



MSSM 4G[📶] scenario

[Sho IWAMOTO](#) (岩本 祥)

15 Sep. 2016

Seminar @ Osaka University

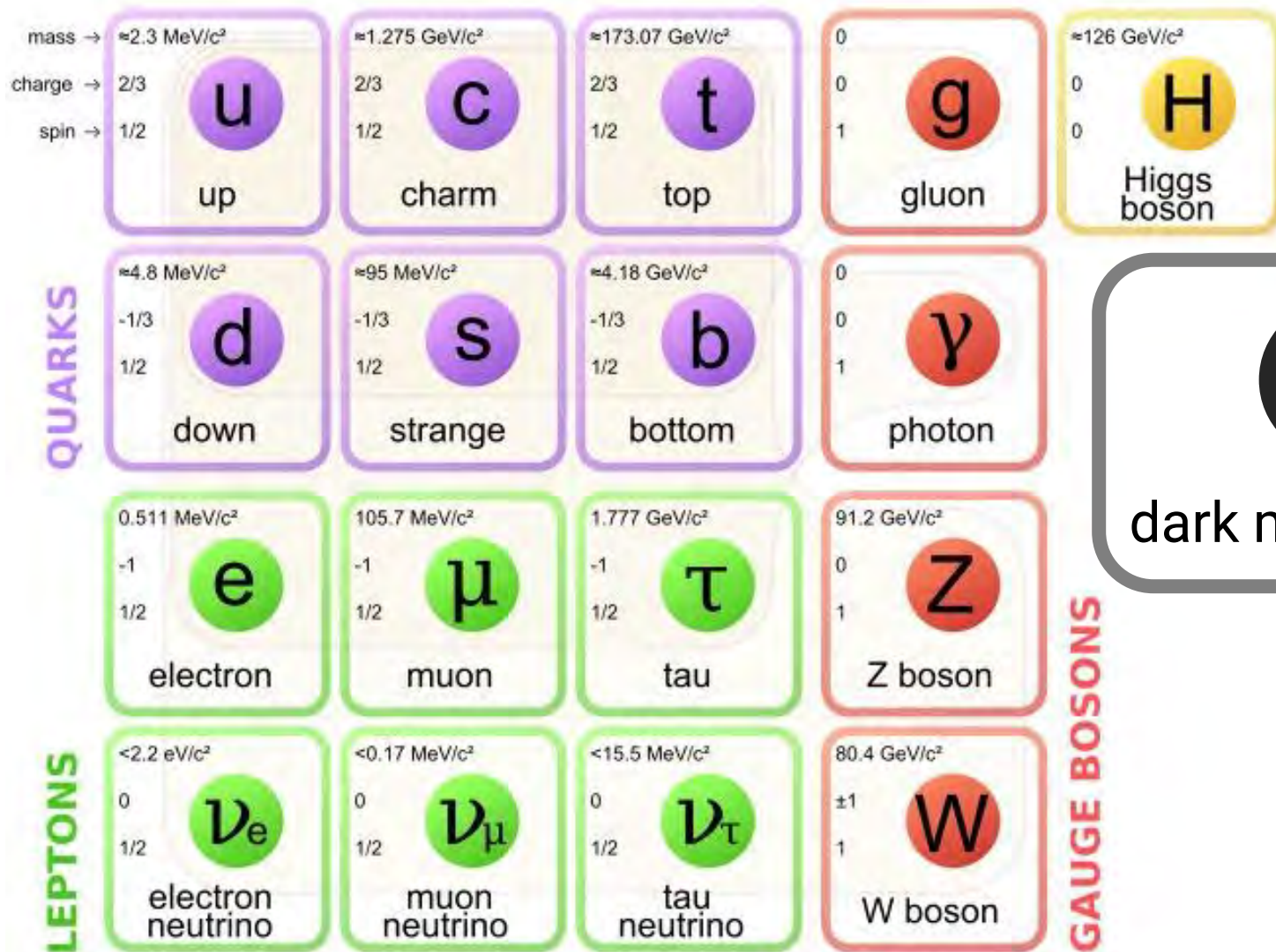
Based on [[1608.00283](#)] in collaboration with
M. Abdullah, J. L. Feng, and B. Lillard (UC Irvine)

The Standard Model of Particle Physics

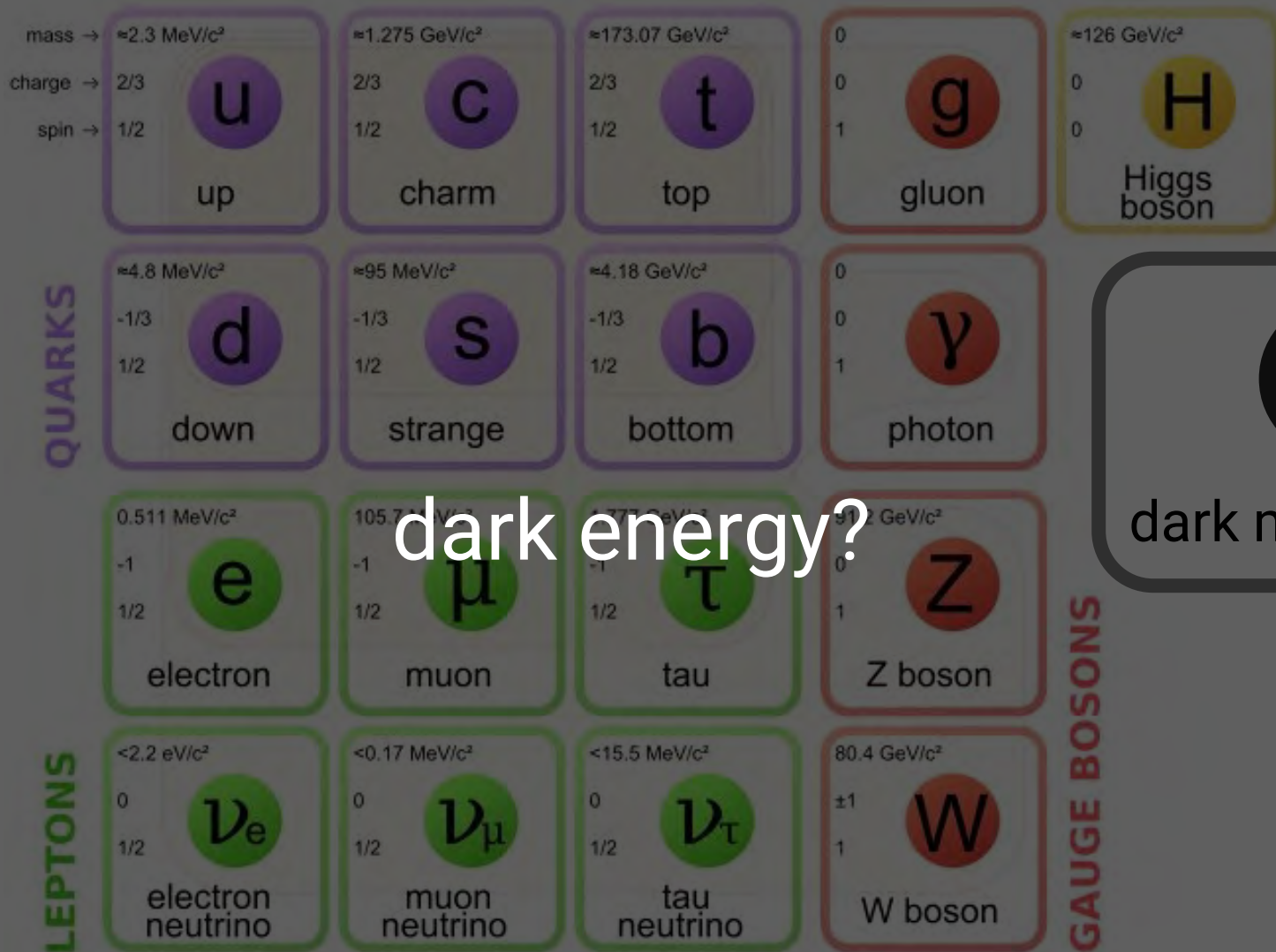
Universe =

| | | | | | |
|----------------|--|--|--|--------------------------------------|-------------------------------|
| mass → | $\approx 2.3 \text{ MeV}/c^2$ | $\approx 1.275 \text{ GeV}/c^2$ | $\approx 173.07 \text{ GeV}/c^2$ | 0 | $\approx 126 \text{ GeV}/c^2$ |
| charge → | $2/3$ | $2/3$ | $2/3$ | 0 | 0 |
| spin → | $1/2$ | $1/2$ | $1/2$ | 1 | 0 |
| | u up | c charm | t top | g gluon | H Higgs boson |
| QUARKS | $\approx 4.8 \text{ MeV}/c^2$ | $\approx 95 \text{ MeV}/c^2$ | $\approx 4.18 \text{ GeV}/c^2$ | 0 | |
| | $-1/3$ | $-1/3$ | $-1/3$ | 0 | |
| | $1/2$ | $1/2$ | $1/2$ | 1 | |
| | d down | s strange | b bottom | γ photon | |
| | $0.511 \text{ MeV}/c^2$ | $105.7 \text{ MeV}/c^2$ | $1.777 \text{ GeV}/c^2$ | $91.2 \text{ GeV}/c^2$ | |
| | -1 | -1 | -1 | 0 | |
| | $1/2$ | $1/2$ | $1/2$ | 1 | |
| | e electron | μ muon | τ tau | Z Z boson | |
| LEPTONS | $< 2.2 \text{ eV}/c^2$ | $< 0.17 \text{ MeV}/c^2$ | $< 15.5 \text{ MeV}/c^2$ | $80.4 \text{ GeV}/c^2$ | |
| | 0 | 0 | 0 | ± 1 | |
| | $1/2$ | $1/2$ | $1/2$ | 1 | |
| | ν_e electron neutrino | ν_μ muon neutrino | ν_τ tau neutrino | W W boson | |
| | | | | GAUGE BOSONS | |

Universe =



Universe =



dark energy?



Hints of “New Physics”

- Dark matter
- Dark energy
- Neutrino mass
- Gauge coupling unification
- Higgs mass (“naturalness”)
- Muon “ $g - 2$ ”
- ...

New Physics Candidates

-
-
-
-

etc...

Hints of “New Physics”

- Dark matter
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New Physics Candidates

- SUSY [supersymmetry]
 -
 -
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- etc...

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New Physics Candidates

- SUSY [supersymmetry]



Please fill this list
with your models
/ models you like



etc...

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New Physics Candidates

- SUSY [supersymmetry]
- Gauge-Higgs unification
- Hidden strong $SU(N)$
- etc...

Hints of “New Physics”

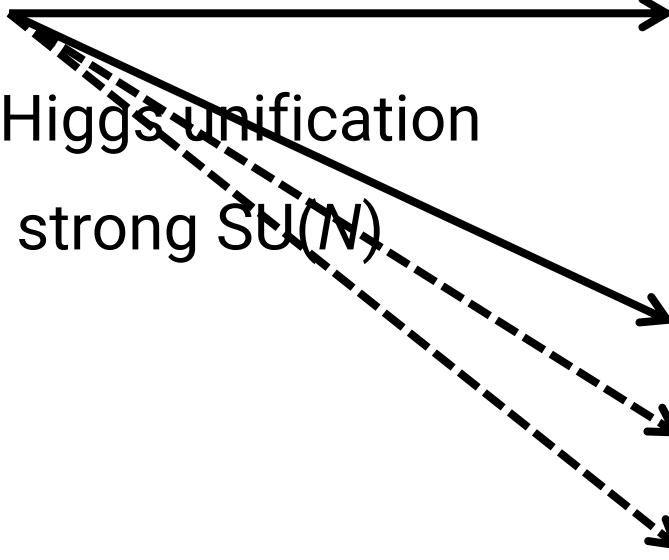
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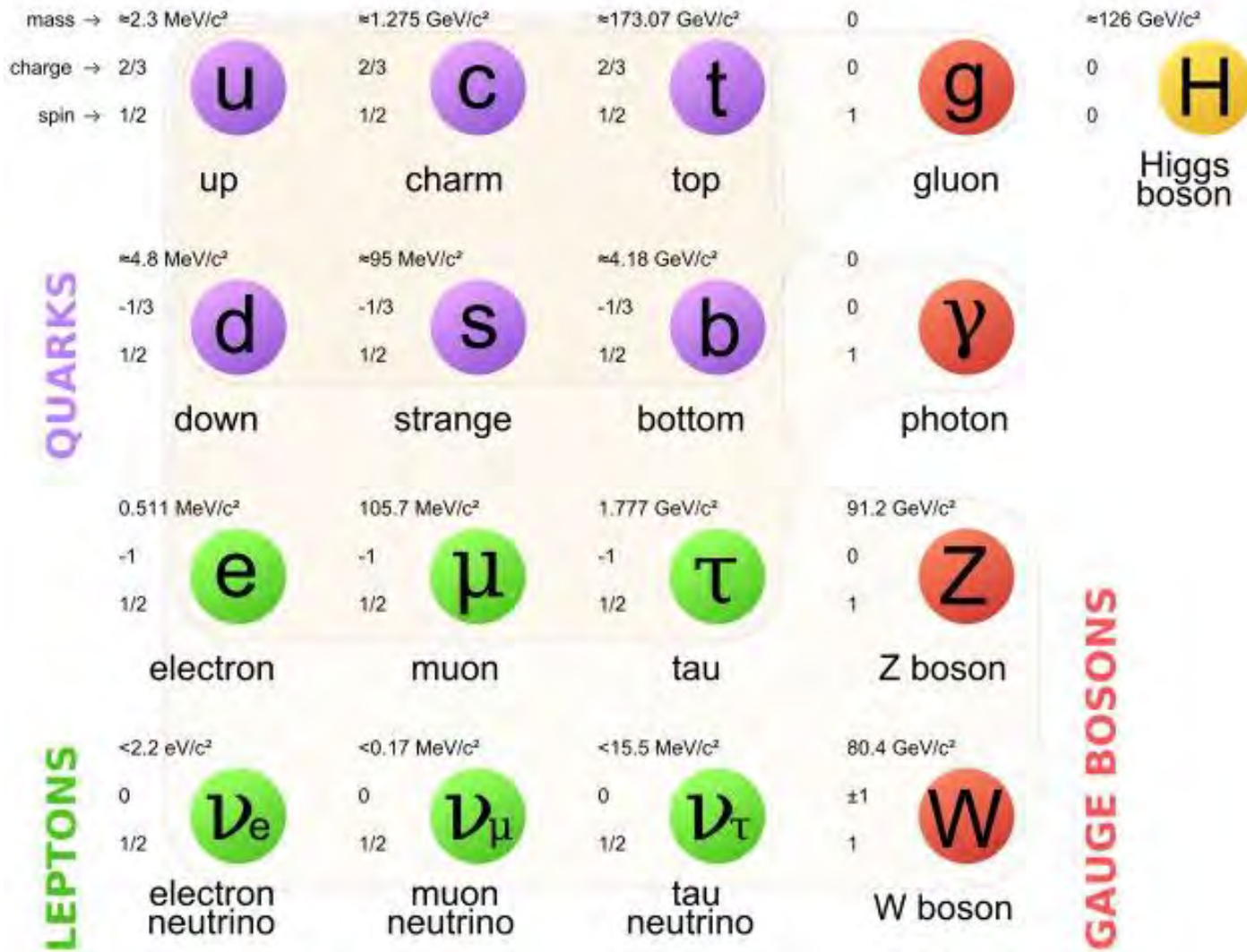
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■ SM =



