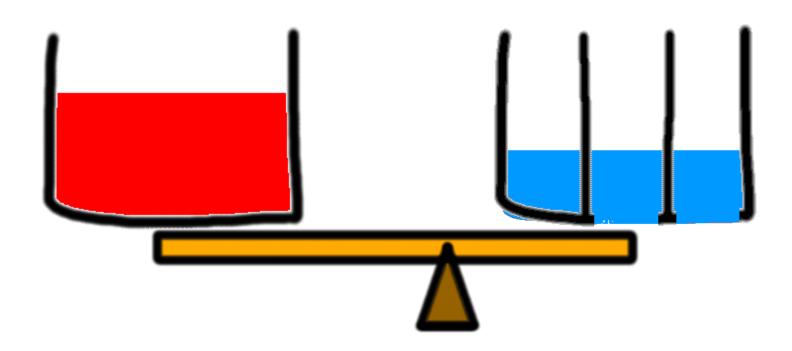


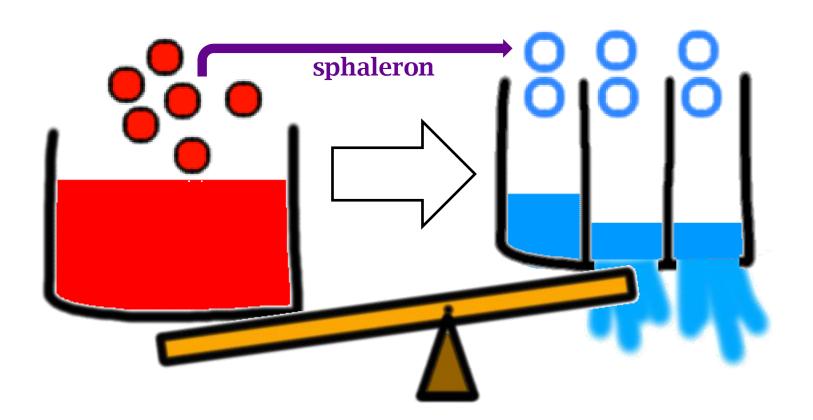
# Wash-out with L-viol.

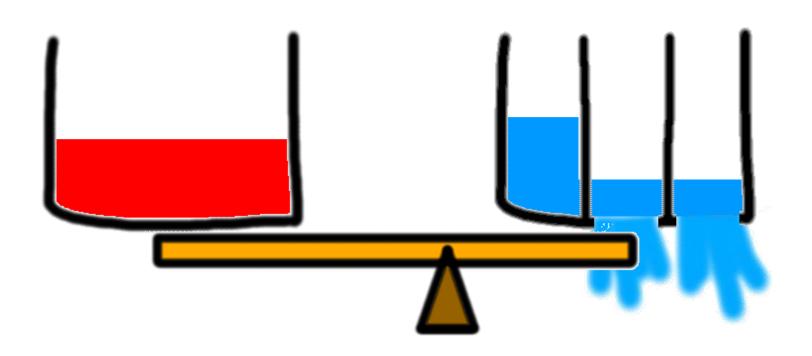
Imagine this case.