■ MSSM =

[Minimal Supersymmetric Standard Model]

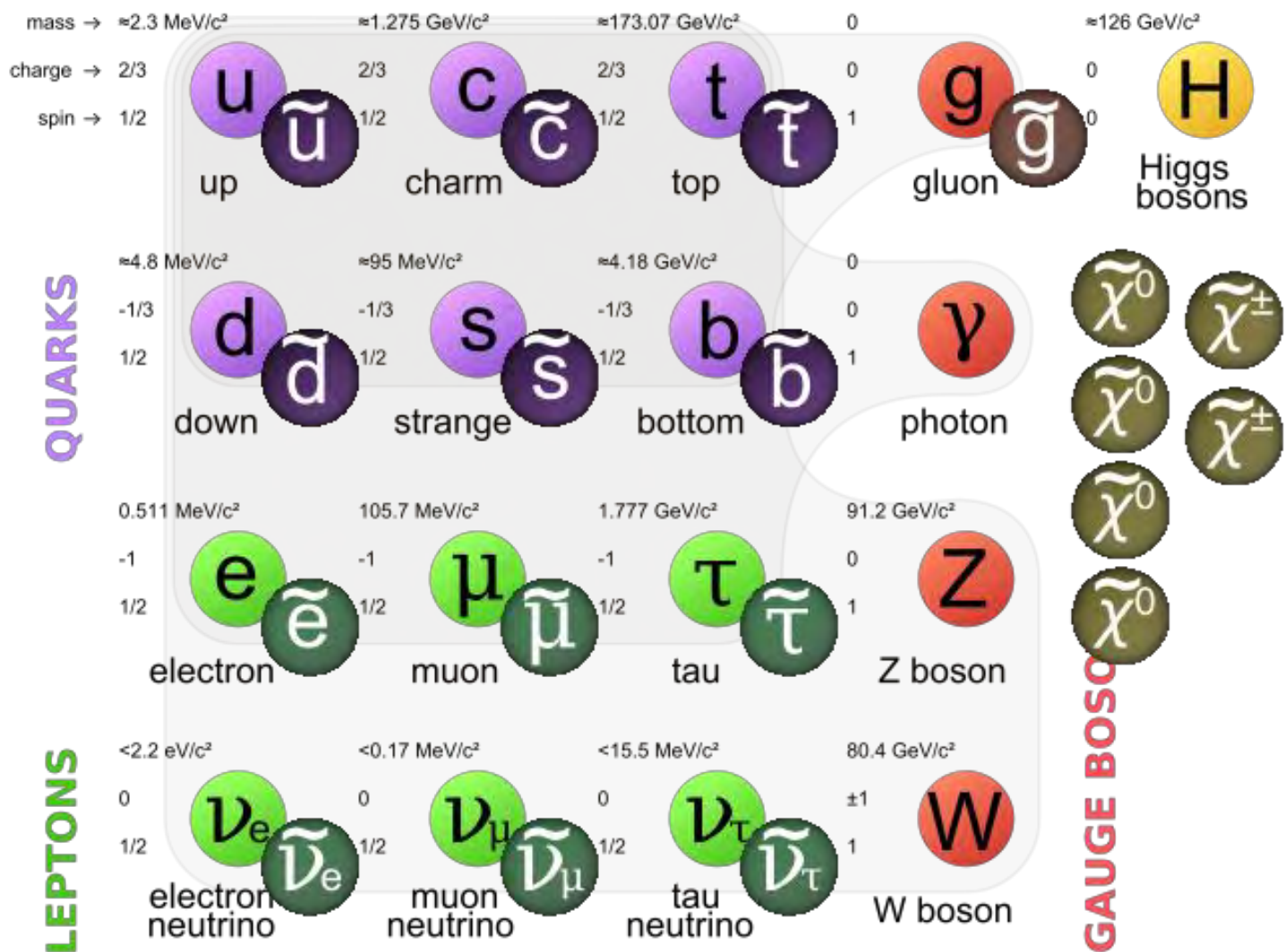


Image by [MissBJ](#) [CC BY 3.0], via [Wikimedia Commons](#) (changes were made by S.I.)

New Physics Candidates

■ SUSY

Hints of “New Physics”

■ Dark matter

■ Dark energy

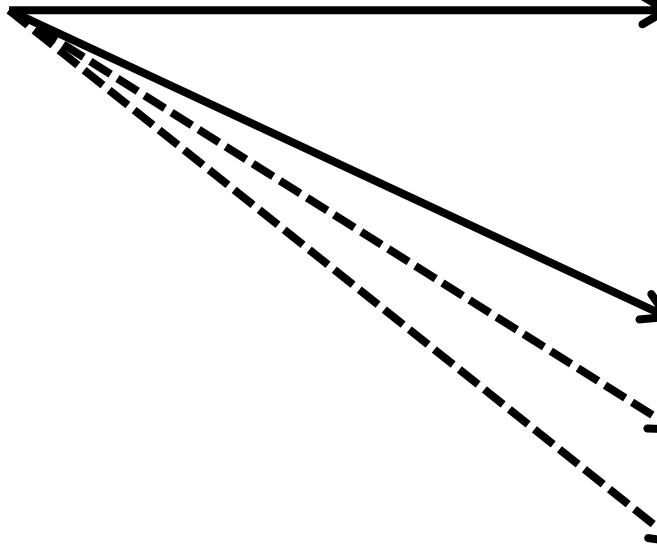
■ Neutrino mass

■ Gauge coupling unification

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■ Muon “ $g - 2$ ”

■ ...



New Physics Candidates

■ SUSY

Hints of “New Physics”

■ Dark matter

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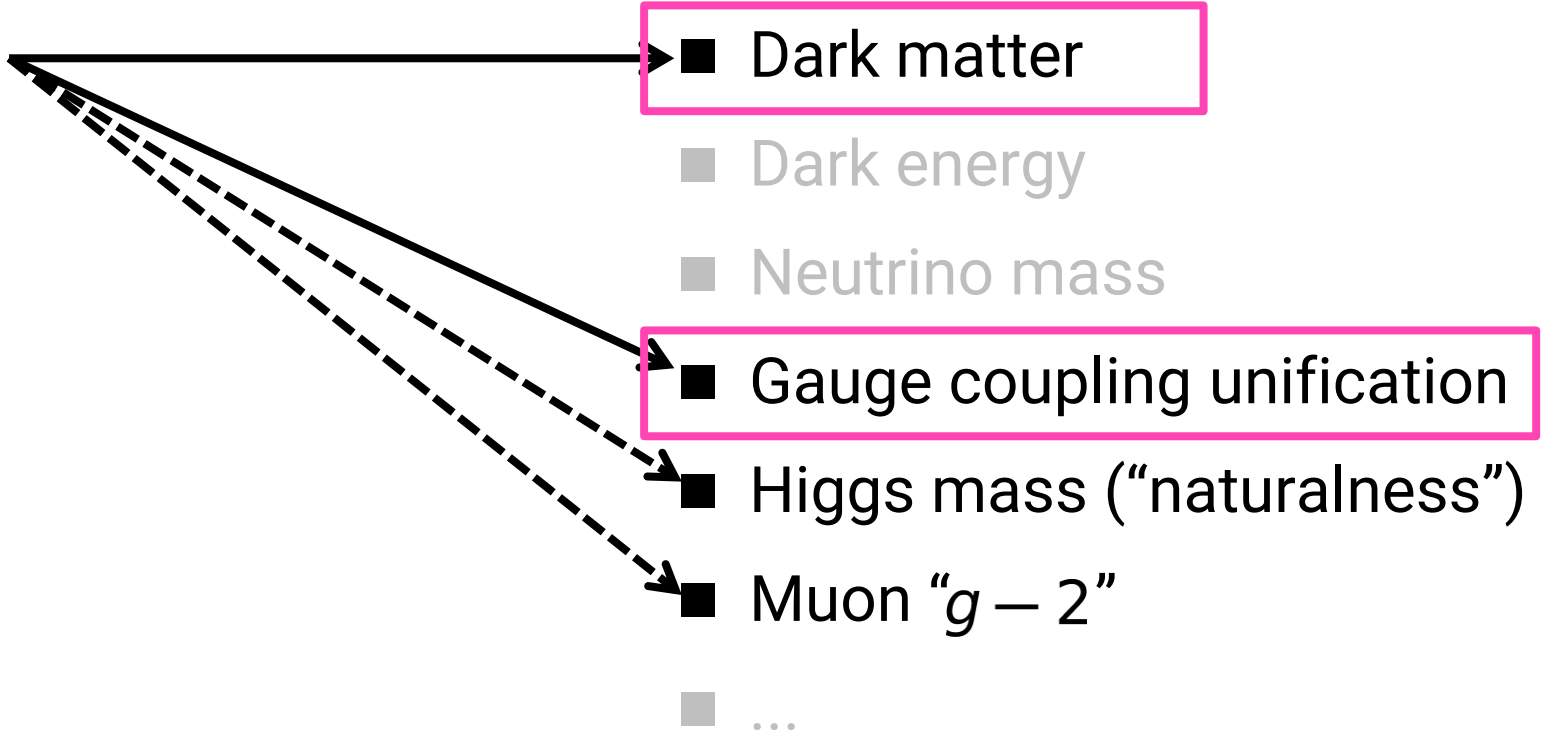
■ Neutrino mass

■ Gauge coupling unification

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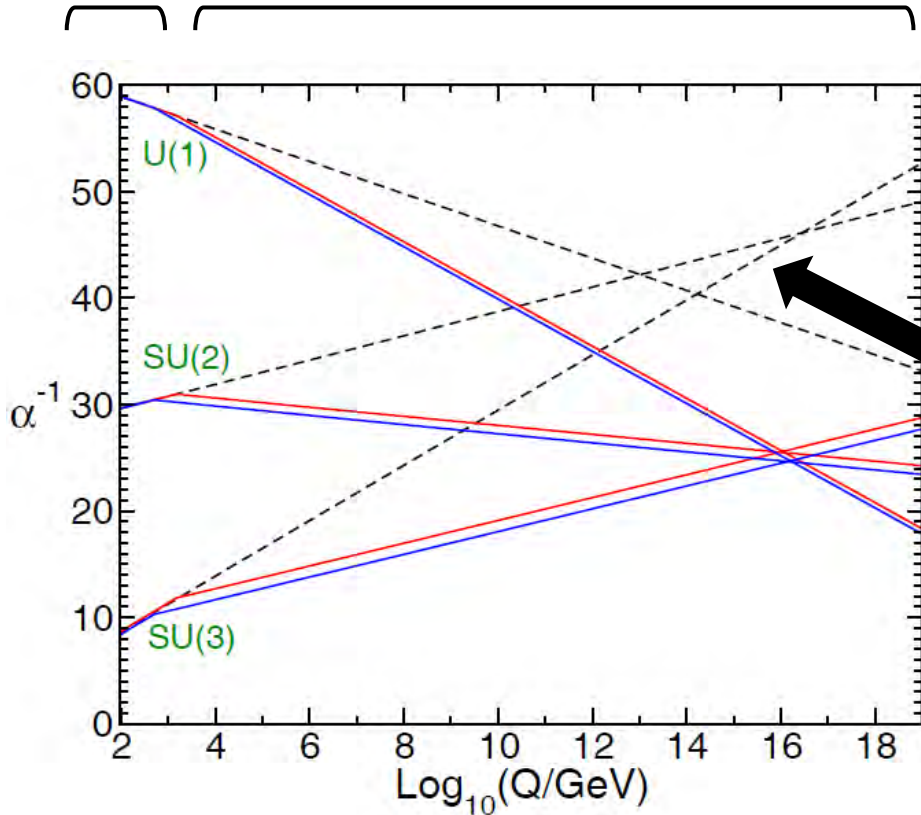
■ ...



Gauge coupling unification

- SM \ni 3 forces : U(1), SU(2), SU(3) [Why three?]

measured theoretical prediction



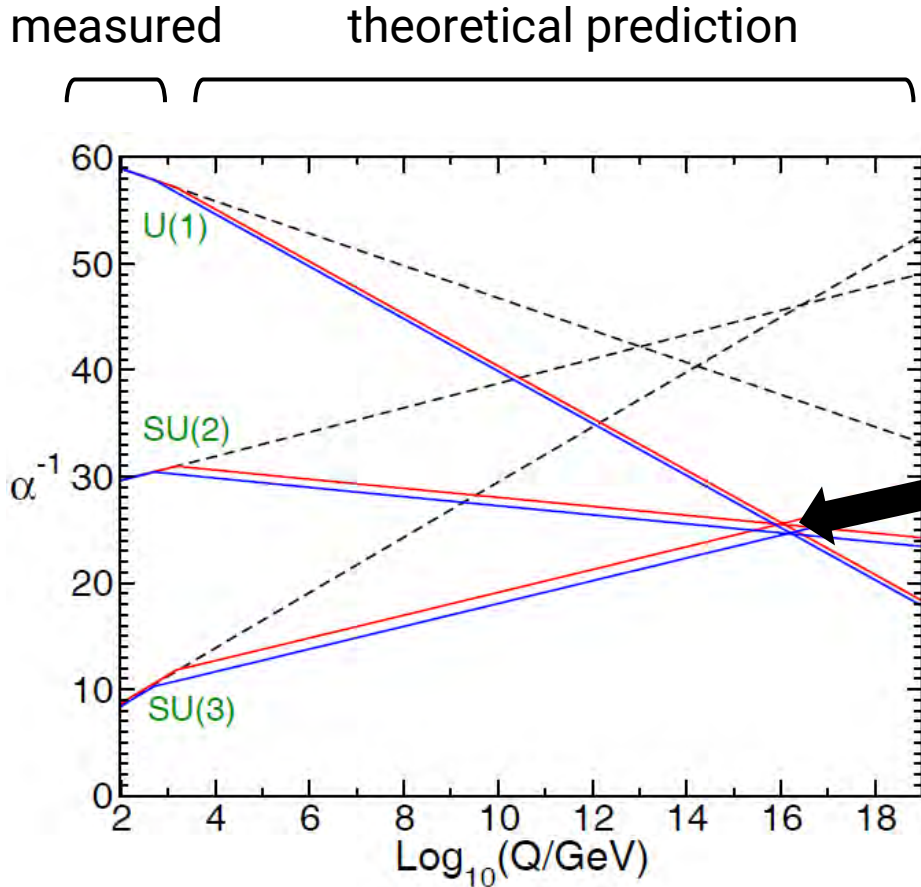
Gauge coupling unification

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| | 1/2 | 1/2 | 1/2 | 1 | 1 |
| | ν_e electron neutrino | ν_μ muon neutrino | ν_τ tau neutrino | W W boson | |
| | | | | | GAUGE BOSONS |

Figure from S. P. Martin, *A Supersymmetry Primer*, hep-ph/9709356

Gauge coupling unification

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Gauge coupling unification

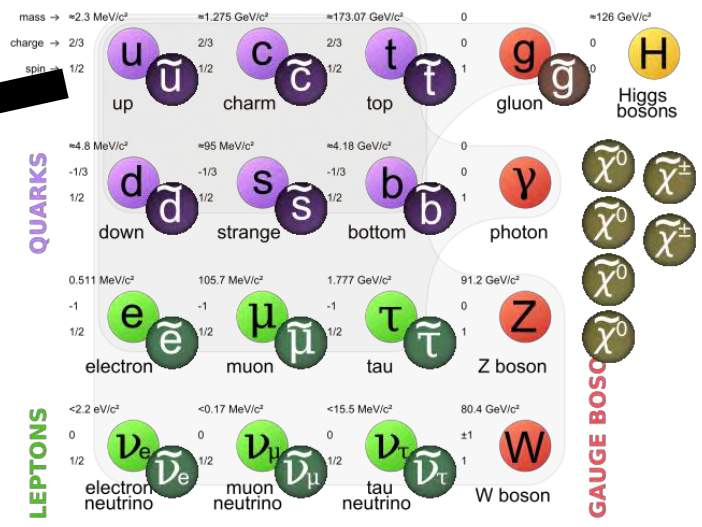


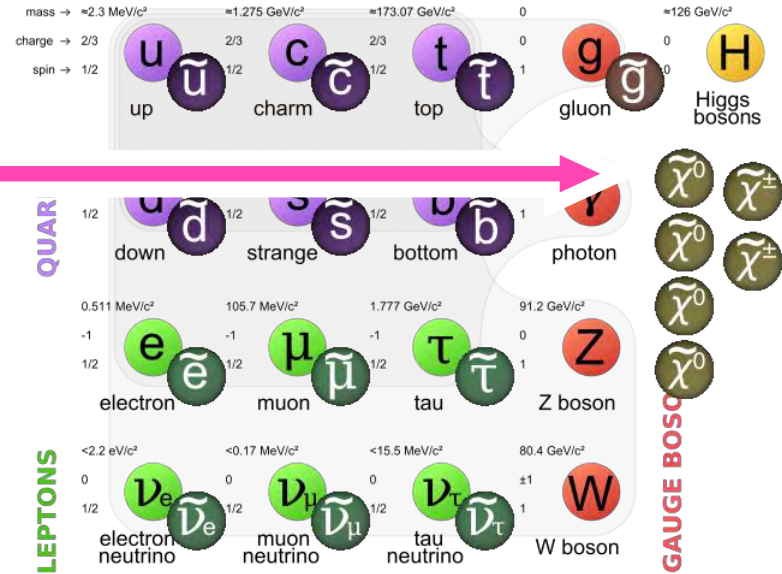
Figure from S. P. Martin, *A Supersymmetry Primer*, hep-ph/9709356

■ MSSM \ni Dark matter candidate



■ Dark matter?

- stable (at least 10^{10} yr)
- charge neutral
- density $\Omega h^2 = 0.12$
- not detected by astrophysics / direct search / LHC



■ MSSM \ni Dark matter candidate



■ Dark matter?

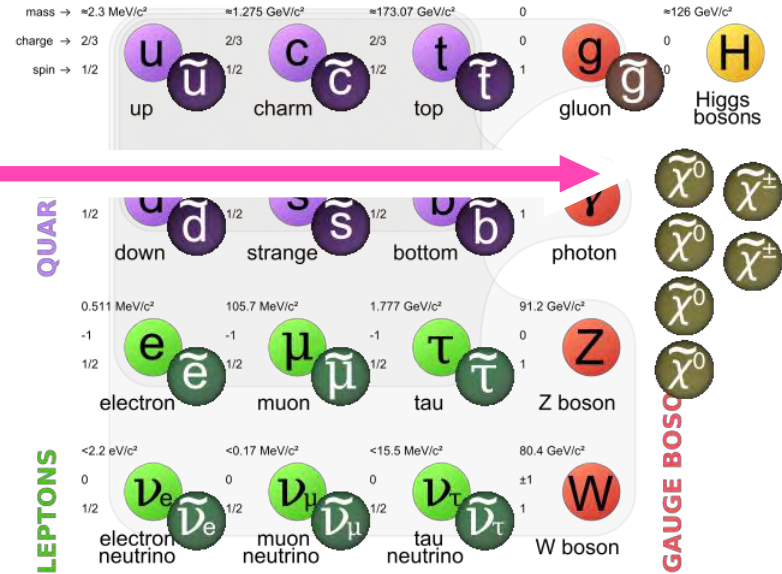
if we introduce R-parity

✓ stable (at least 10^{10} yr)

✓ charge neutral

➤ density $\Omega h^2 = 0.12$

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- MSSM \ni Dark matter candidate



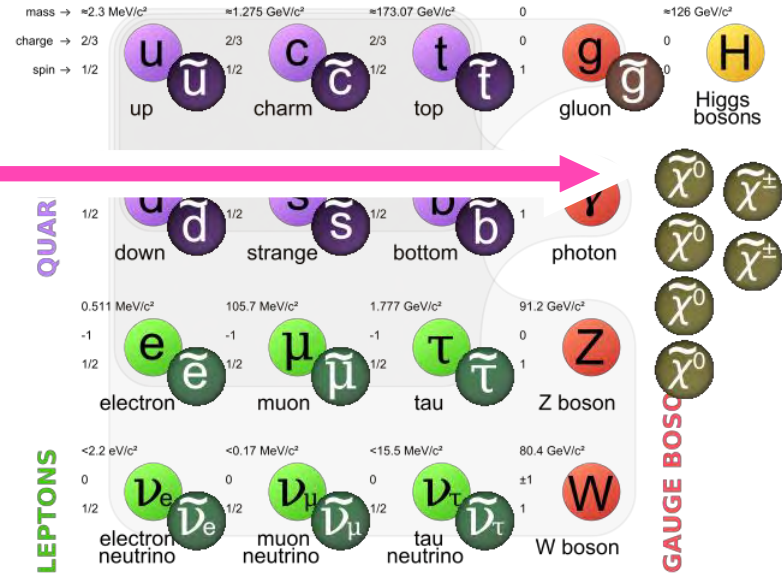
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if we introduce R-parity

- ✓ stable (at least 10^{10} yr)
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$$\tilde{\chi}^0 = \tilde{B} \oplus \tilde{W}^0 \oplus \tilde{H}_d^0 \oplus \tilde{H}_u^0$$

- \tilde{B} -like?

→ “overabundant” problem

- \tilde{W} -like?

$$\Omega h^2 \gg 0.12$$

- \tilde{H} -like?

$$\tilde{\chi}^0 = \tilde{B} \oplus \tilde{W}^0 \oplus \tilde{H}_d^0 \oplus \tilde{H}_u^0$$

• \tilde{B} -like?

→ “overabundant” problem

• \tilde{W} -like?

$h^2 \sim 0.12$

• \tilde{H} -like?

MSSM 4G³ model

solves this problem!

Introduction: why overabundant?

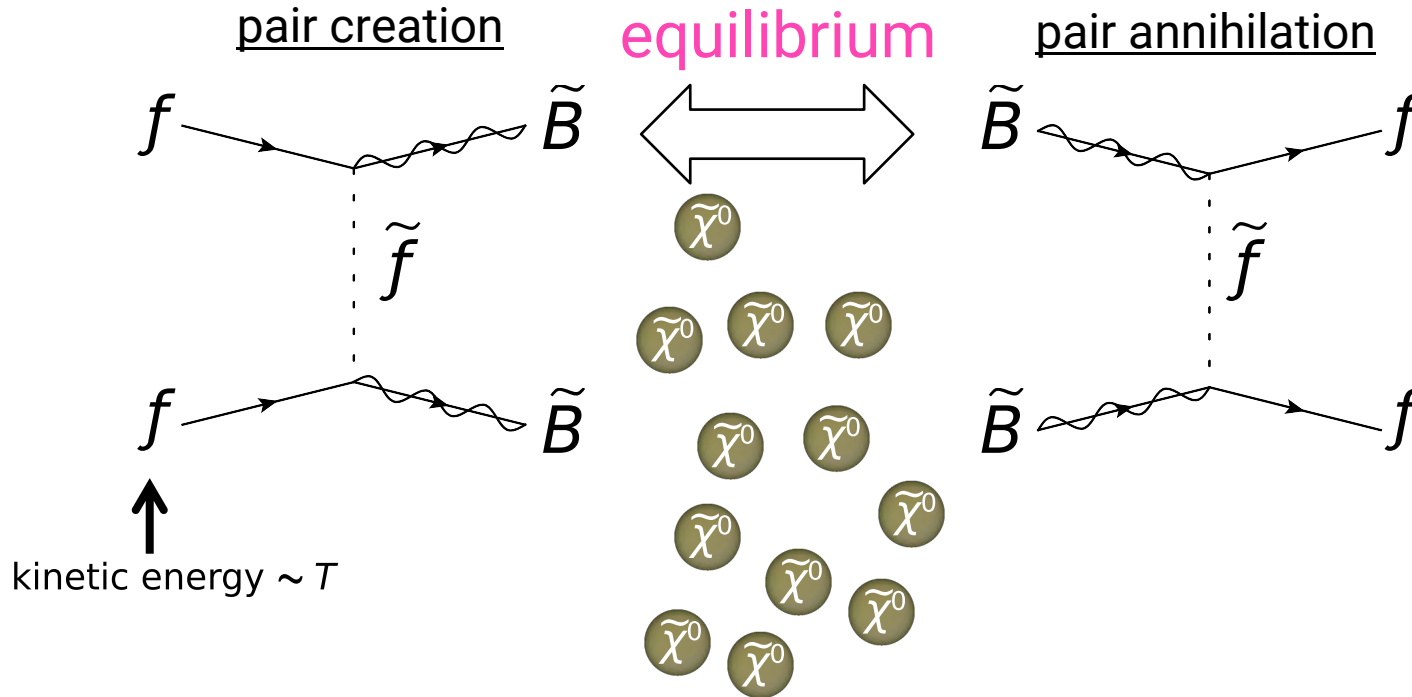
Model: **MSSM4G**  solves overabundance.

Analysis:

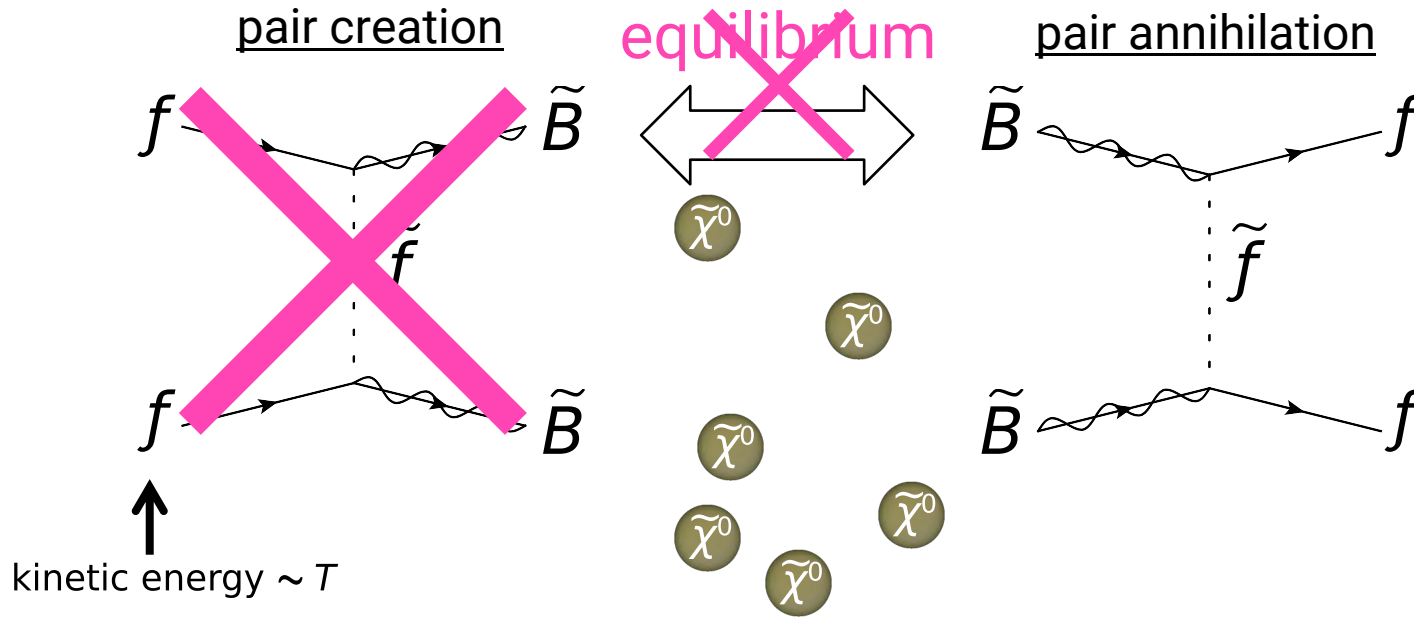
- cosmic rays (CTA, Fermi, MAGIC)
- colliders (LHC)
- direct detection (LUX)