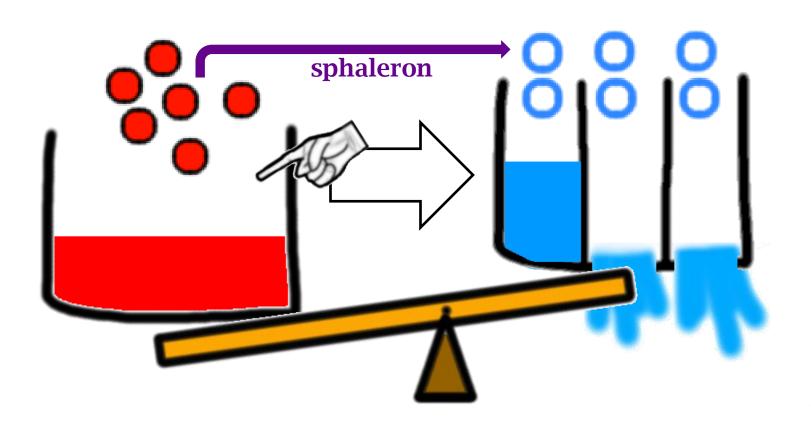


# If the Lepton Flavor is NOT violated, and $L_i$ is conserved,



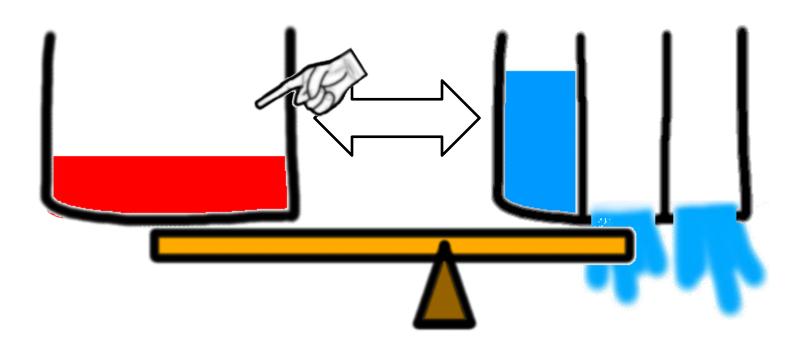


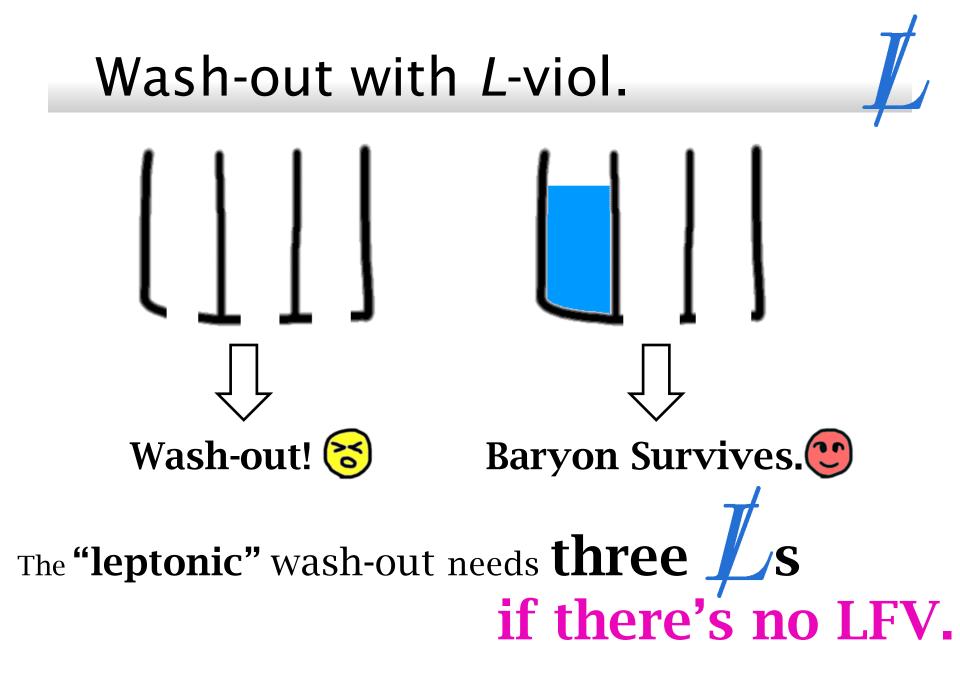




# Wash-out with L-viol.

# Baryon SURVIVES!!! @





Endo, Hamaguchi, and SI, 2009

### Wash-out with L-viol.



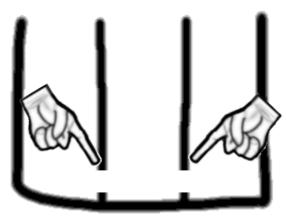
#### But remember! In MSSM,

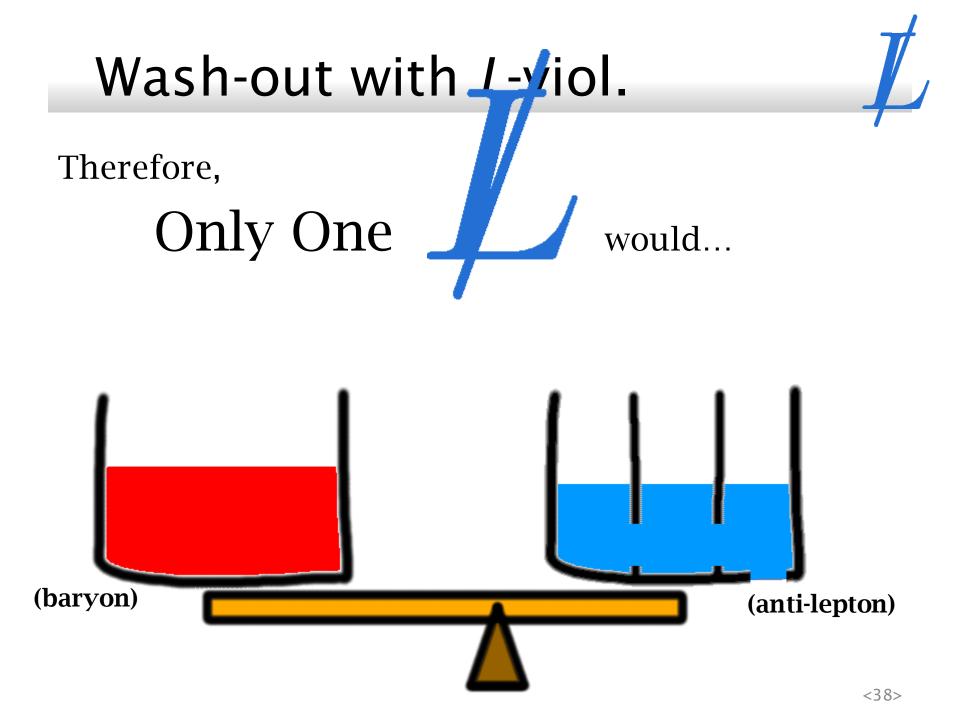
## We have LFVS in general!!!