Summary with discussion seeds

■ Early Universe with $T > m_{\tilde{B}}$



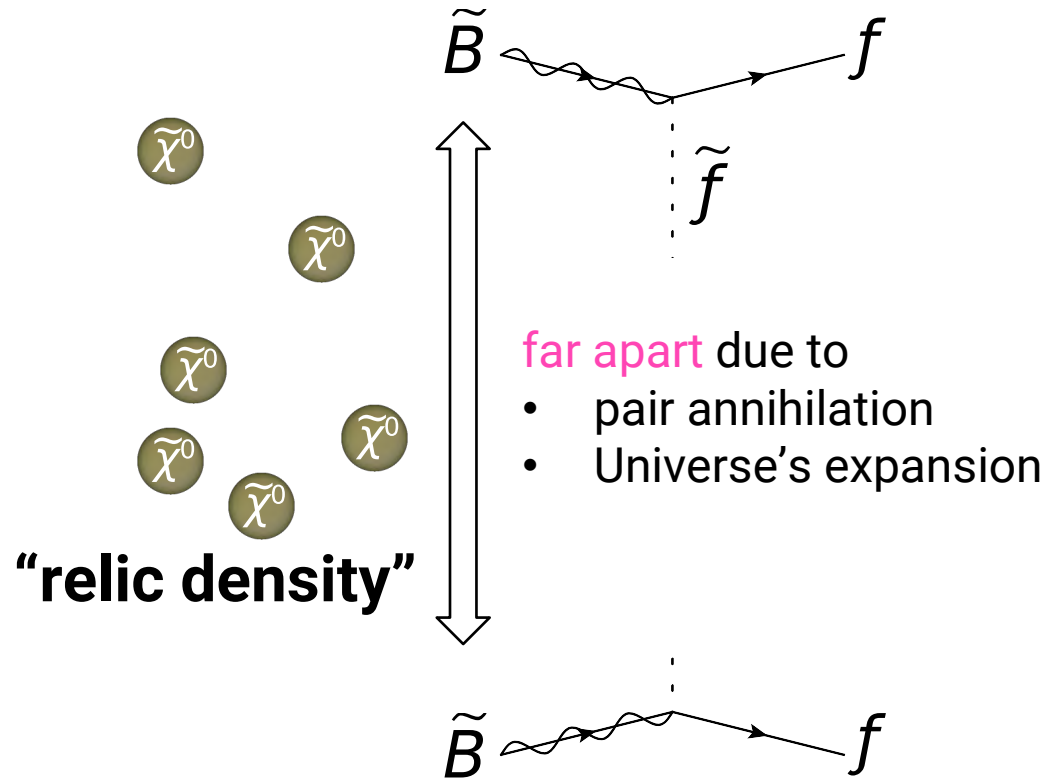
■ Early Universe with $T \lesssim m_{\tilde{B}}$



■ Early Universe with $T \lesssim m_{\tilde{B}}/20$

pair creation

pair annihilation



■ “observed” relic density Ωh^2

← “proper” crosssection $\langle \sigma v \rangle$ of $(DM)(DM) \rightarrow SM$

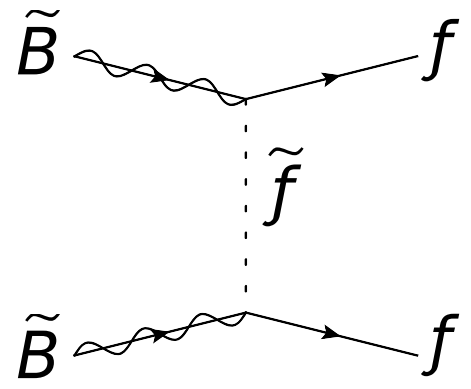
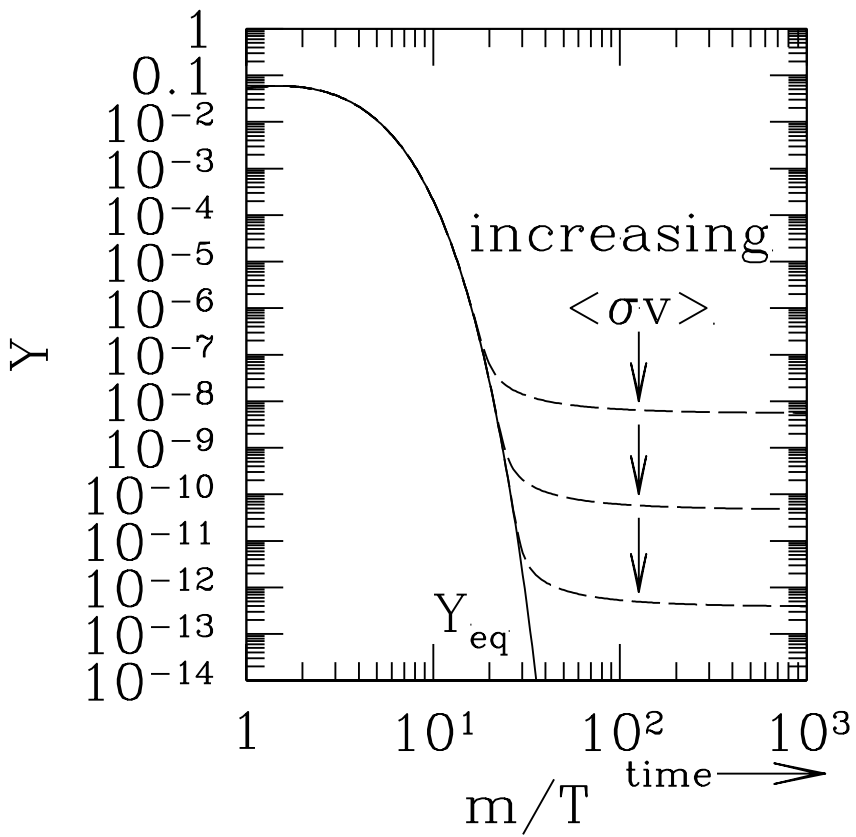


Figure from Gelmini and Gondolo, [1009.3690](https://arxiv.org/abs/1009.3690)

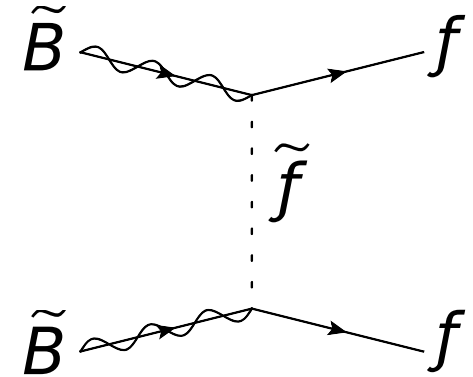
- “observed” relic density Ωh^2

← “proper” crosssection $\langle \sigma v \rangle$ of $(\text{DM})(\text{DM}) \rightarrow \text{SM}$

- pure \tilde{B} -DM (i.e., LSP $\tilde{\chi}^0$ is \tilde{B} -like)

➤ $\langle \sigma v \rangle$ strongly depends on $m_{\tilde{f}}$

↳ $m_{\tilde{f}} \sim 100 \text{ GeV}$

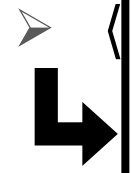


$m_{\tilde{f}} \gg 100 \text{ GeV} \implies \langle \sigma v \rangle$ too small

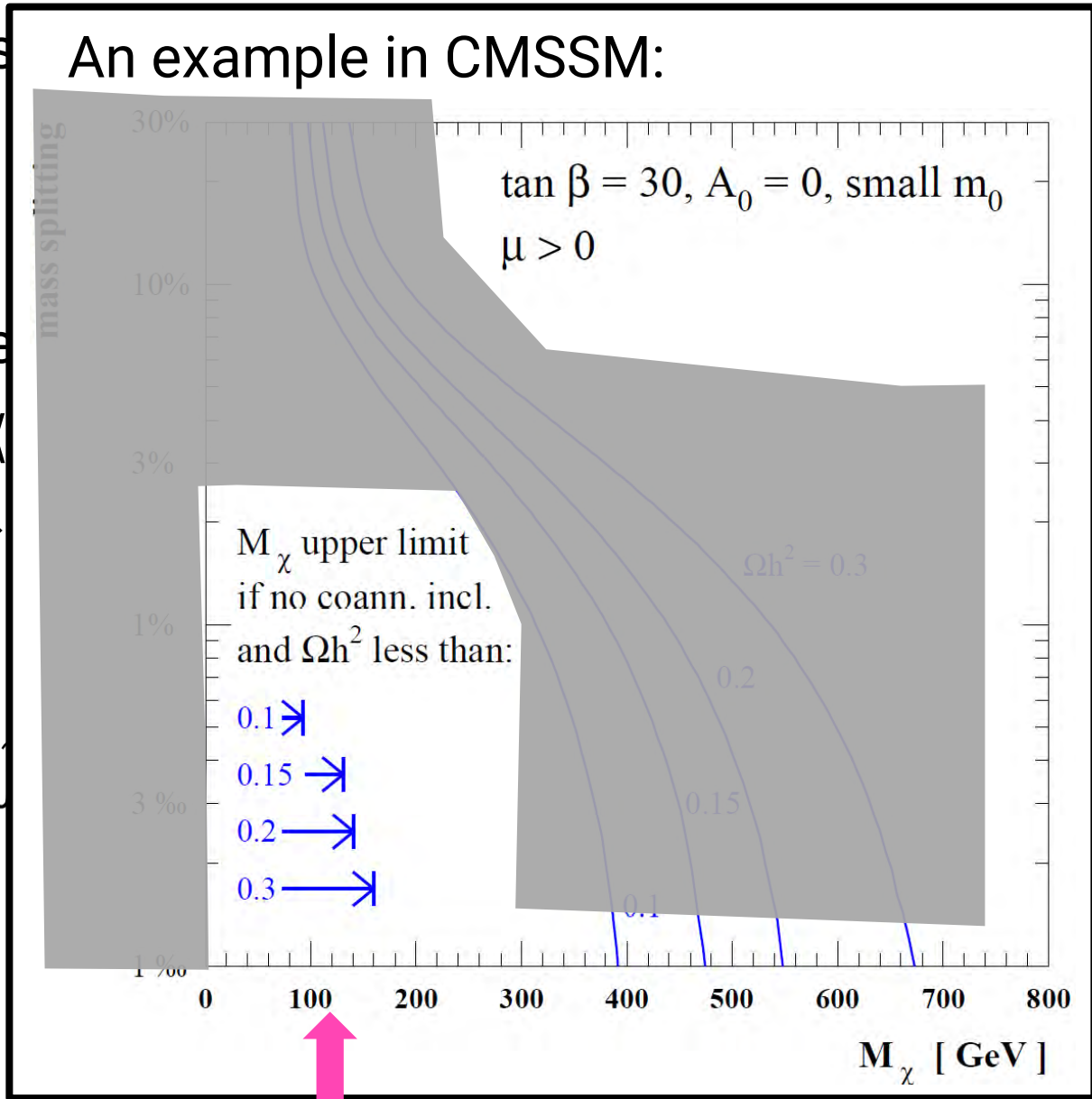
\implies “overabundant” problem

■ “obs

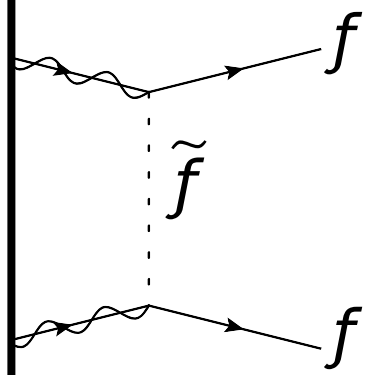
■ pure



$m_{\tilde{f}}$



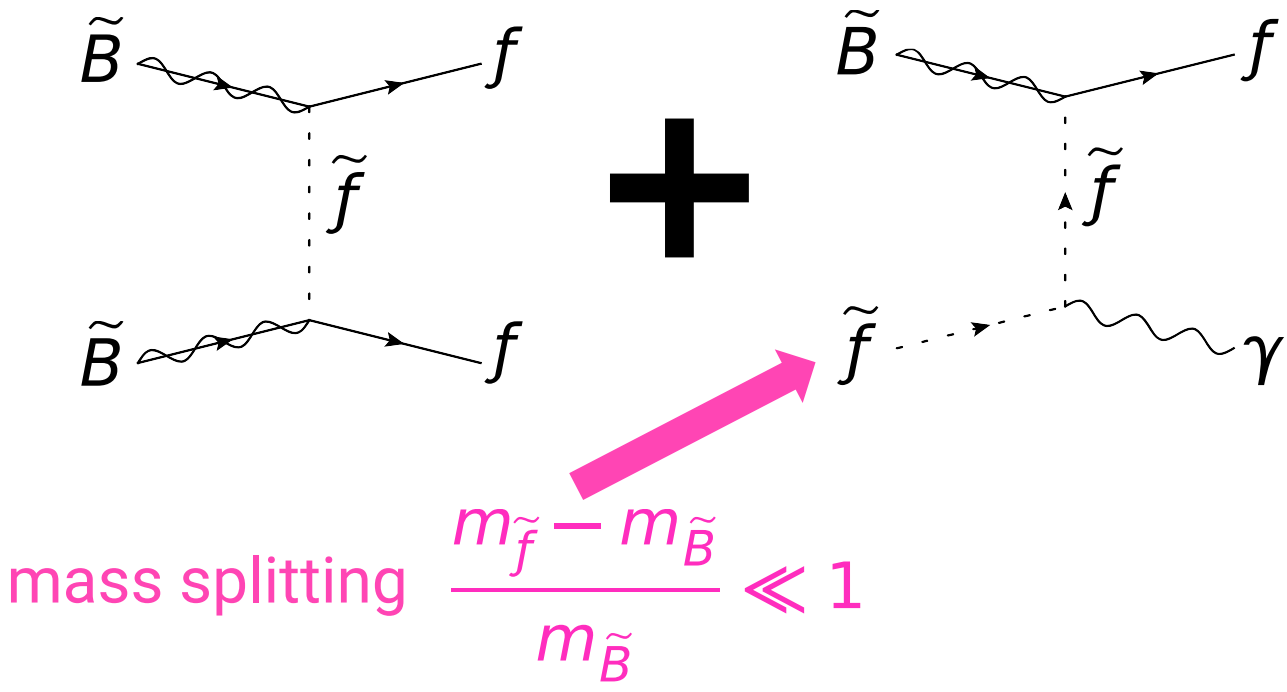
$\tilde{f} \rightarrow f + f$



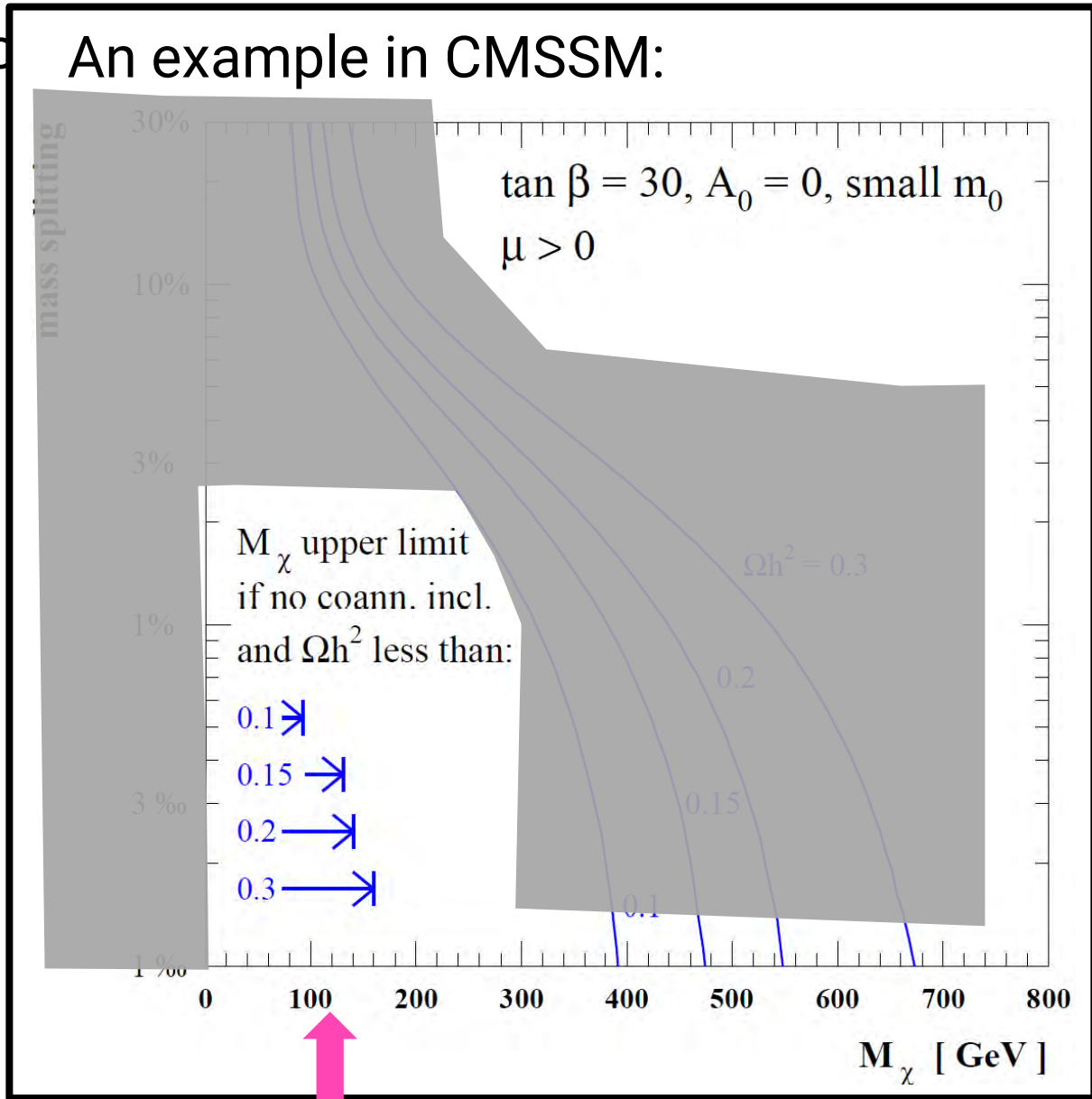
problem

Figure from Edsjö, Schelke, Ullio, Gondolo, hep-ph/0301106

- An old solution to increase $\langle \sigma v \rangle$: “co-annihilation”



■ An example in CMSSM:



on"

f

γ

Figure from Edsjö, Schelke, Ullio, Gondolo, hep-ph/0301106

■ An example in CMSSM with $\tilde{\tau}$ -coann.: "on"

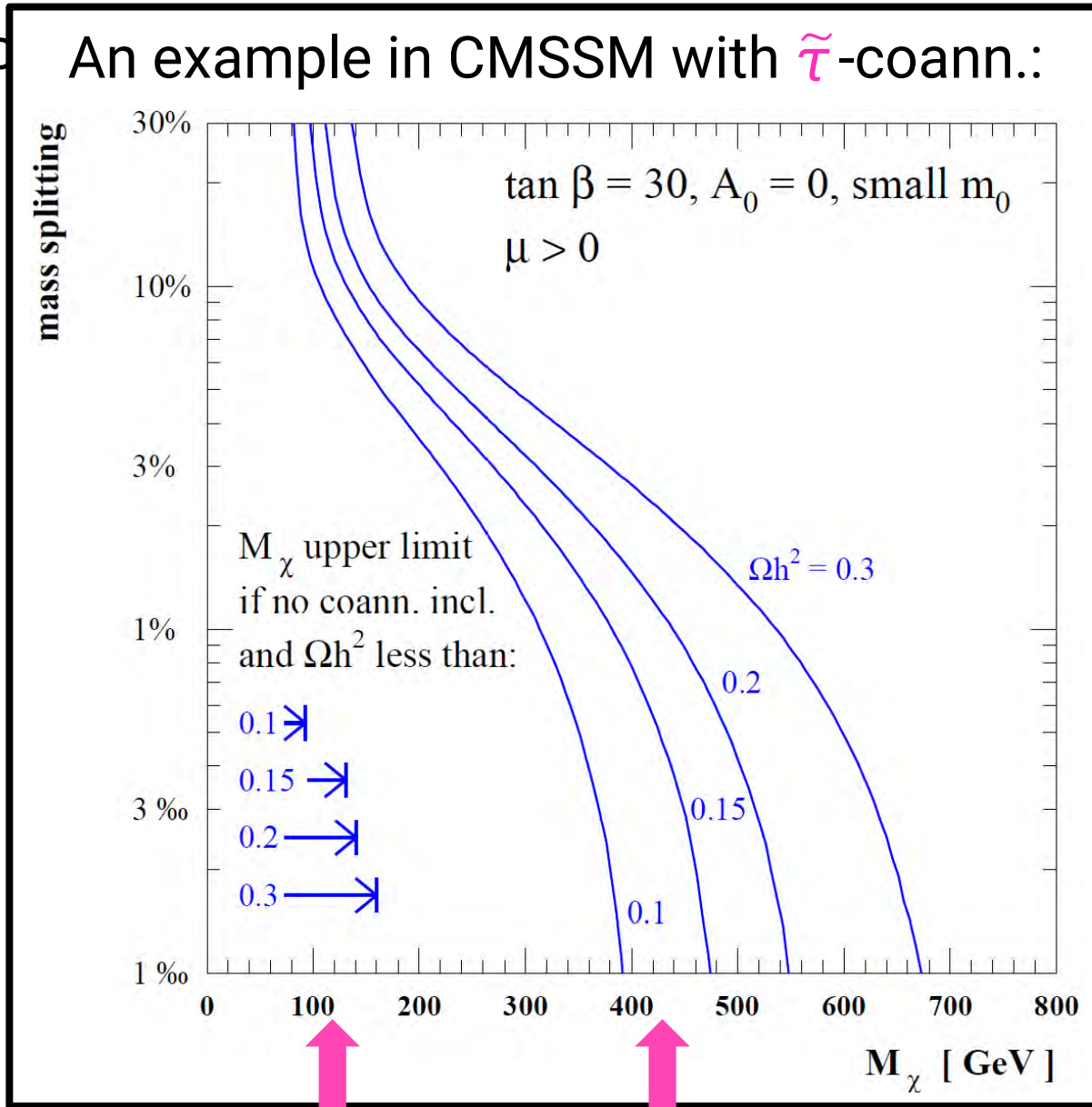


Figure from Edlö, Schelke, Ullio, Gondolo, hep-ph/0301106

Introduction: why overabundant?

Model: **MSSM4G**  solves overabundance.

Analysis:

- cosmic rays (CTA, Fermi, MAGIC)
- colliders (LHC)
- direct detection (LUX)

Summary with discussion seeds

■ MSSM = 3Generations

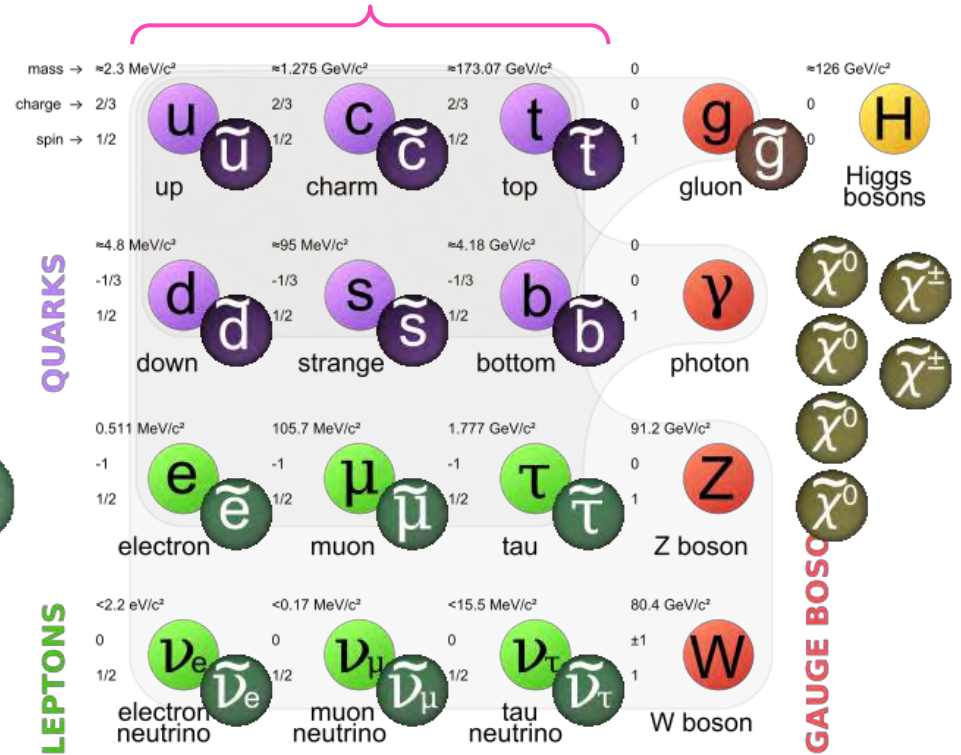


extra vector-like

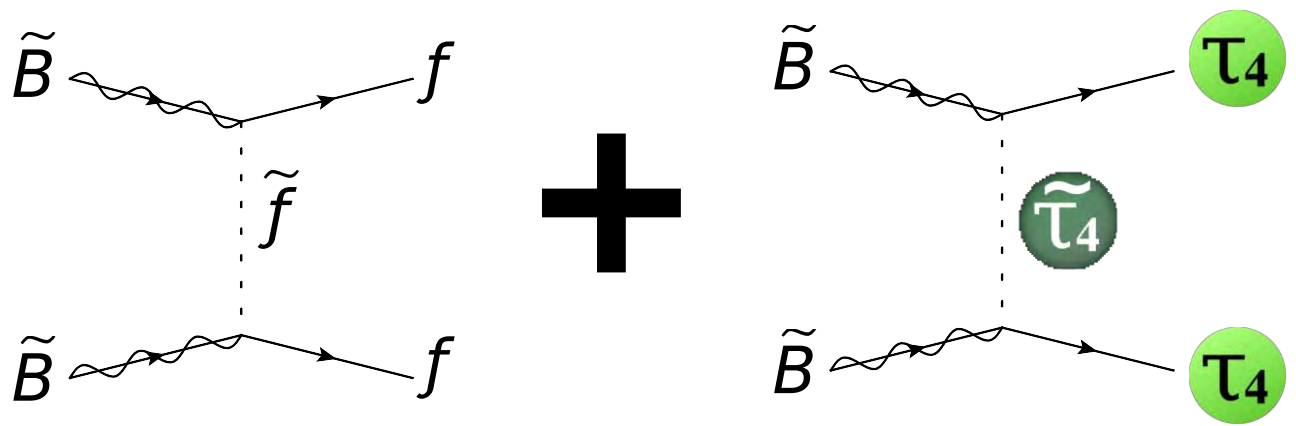
4th-Generation lepton



MSSM4G



- A new solution to increase $\langle \sigma v \rangle$: MSSM4G



extra annihilation channel

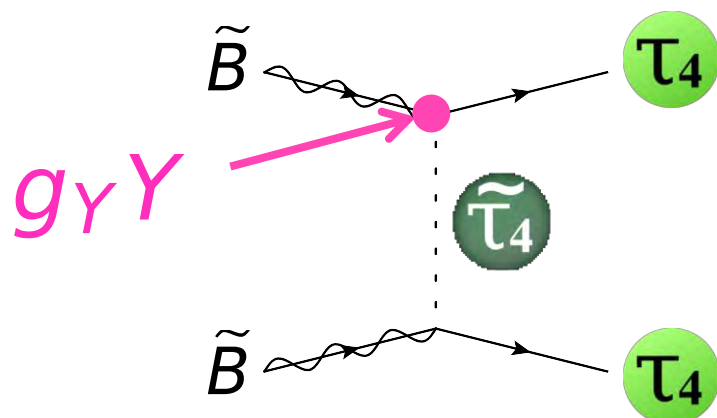
- larger Ωh^2
- “proper” $\langle \sigma v \rangle$

if $\tilde{\tau}_4 \gtrsim \tilde{B} > \tau_4$

$$(Q_i, \bar{U}_i, \bar{D}_i, L_i, \bar{E}_i) + (H_u, H_d) \quad [\text{MSSM}]$$

$(i = 1 \dots 3)$

$$+ (E_4, \bar{E}_4) \quad [\text{MSSM4G}]$$



$$\Rightarrow \langle \sigma \nu \rangle \propto Y^4$$

| | $SU(3)_{\text{color}}$ | $SU(2)_{\text{weak}}$ | $U(1)_Y$ |
|-------------|------------------------|-----------------------|----------|
| Q_i | 3 | 2 | 1/6 |
| \bar{U}_i | $\bar{3}$ | 1 | -2/3 |
| \bar{E}_i | 1 | 1 | 1 |
| \bar{D}_i | $\bar{3}$ | 1 | 1/3 |
| L_i | 1 | 2 | -1/2 |
| H_u | 1 | 2 | 1/2 |
| H_d | 1 | 2 | -1/2 |
| \bar{E}_4 | 1 | 1 | 1 |
| E_4 | 1 | 1 | -1 |

$$W = Y_u H_u Q \bar{U} + Y_d H_d Q \bar{D} + Y_e H_d L \bar{E}$$

$$+ M_{E_4} E_4 \bar{E}_4 + \epsilon_i H_d L_i \bar{E}_4$$

[vector-like mass]

[mixing with SM leptons]

■ MSSM + $E\bar{E}$ → breaks coupling unification

■ QUE model : MSSM + $Q\bar{Q}U\bar{U}E\bar{E}$

✓ gauge coupling unification

✓ SU(5) GUT

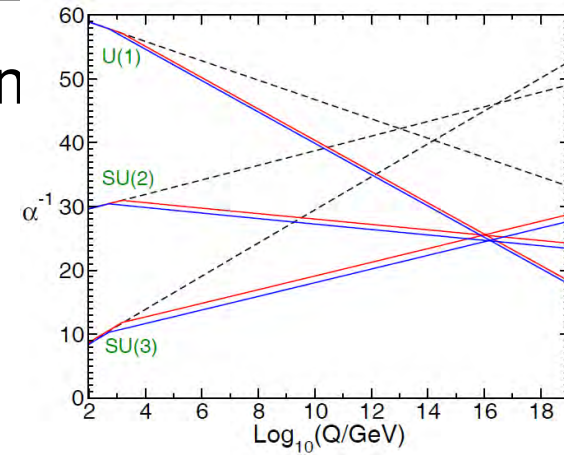
➤ extra $H_u Q_4 \bar{U}_4$ interaction → m_h **UP**

■ QDEE model : MSSM + $Q\bar{Q}D\bar{D}E\bar{E}E\bar{E}$

✓ gauge coupling unification

✗ SU(5) GUT

➤ extra $H_d Q_4 \bar{D}_4$ coupling → m_h slightly **UP**



■ MSSM + $E\bar{E}$ → breaks coupling unification

■ QUE model : MSSM + $Q\bar{Q}U\bar{U}E\bar{E}$

⇒ MSSM + $T_4, B_4, t_4, \tau_4,$

$\tilde{T}_{4L}, \tilde{T}_{4R}, \tilde{B}_{4L}, \tilde{B}_{4R}, \tilde{t}_{4L}, \tilde{t}_{4R}, \tilde{\tau}_{4L}, \tilde{\tau}_{4R}$

■ QDEE model : MSSM + $Q\bar{Q}D\bar{D}E\bar{E}E\bar{E}$

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assumed to be “decoupled” (very heavy)
and we will ignore them.