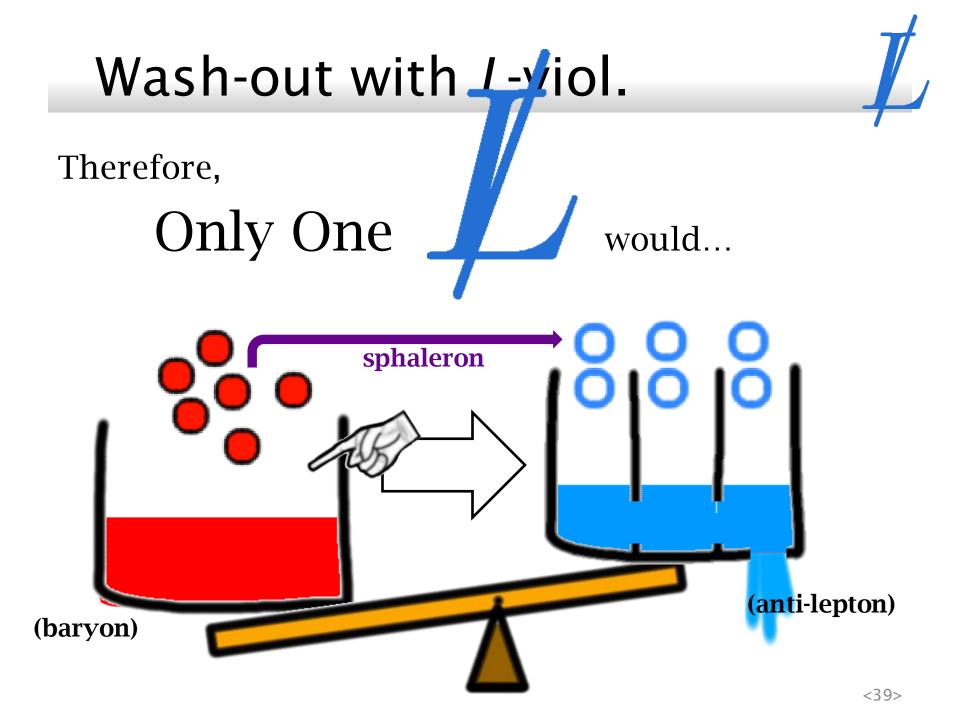
The Standard Model

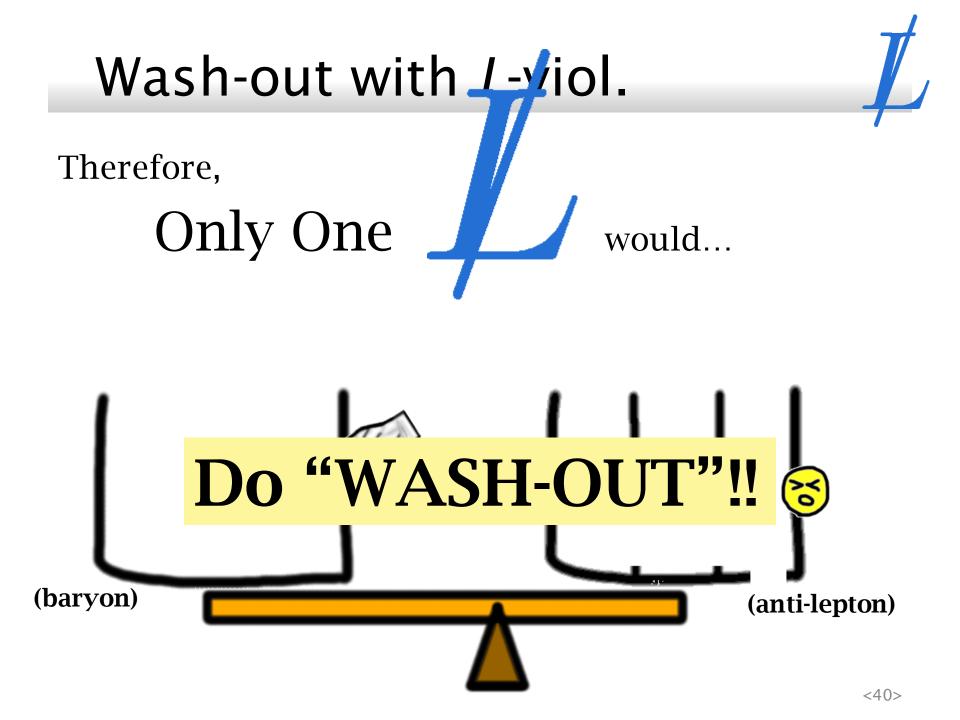


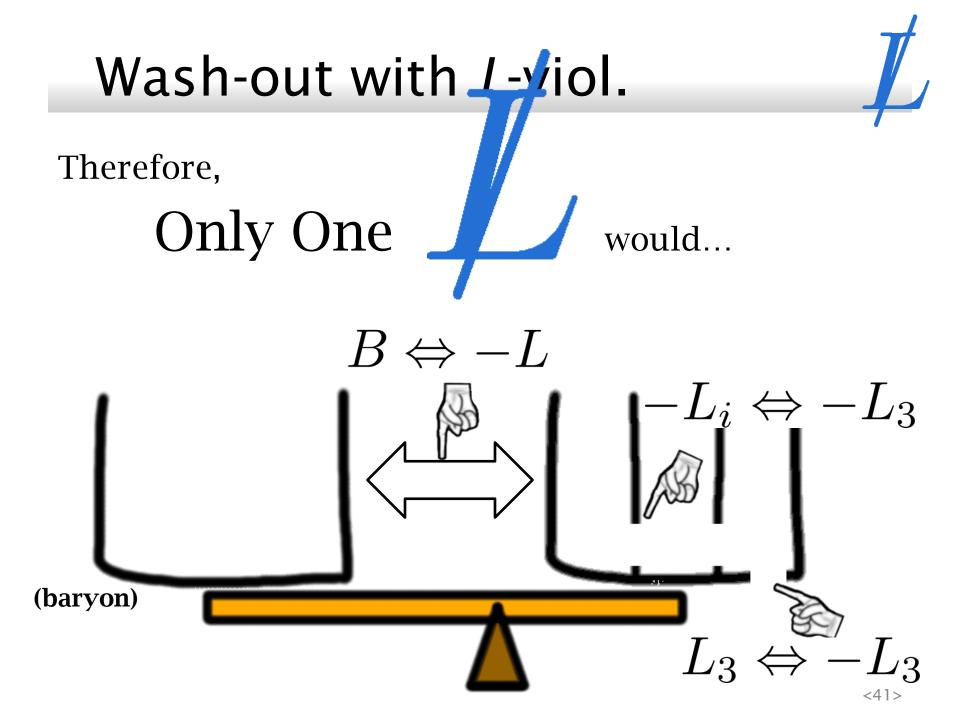
As Shimomura-san mentioned. The MSSM

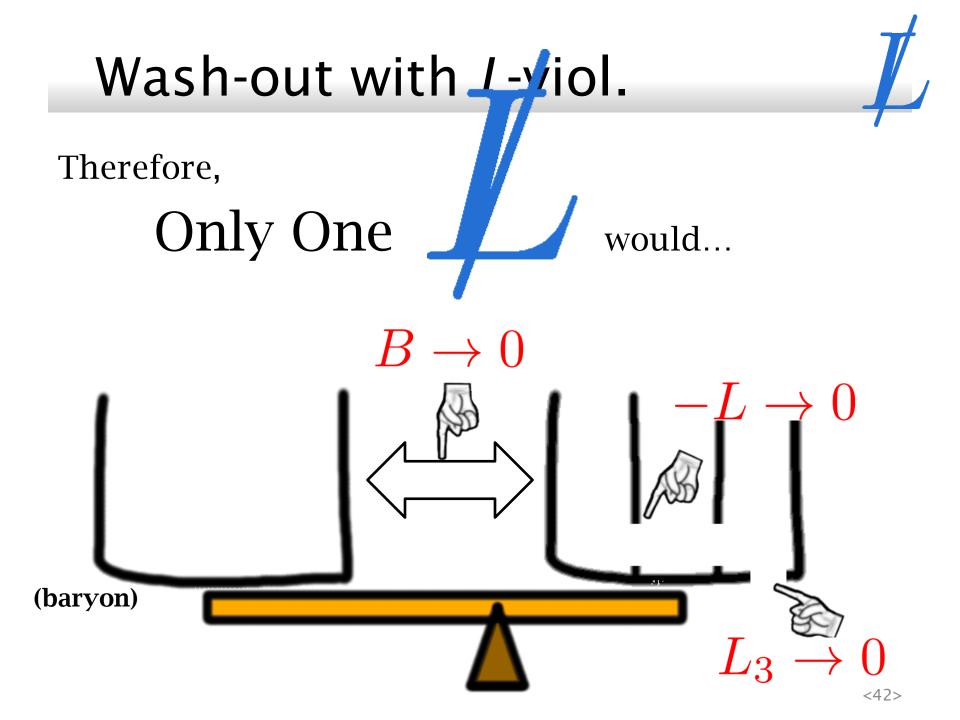










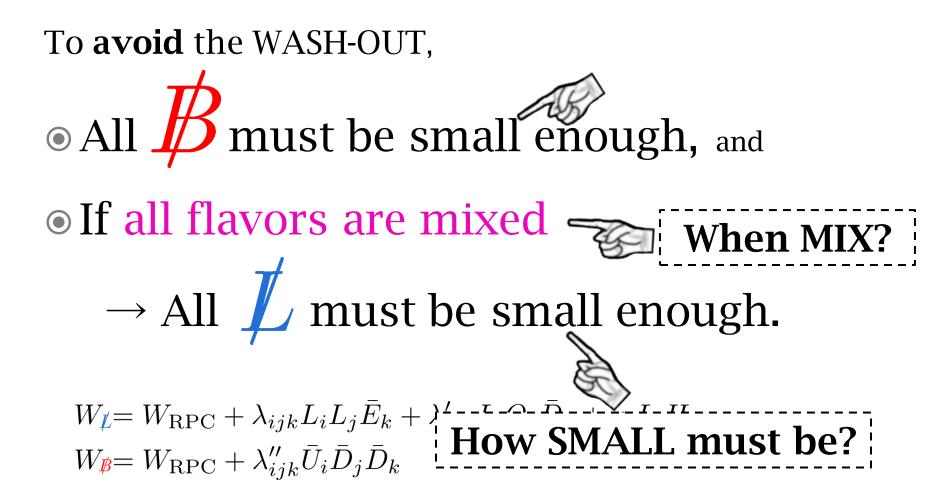


### These are what we studied!

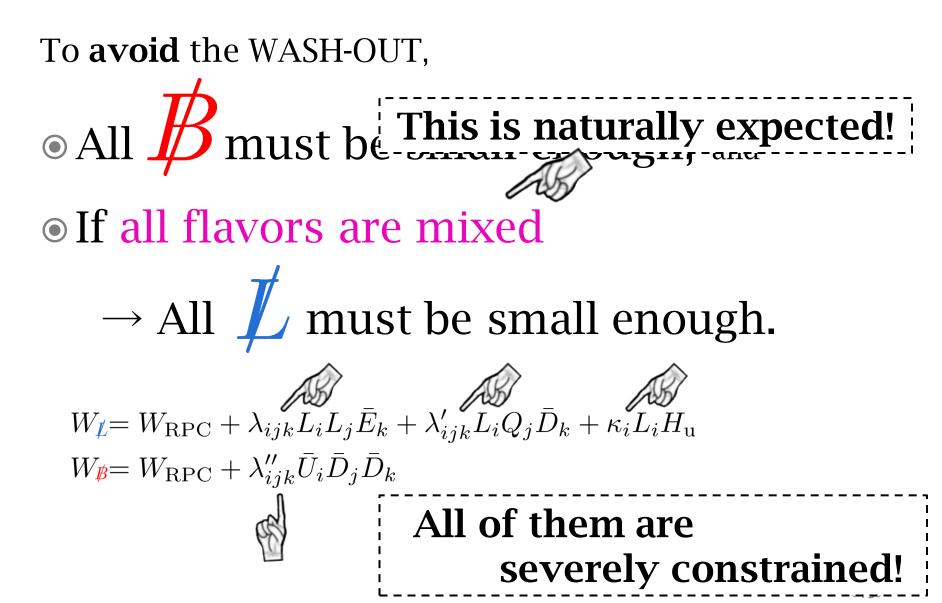
To **avoid** the WASH-OUT, • All  $\not B$  must be small enough, and • If all flavors are mixed  $\rightarrow$  All  $\not L$  must be small enough.

 $W_{\mathbb{Z}} = W_{\text{RPC}} + \lambda_{ijk} L_i L_j \bar{E}_k + \lambda'_{ijk} L_i Q_j \bar{D}_k + \kappa_i L_i H_u$  $W_{\mathbb{B}} = W_{\text{RPC}} + \lambda''_{ijk} \bar{U}_i \bar{D}_j \bar{D}_k$ 

### These are what we studied!



### And we will claim that...



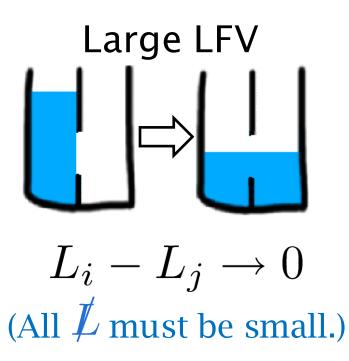
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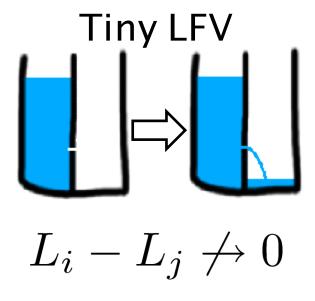
#### 3. Our Results

#### Lepton number density in *i*-th generation

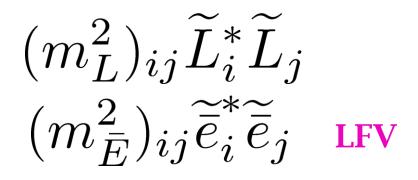
We calculated