■ QDEE model : MSSM + $Q\bar{Q}D\bar{D}E\bar{E}E\bar{E}$

⇒ MSSM + ~~$T_4, B_4, b_4, \tau_4, \tau_5,$~~

~~$\tilde{T}_{4L}, \tilde{T}_{4R}, \tilde{B}_{4L}, \tilde{B}_{4R}, \tilde{b}_{4L}, \tilde{b}_{4R}, \tilde{\tau}_{4L}, \tilde{\tau}_{4R}, \tilde{\tau}_{5L}, \tilde{\tau}_{5R}$~~

Other working assumptions

- $M_1 \ll \mu \ll M_2$
→ LSP $\tilde{\chi}_1^0$ is \tilde{B} -like
- All the other SUSY particles & extra Higgses are decoupled.

■ MSSM + $E\bar{E}$ → breaks coupling

■ QUE model : MSSM + $Q\bar{Q}U\bar{U}E\bar{E}$

⇒ SM + $\tilde{\chi}_1^0 (\approx \tilde{B})$, τ_4 ,
 $\underbrace{\tilde{\tau}_{4L}, \tilde{\tau}_{4R}}_{\text{assumed to be equal-mass}}$

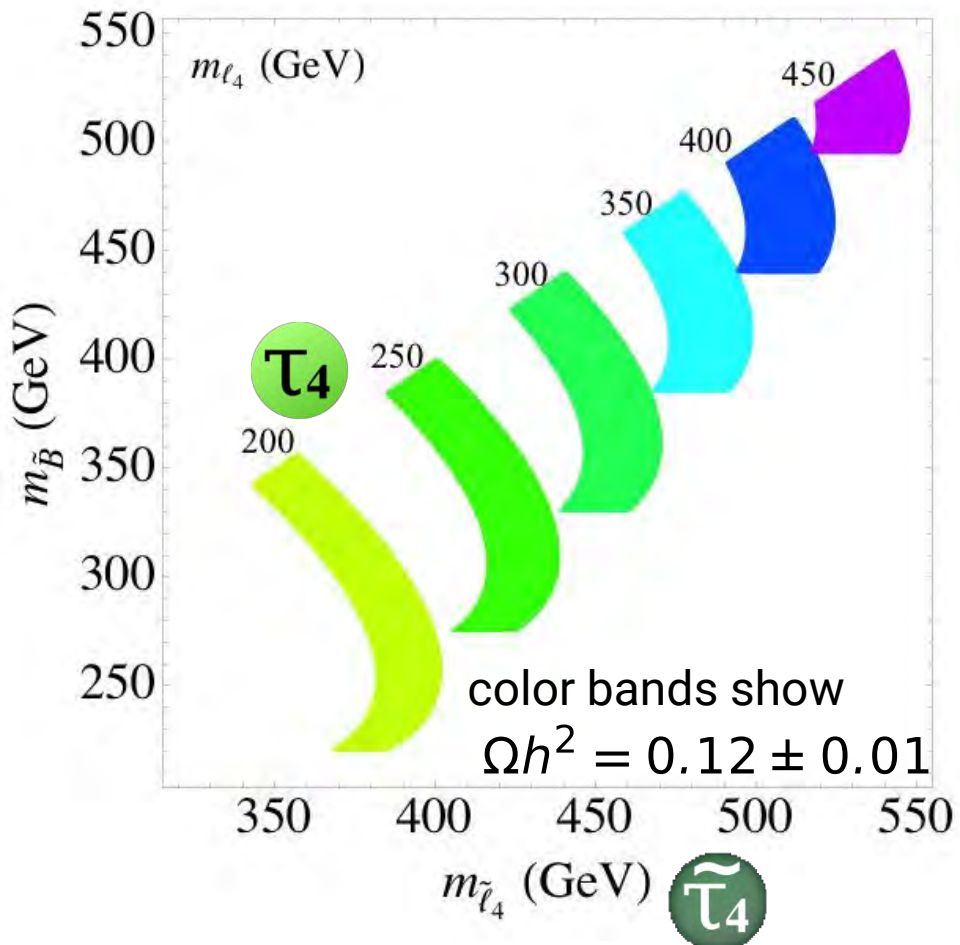
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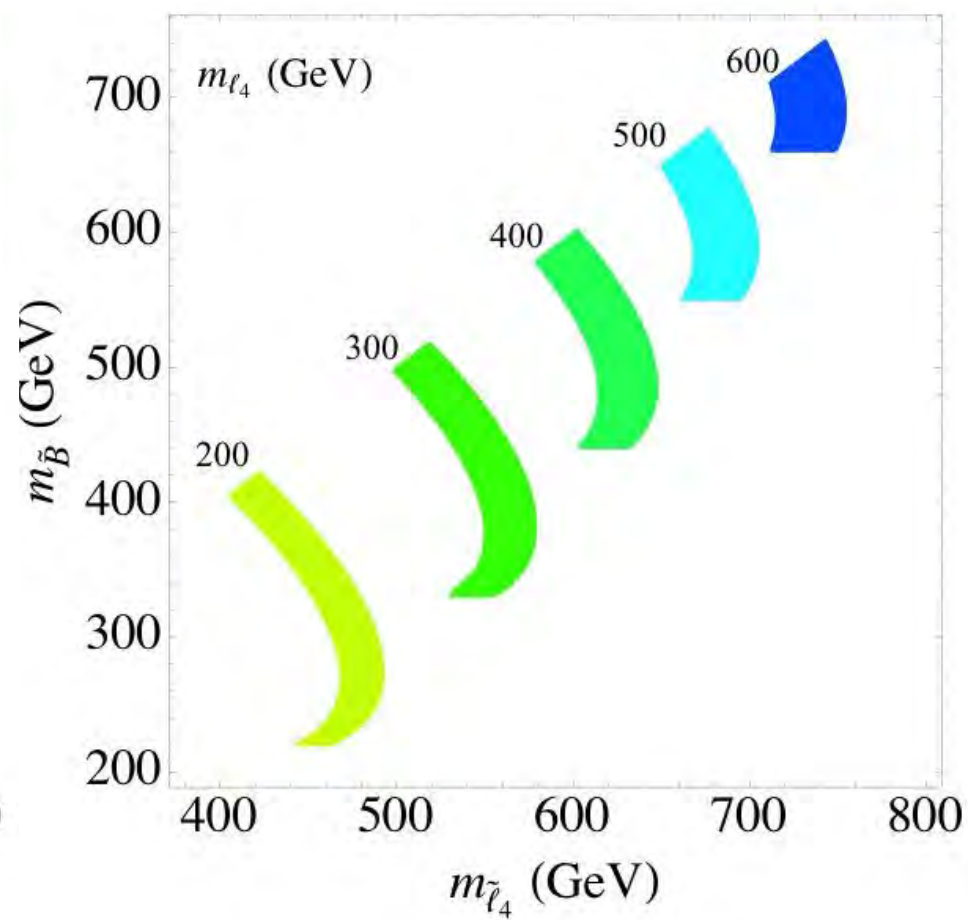
■ QDEE model : MSSM + $Q\bar{Q}D\bar{D}E\bar{E}E\bar{E}$

⇒ SM + $\tilde{\chi}_1^0 (\approx \tilde{B})$, $\underbrace{\tau_4, \tau_5}_{\text{assumed to be equal-mass}}$,
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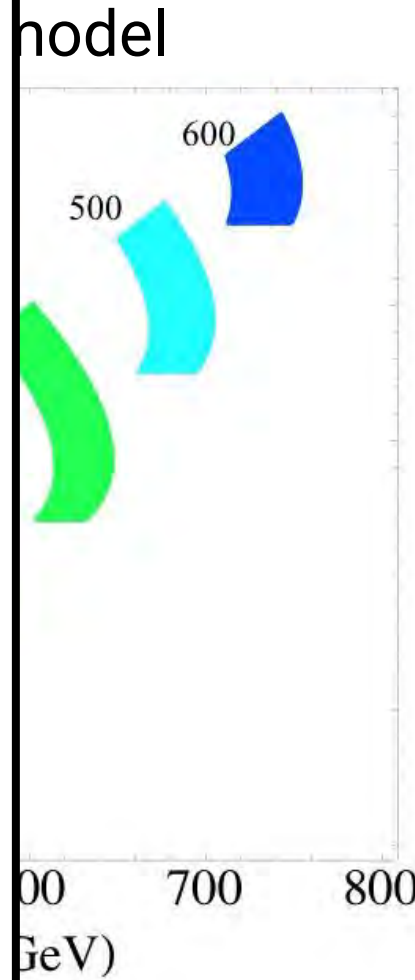
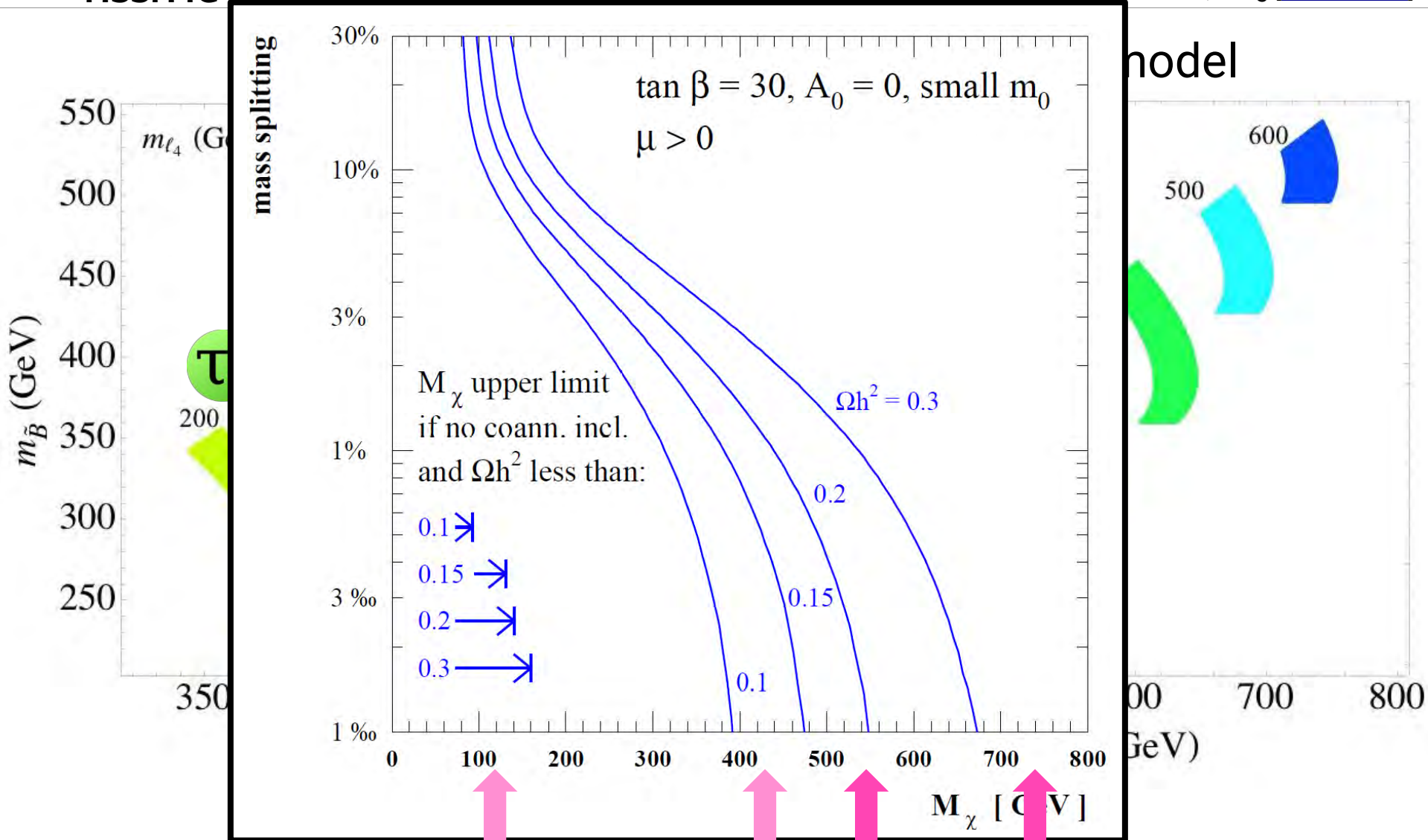
QUE model



QDEE model



$$\tilde{\tau}_4 \gtrsim \tilde{B} > \tau_4$$



$\tilde{\tau}_4 \gtrsim \tilde{B} > \tau_4$

vanilla stau-coann. QUE QDEE

Introduction: why overabundant?

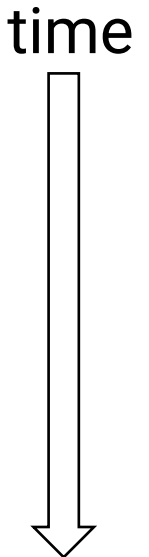
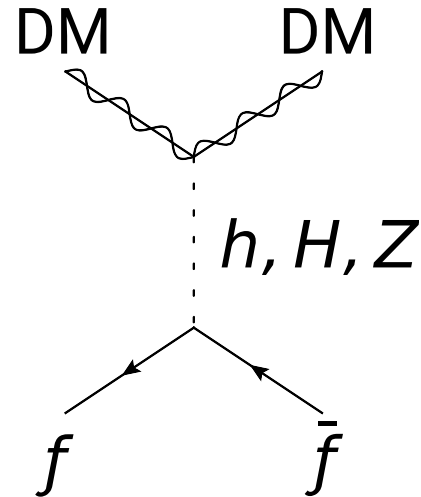
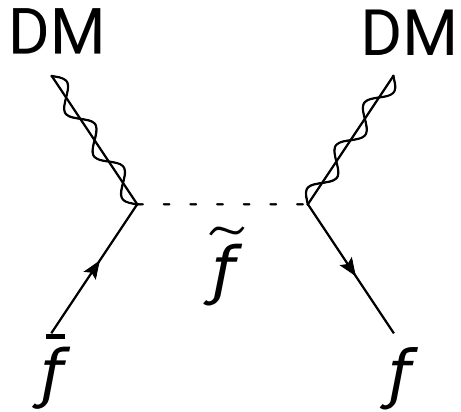
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Analysis:

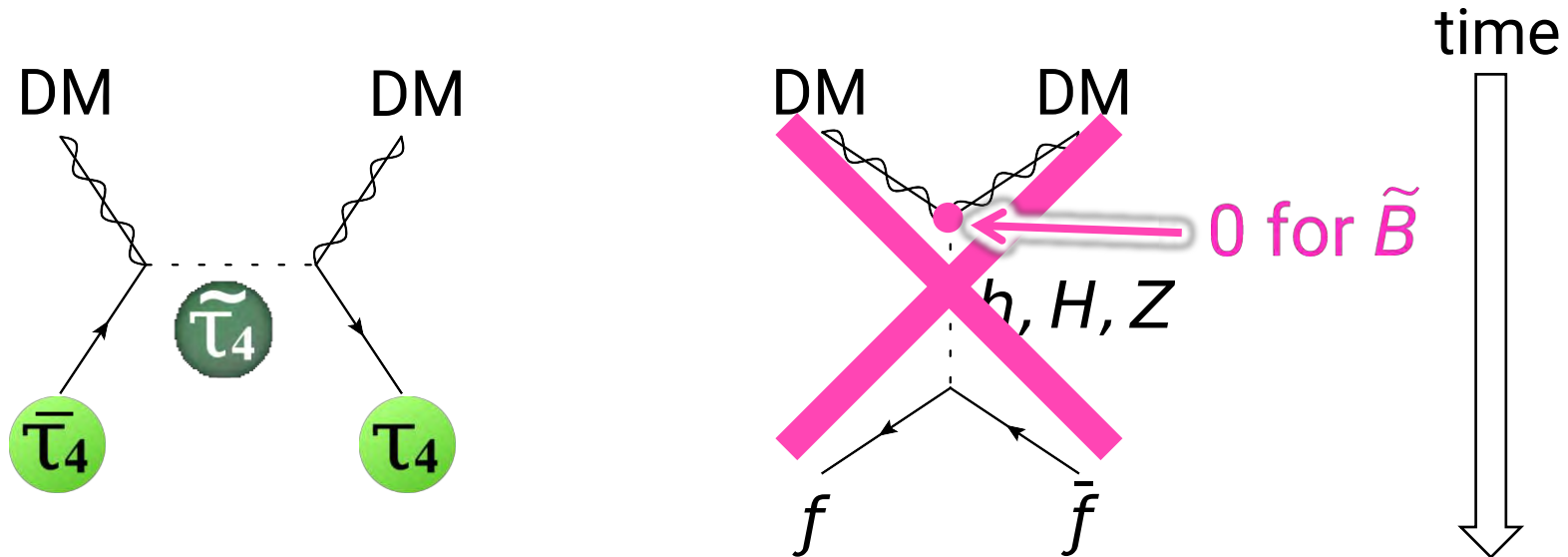
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- direct detection (LUX)

Summary with discussion seeds

- DM indirect detection (= searches for DM annihilation)



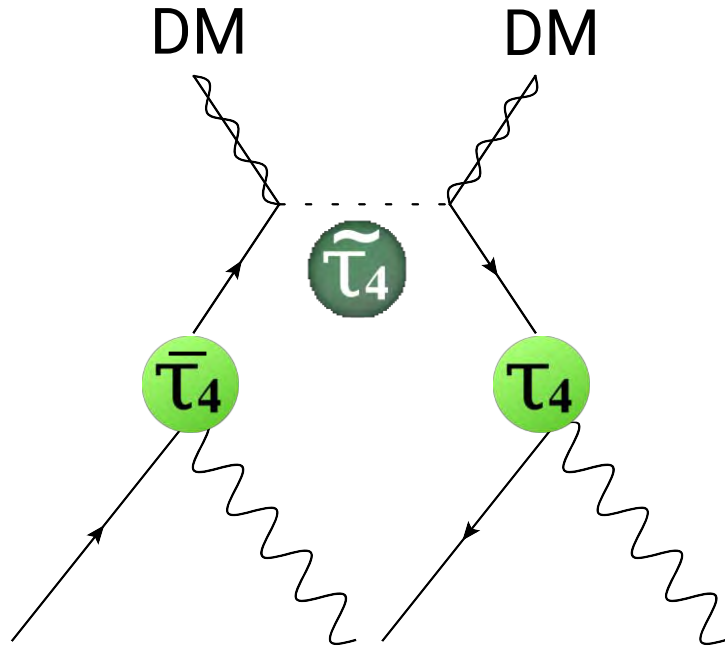
- DM indirect detection (= searches for DM annihilation)



$$\langle \sigma v \rangle = \frac{g_Y^4 Y_L^2 Y_R^2}{2\pi} \frac{m_f^2}{m_{\tilde{B}}^2} \frac{\sqrt{m_{\tilde{B}}^2 - m_f^2}}{(m_{\tilde{B}}^2 + m_f^2 - m_f^2)^2}$$

(in convention of $Q = T_3 + Y$)

- DM indirect detection (= searches for $DM DM \rightarrow \tau_4 \bar{\tau}_4$)



$$\tau_4 \rightarrow \begin{cases} W + \nu \\ Z + l \\ h + l \end{cases} \quad \left(\begin{array}{l} \nu = \nu_e, \nu_\mu, \nu_\tau \\ l = e, \mu, \tau \end{array} \right)$$

$$W\nu : Zl : hl \sim 2 : 1 : 1$$

$$W \ni Y_e H_d L \bar{E} + M_{E_4} E_4 \bar{E}_4 + \epsilon_i H_d L_i \bar{E}_4$$

[vector-like mass] [mixing with SM leptons]

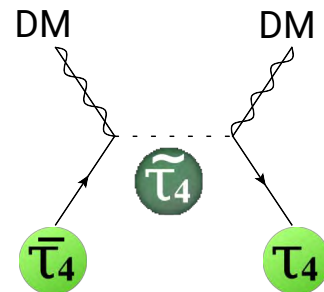
$$\langle \sigma v \rangle = \frac{g_Y^4 Y_L^2 Y_R^2}{2\pi} \frac{m_f^2}{m_{\tilde{B}}^2} \frac{\sqrt{m_{\tilde{B}}^2 - m_f^2}}{(m_{\tilde{B}}^2 + m_f^2 - m_f^2)^2}$$

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$$W\nu : Zl : hl \sim 2 : 1 : 1$$



DM DM →

$\tau_{4(5)}$ mixes with e W^+W^- ZZ hh $\nu\bar{\nu}$ e^+e^-

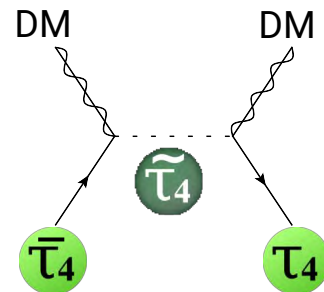
$\tau_{4(5)}$ mixes with μ W^+W^- ZZ hh $\nu\bar{\nu}$ $\mu^+\mu^-$

$\tau_{4(5)}$ mixes with τ W^+W^- ZZ hh $\nu\bar{\nu}$ $\tau^+\tau^-$

■ DM indirect detection

$$W \ni Y_e H_d L \bar{E} + M_{E_4} E_4 \bar{E}_4 + \epsilon_i H_d L_i \bar{E}_4$$

$$W\nu : Zl : Hl \sim 2 : 1 : 1$$



insensitive (IceCube)

DM DM →

$\tau_{4(5)}$ mixes with e

$W^+W^- \quad ZZ \quad hh$

$\nu\bar{\nu}$

less sensitive / large BKG uncertainty

e^+e^-

$\tau_{4(5)}$ mixes with μ

$W^+W^- \quad ZZ \quad hh$

$\nu\bar{\nu}$

$\mu^+\mu^-$

$\tau_{4(5)}$ mixes with τ

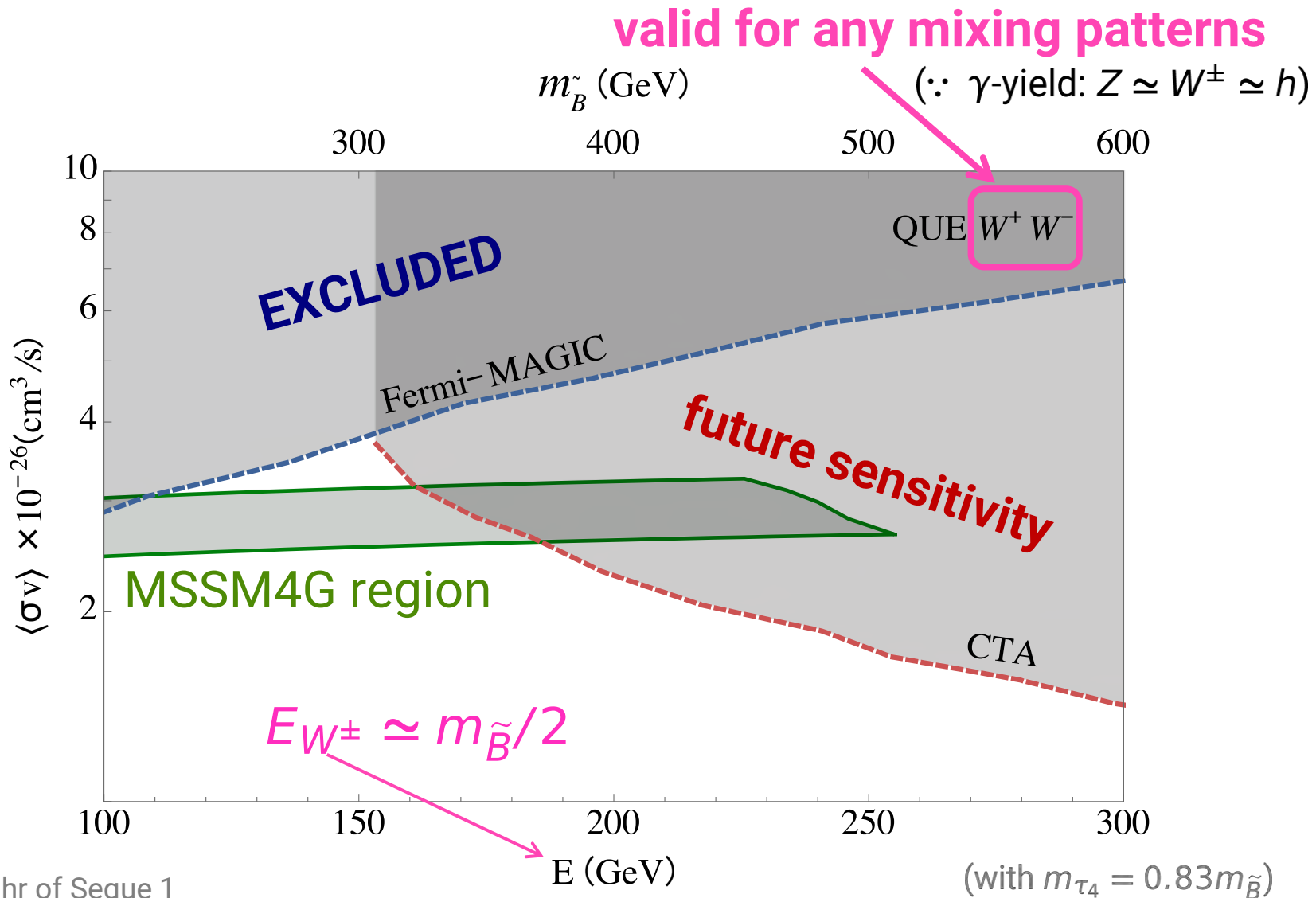
$W^+W^- \quad ZZ \quad hh$

$\nu\bar{\nu}$

$\tau^+\tau^-$

→ ... → γ

→ π^0 → γ



MAGIC: 158 hr of Segue 1

Fermi-LAT: 6 yr of 15 dSph (incl. Segue 1)

DM profile: NFW

Fermi-LAT dominates MAGIC in almost all E -range.

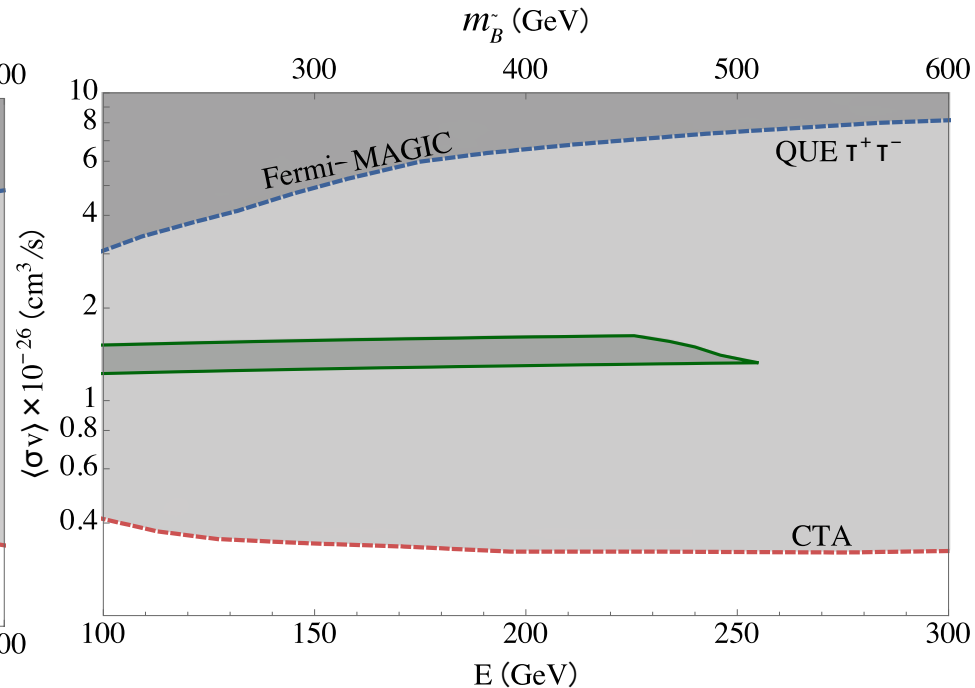
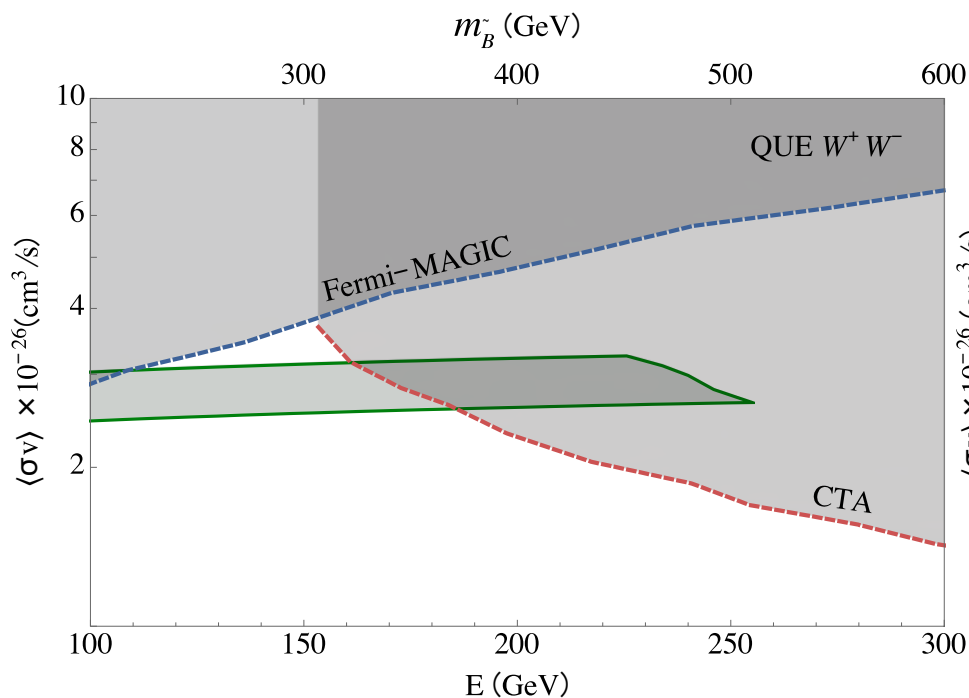
CTA prospect : 500hr of Milky Way