# $\frac{\mathrm{d}}{\mathrm{d}t} \left( L_i - L_j \right)$ by **Boltzmann Eq.**





 $(h_i)H_{\rm d}L_iE_i$ 



#### Generally NOT diagonal

As Shimomura-san discussed.

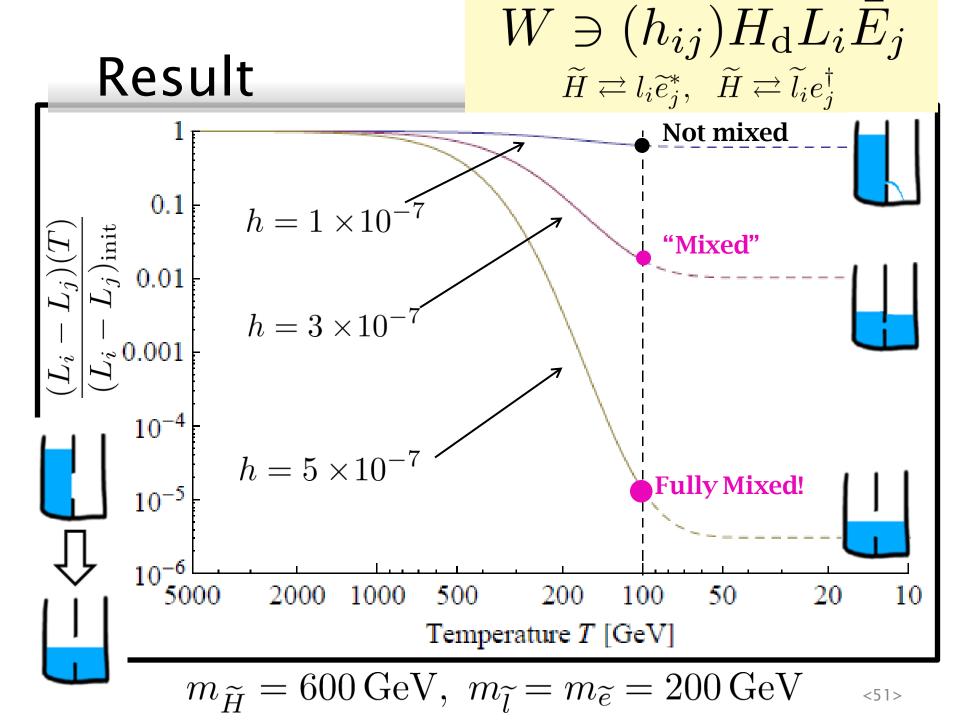
$$(h_{i})H_{d}L_{i}\bar{E}_{i} \qquad (m_{L}^{2})_{ij}\widetilde{L}_{i}^{*}\widetilde{L}_{j} \\ \begin{pmatrix} h_{i}\end{pmatrix}H_{d}L_{i}\bar{E}_{i} & (m_{\bar{E}}^{2})_{ij}\widetilde{e}_{i}^{*}\widetilde{e}_{j} & \text{LFV} \\ \end{bmatrix}$$

$$\begin{array}{c} \text{Diagonalize} \\ \text{by }\theta \text{ rotation} \\ \text{``mixing angle''} \\ \end{pmatrix} \\ \begin{array}{c} \text{LFV} (h_{ij})H_{d}L_{i}\bar{E}_{j} & (m_{L}^{2})_{i}\widetilde{L}_{i}^{*}\widetilde{L}_{i} \\ h_{ij} = h_{i}\theta_{ij}^{\bar{E}} + h_{j}\theta_{ji}^{L} & (m_{\bar{E}}^{2})_{i}\widetilde{e}_{i}^{*}\widetilde{e}_{i} \end{array}$$

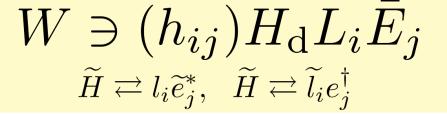
For example

$$h_{23} \simeq \left(0.006 \cdot \theta_{23}^{\bar{E}} + 0.1 \cdot \theta_{32}^{L}\right) \left(\frac{\tan\beta}{10}\right)$$

(We know  $h_i$  , because we know the lepton masses.)



#### Conclusion



 $\| h \gtrsim 3 \times 10^{-7} \rightarrow \text{MIXED}$ 

This corresponds to  $\theta_{23}, \theta_{13} \gtrsim 3 \times 10^{-6},$  $\theta_{12} \gtrsim 7 \times 10^{-5}.$ 

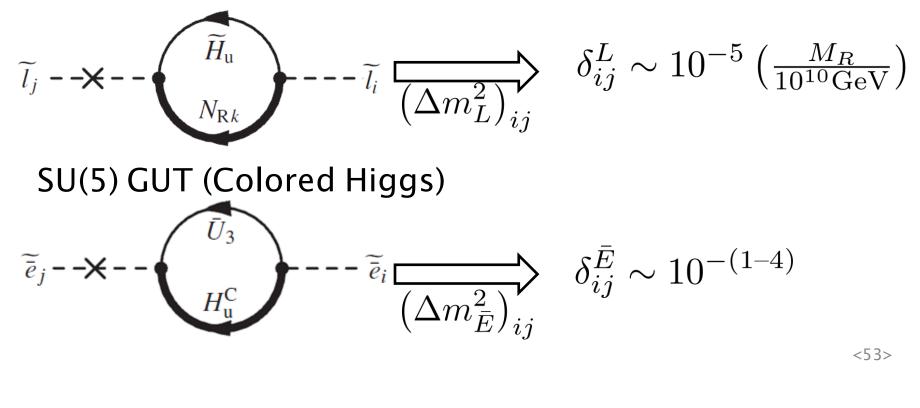
By the way,

Remember:  $h_{23} \simeq \left( 0.006 \cdot \theta_{23}^{\bar{E}} + 0.1 \cdot \theta_{32}^{L} \right) \left( \right)$  $\frac{\tan\beta}{10}$ 

#### Conclusion

 $W \ni (h_{ij})H_{\rm d}L_iE_j$  $\widetilde{H} \rightleftharpoons l_i \widetilde{e}_i^*, \quad \widetilde{H} \rightleftharpoons \widetilde{l}_i e_i^\dagger$ 

**Right-handed neutrino** 



where 
$$\delta_{ij}^X := \frac{(m_X^2)_{ij}}{(m_X^2)_{\text{diag}}}.$$

## Conclusion

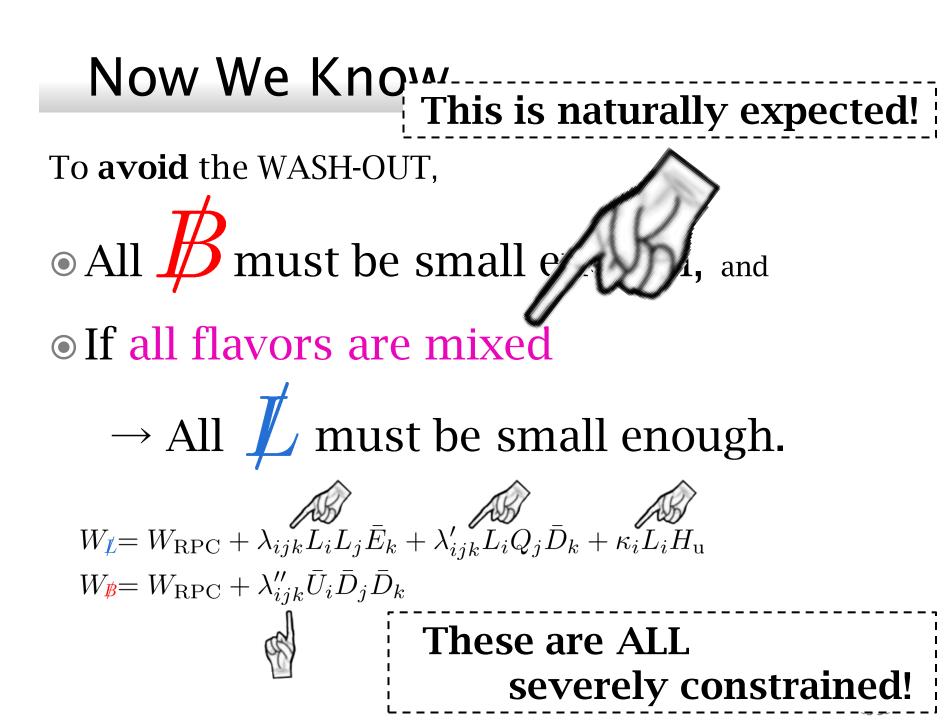
 $\delta_{ii}^{\bar{E}} \sim 10^{-(1-4)}$ 

 $W \ni (h_{ij}) H_{\mathrm{d}} L_i \bar{E}_j$  $\widetilde{H} \rightleftharpoons l_i \widetilde{e}_j^*, \quad \widetilde{H} \rightleftharpoons \widetilde{l}_i e_j^\dagger$ 

 $\underbrace{\bigcup}_{\substack{\theta_{23}, \theta_{13} \gtrsim 3 \times 10^{-6}, \\ \theta_{12} \gtrsim 7 \times 10^{-5}.} \rightarrow \text{MIXED}}_{\text{Naturally Expected!}}$   $\underbrace{\text{Expected Value}}_{\substack{\delta_{ij}^L \sim 10^{-5} \left(\frac{M_R}{10^{10} \text{GeV}}\right)}} \qquad \underbrace{\text{Experimental Reach}}_{\substack{\text{MEGA} : \delta_{21}^L \lesssim 10^{-3}}$ 

MEG :  $\delta_{21}^L \Rightarrow 10^{-4}$ 

$$\left(\theta_{ij} \sim \frac{m_{ij}^2}{m_i^2 - m_j^2} = \frac{m_{\text{diag}}^2}{m_i^2 - m_j^2} \delta_{ij}\right)$$



#### Constraints on RpVs

• In a similar manner...

$$\frac{\mathrm{d}}{\mathrm{d}t} \left( B - L \right)$$
 $\rightarrow$  calculated by the Boltzmann Eq.

We obtained the bounds for

*R*-parity violating couplings.

#### Just the results...

$$\begin{split} \lambda \lesssim 1 \times 10^{-6} \\ \lambda' \lesssim 3 \times 10^{-7} \\ \kappa \lesssim 1.5 \times 10^{-6} \\ \lambda'' \lesssim 4 \times 10^{-7} \end{split} \text{ (For all } i, j, k) \\ W_{\underline{I}} = W_{\text{RPC}} + \lambda_{ijk} L_i L_j \bar{E}_k + \lambda'_{ijk} L_i Q_j \bar{D}_k + \kappa_i L_i H_u \\ W_{\underline{I}} = W_{\text{RPC}} + \lambda''_{ijk} \bar{U}_i \bar{D}_j \bar{D}_k \end{split}$$

For

$$m_{\widetilde{q}} = 600 \,\mathrm{GeV}, \ m_{\widetilde{H}} = 300 \,\mathrm{GeV}, \ m_{\widetilde{l}} = 100 \,\mathrm{GeV}.$$

#### 4. Application for LHC

"Now we have a good tool to study LHC phenomenology of RpV-MSSM."

#### SUSY Detection @ LHC

• **SUSY detection** in LHC is important.

*R*-parity is Conserved  $\rightarrow$  LSP  $\mathcal{P}_{T}$  Signal  $\bigcirc$ 

Then if not? → LSP decays! How to detect RpV-SUSY? 😒

#### **Application for LHC**

Stringent RpV-constraint of order  $10^{-(5-7)}$   $\rightarrow$  LSP is a bit "long-lived."

• Example:  $W \ni \lambda_{ij3} L_i L_j \bar{E}_3$  ( $\tilde{\tau}$ -LSP)  $\tilde{\tau} \longrightarrow l \nu$ 

Decay Length  $\simeq 50 \,\mu \mathrm{m} \left(\frac{\lambda_{ij3}}{10^{-6}}\right)^{-2} \left(\frac{m_{\tilde{\tau}}}{100 \,\mathrm{GeV}}\right)^{-1}$ (cf. tau-lepton: 87  $\mu \mathrm{m}$ )

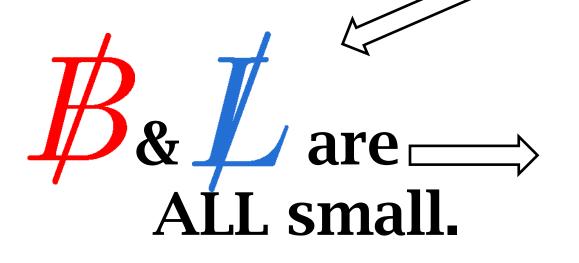
## To be a good signal of RpV-SUSY? $\rightarrow$ Future works!

# That's all. Thank you for listening.



## $MSSM \sqsubset$ *R*-parity is not a must.





LSP would be a bit **long-lived** even if **NO** *R***-Parity.** 

#### Appendices

A) Hierarchy Problem	JUMP
B) Weak points of RpV-MSSM	JUMP
C) Collider Constraints	JUMP
D) The RpV Results	JUMP
E) Several Details	JUMP
F) Experimental LFV Bounds	JUMP

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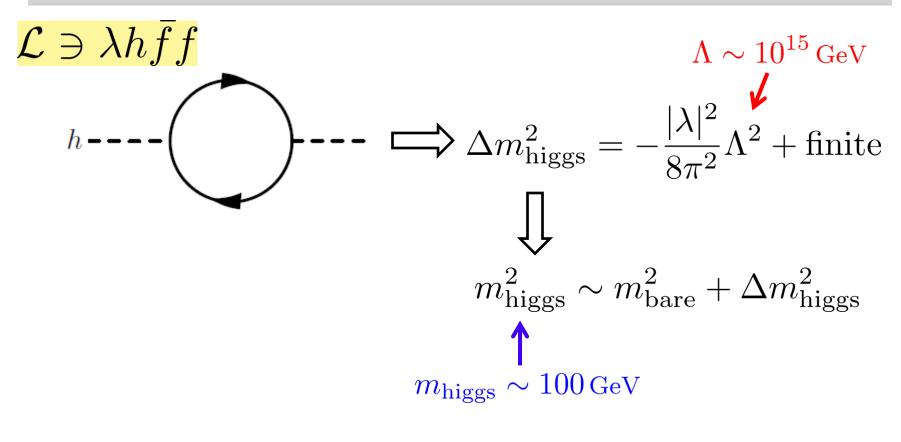
#### A. Hierarchy Problem

"In the Standard Model, the quantum correction for the mass of the Higgs requires a miraculous cancellation as  $O(10^{30}) - O(10^{30}) \rightarrow 10^4 ~!?$ "

In the

# Standard Model

with Higgs,

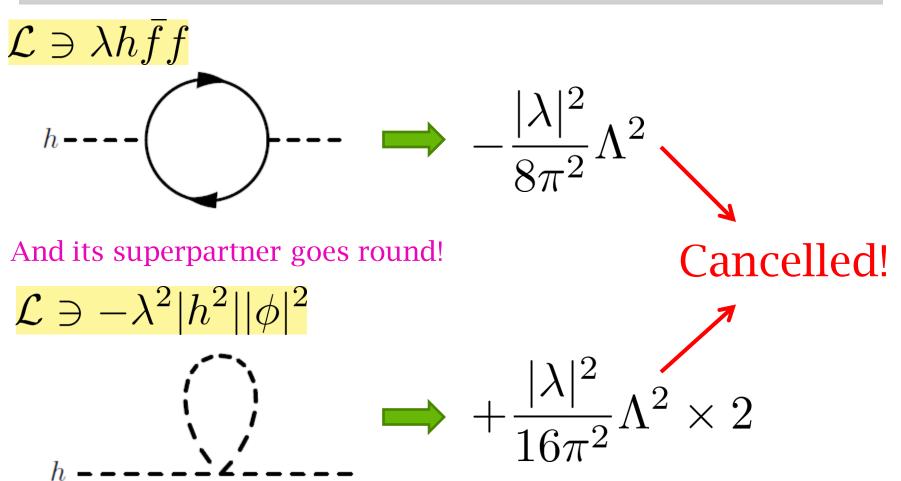


: 
$$O(10^{30}) - O(10^{30}) \to 10^4 !?$$

• In

# MSSM

(or other SUSY models),



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**APPENDICES** 

#### B. Weak Points of RpV-MSSM

"The RpV-MSSM has some weak points, but anyway important for the SUSY detection."

### Weak point of "RpV-MSSM"

#### Weak Points

- Anyway we need "some symmetry."
- Dark Matter  $\rightarrow$  left unsolved.
- GUT compatibility... ( $\bullet \omega \bullet \$ )

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**APPENDICES** 

#### C. Collider Constraints

"The RpV interactions are constrained by several experimental facts."

#### Constraints

The RpV parameters

 $\{\kappa, \lambda, \lambda'\}, \{\lambda''\}$ 

 $\rightarrow$  experimental constraints

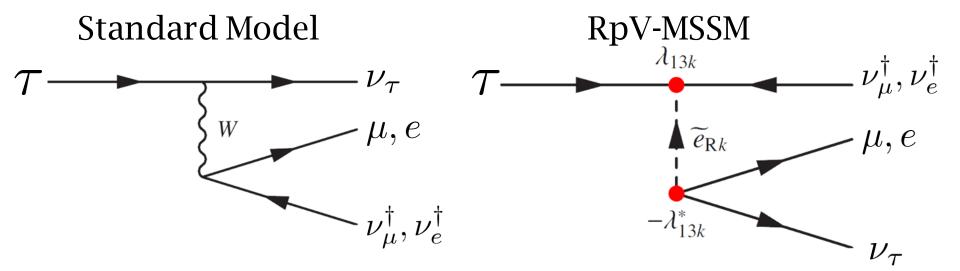
And the constraints are important to study RpV-MSSM.

$$W_{\rm RPV} = \kappa_i L_i H_{\rm u} + \lambda_{ijk} L_i L_j \bar{E}_k + \lambda'_{ijk} L_i Q_j \bar{D}_k$$
  
or  $= \lambda''_{ijk} \bar{U}_i \bar{D}_j \bar{D}_k$ 

## Constraints

• Example:

$$R_{\tau} = \frac{\Gamma(\tau \to \nu_{\tau} \, e \, \nu_{e}^{\dagger})}{\Gamma(\tau \to \nu_{\tau} \, \mu \, \nu_{\mu}^{\dagger})}$$



## **Additional Contribution!**

## Constraints

 $\mathcal{T}$ 

$$\frac{R_{\tau}}{(R_{\tau})_{\rm SM}} = 1 + \frac{2}{4\sqrt{2}G_{\rm F}} \sum_{k} \frac{|\lambda_{13k}|^2 - |\lambda_{23k}|^2}{(m_{\tilde{e}_{\rm R}k})^2}$$

$$R_{\tau} = \underbrace{(R_{\tau})_{\rm expm}}_{\ell} = 1.028(4)$$

$$(R_{\tau})_{\rm SM} = 1.028$$

$$\underbrace{(R_{\tau})_{\rm SM}}_{\ell} = 1.028$$

$$\underbrace{(R_{\tau})_{\rm SM}}_{\ell} = 1.028$$

$$\underbrace{(R_{\tau})_{\rm SM}}_{\ell} = 1.028$$

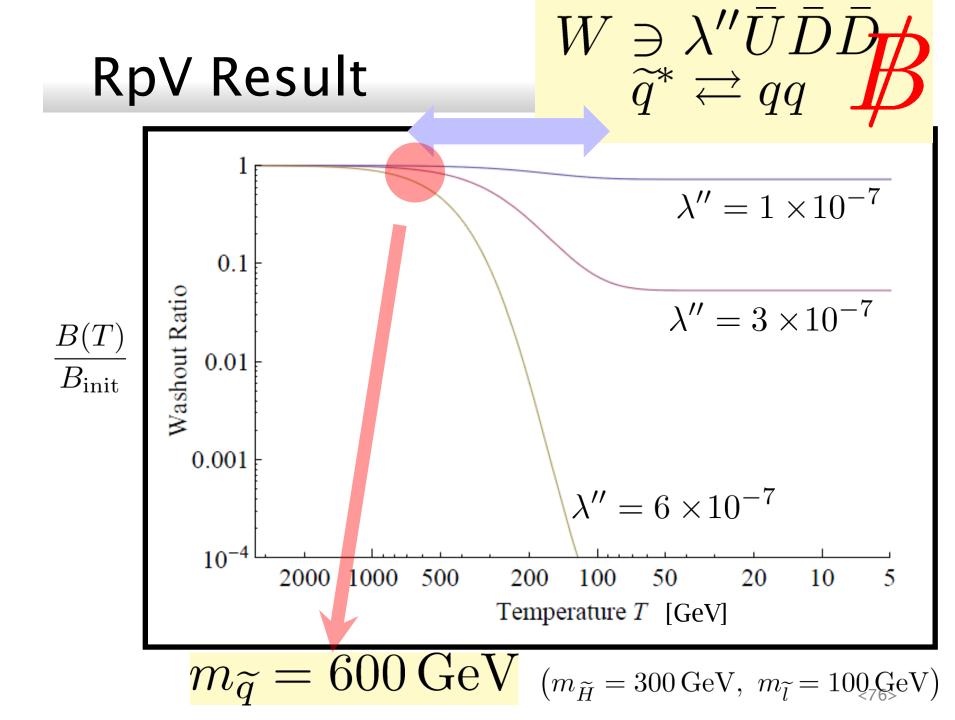
$$\underbrace{(R_{\tau})_{\rm SM}}_{\ell} = 1.028$$

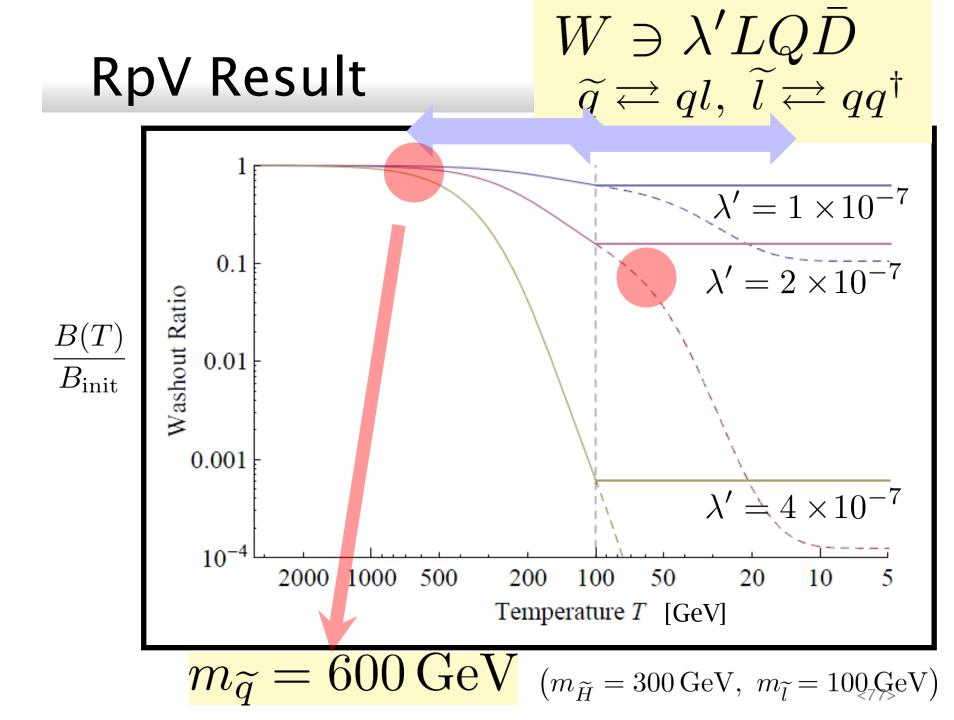
## **Additional Contribution!**

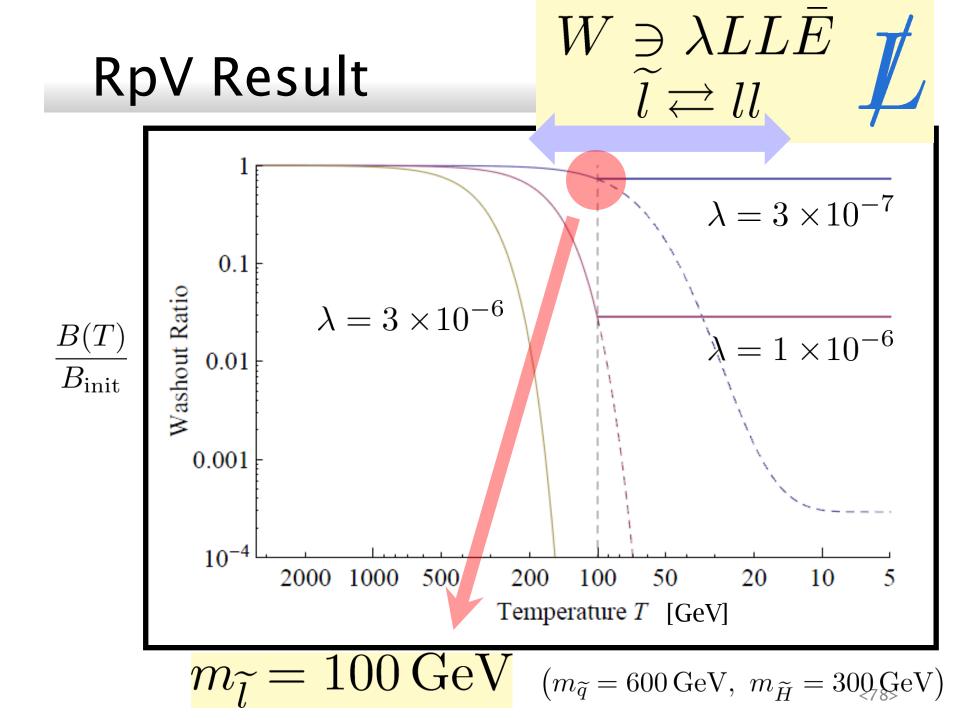
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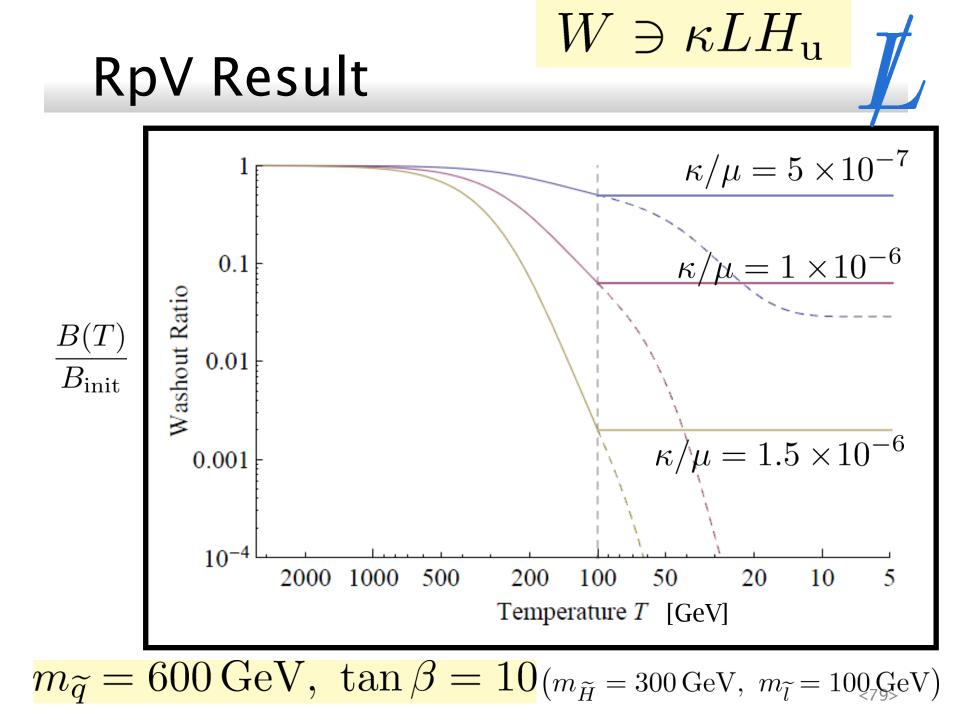
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## D. RpV Results









## E. Several Details

# Approximations we used $(y_e)_{ij}H_dL_i\overline{E}_j$

#### <u>Set up</u>

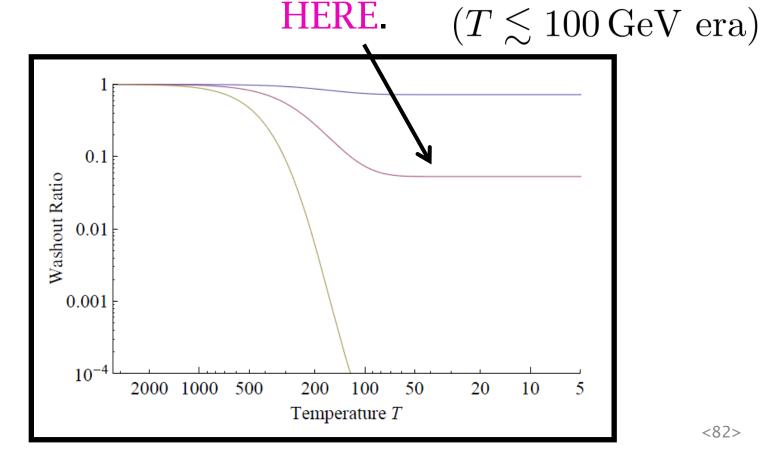
• MSSM; **before EWPT** (sphaleron era:  $T \gtrsim 100 \,\text{GeV}$ )

### **Approximations**

- We consider only the decay of Higgsino  $\widetilde{H} \rightleftharpoons l_i \widetilde{e}_j^*, \quad \widetilde{H} \rightleftharpoons \widetilde{l}_i e_j^{\dagger}$ and the antiparticles' processes.
- Mass of Higgs bosons  $\rightarrow$  Ignored
- Fermi/Bose distribution → **Boltzmann** distribution
- Sphaleron  $\rightarrow$  Shut off at T = 100 GeV.

# Some Loophole

# We can avoid any "wash-out" with creating the current *B*-asymmetry



# F. Experimental LFV Bounds

## MEGA Result / MEG Prospect

 $\delta_{21}^L \sim \sqrt{10^{+(4-5)} \operatorname{Br}(\mu \to e\gamma)} \frac{10}{\tan \beta} \left(\frac{m_{\text{soft}}}{400 \operatorname{GeV}}\right)^2$   $\operatorname{MEGA} : \operatorname{Br} < 1.2 \times 10^{-11}$   $\delta_{21}^L \lesssim 10^{-3}$   $\operatorname{MEG} : \operatorname{Br} \Rightarrow O(10^{-13})$   $\delta_{21}^L \Rightarrow 10^{-4}$