DM profile: Einasto

No syst. unc. (stat only)

WW (any mixing pattern)

$\tau\tau$ (only for τ -mixing cases)



- ✓ τ -mixing fully covered
- ✓ e/ μ -mixing with $m_{\tilde{B}} > 340-380$ GeV covered

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(with $m_{\tau_4} = 0.83m_{\tilde{B}}$)

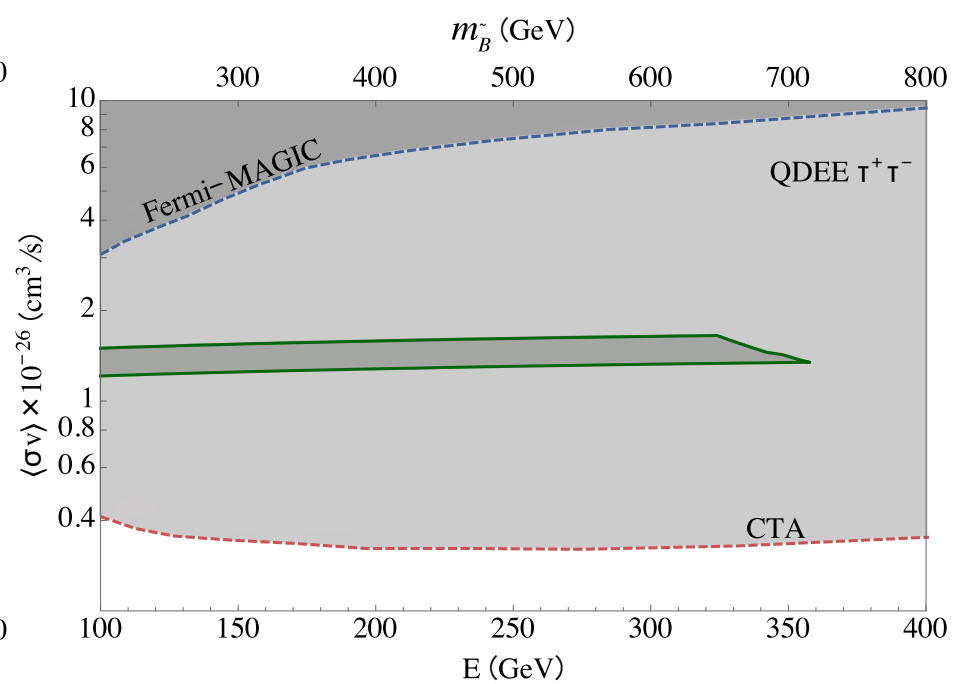
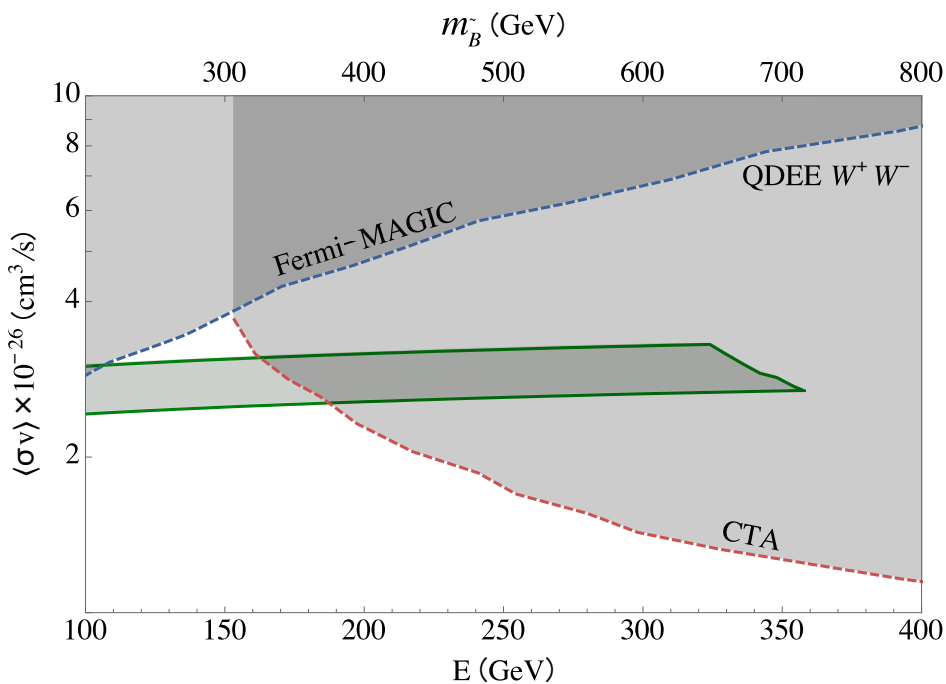
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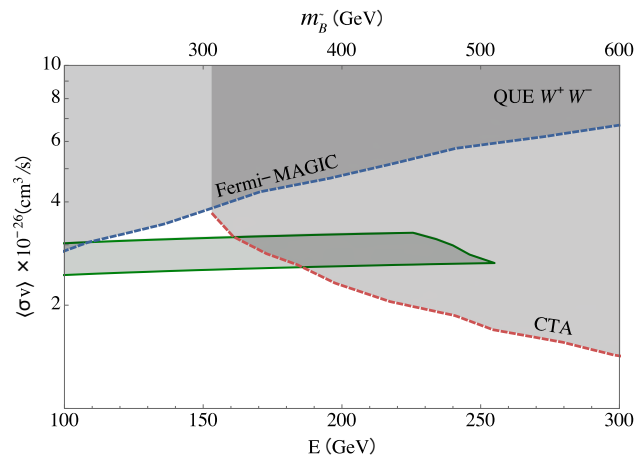
DM profile: Einasto

No syst. unc. (stat only)

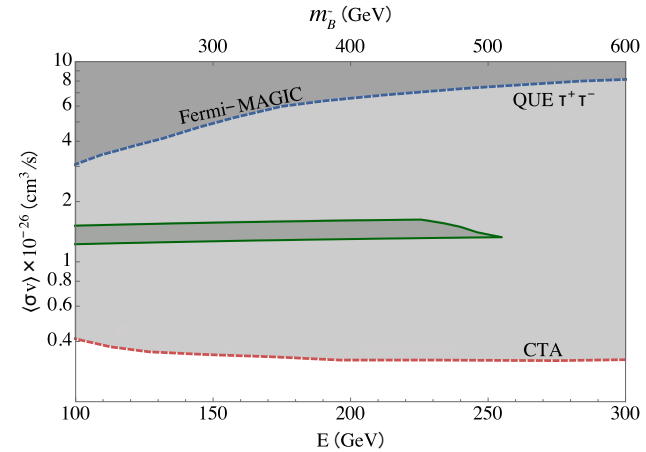
Summary

| | e-mixing | μ -mixing | τ -mixing |
|-----------|--------------------------------------|---------------|----------------------|
| CTA 500hr | covers $m_{\tilde{B}} > 340-380$ GeV | | full coverage |
| HL-LHC | | | |

e/ μ -mixing, QUE



τ / μ -mixing, QUE



Introduction: why overabundant?

Model: MSSM4G[📶] solves overabundance.

Analysis:

- cosmic rays (CTA, Fermi, MAGIC)
- colliders (LHC)
- direct detection (LUX)

Summary with discussion seeds

■ MSSM + $E\bar{E}$ → breaks coupling unification

■ QUE model : MSSM + $Q\bar{Q}U\bar{U}E\bar{E}$

⇒ SM + $\tilde{\chi}_1^0 (\approx \tilde{B})$, τ_4 ,
 $\underbrace{\tilde{\tau}_{4L}, \tilde{\tau}_{4R}}_{\text{assumed to be equal-mass}}$

■ QDEE model : MSSM + $Q\bar{Q}D\bar{D}E\bar{E}E\bar{E}$

⇒ SM + $\tilde{\chi}_1^0 (\approx \tilde{B})$, $\underbrace{\tau_4, \tau_5}_{\text{assumed to be equal-mass}}$,
 $\underbrace{\tilde{\tau}_{4L}, \tilde{\tau}_{4R}, \tilde{\tau}_{5L}, \tilde{\tau}_{5R}}_{\text{assumed to be equal-mass}}$

■ MSSM + $E\bar{E}$ → breaks coupling unification

■ QUE model : MSSM + $Q\bar{Q}U\bar{U}E\bar{E}$

⇒ SM + $\tilde{\chi}_1^0 (\approx \tilde{B}), \tau_4,$
 τ_{4L}, τ_{4R}
 assumed to be equal-mass

extra lepton search (red line from τ_4)

slepton search (blue line from τ_{4L}, τ_{4R})

■ QDEE model : MSSM + $Q\bar{Q}D\bar{D}E\bar{E}E\bar{E}$

⇒ SM + $\tilde{\chi}_1^0 (\approx \tilde{B}), \tau_4, \tau_5,$
 $\tau_{4L}, \tau_{4R}, \tau_{5L}, \tau_{5R}$
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extra lepton search (red line from τ_4, τ_5)

slepton search (blue line from $\tau_{4L}, \tau_{4R}, \tau_{5L}, \tau_{5R}$)

■ MSSM + $E\bar{E}$ → breaks coupling unification

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⇒ SM + $\tilde{\chi}_1^0 (\approx \tilde{B})$, τ_4 ,

$\tilde{\tau}_{4L}, \tilde{\tau}_{4R}$

assumed to be equal-mass

$\equiv 2(4)$

+ $Q\bar{Q}D\bar{D}E\bar{E}E\bar{E}$

assumed to be equal-mass

τ_4, τ_5 ,

$\tilde{\tau}_{4L}, \tilde{\tau}_{4R}, \tilde{\tau}_{5L}, \tilde{\tau}_{5R}$

assumed to be equal-mass

slepton search

$\tilde{\tau}_4 \not\rightarrow \tau_4 + \tilde{B}$
 $\rightarrow (e, \mu, \tau) + \tilde{B}$
 $\times \tilde{l}_R$

extra lepton search

$\tau_4 \rightarrow W\nu, Zl, hl$
 (as discussed before)

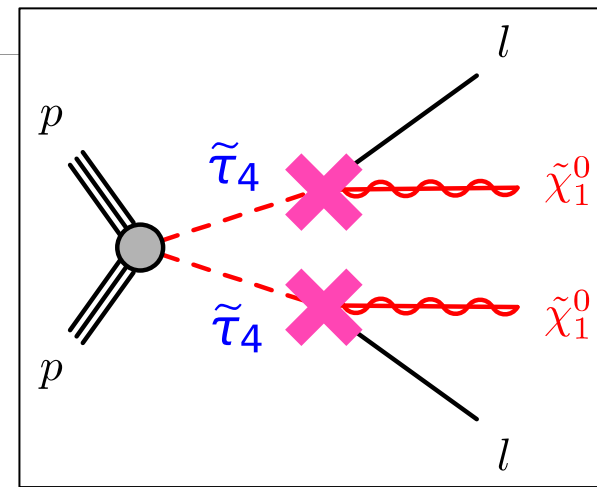
standard searches for vectorlike leptons (but 2x in QDEE)

Collider prospects for **extra slepton** searches

$$pp \rightarrow \tilde{\tau}_{4(5)} \tilde{\tau}_{4(5)}^* \equiv pp \rightarrow \tilde{l}_R \tilde{l}_R^*$$

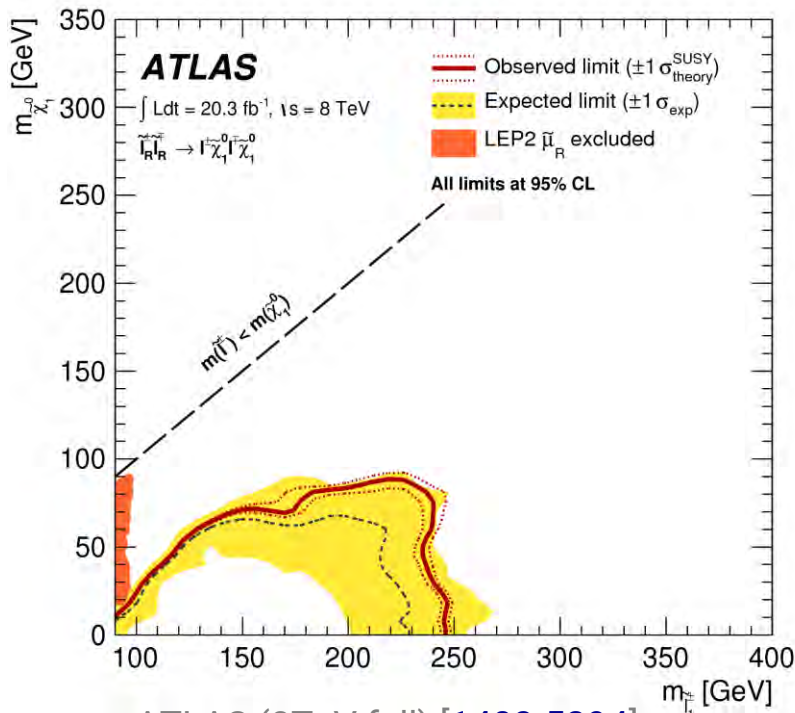
determined by mixing parameters

e/ μ -mixing \rightarrow slepton searches $\times 2$ (4)
($\tilde{e}_R, \tilde{\mu}_R$)

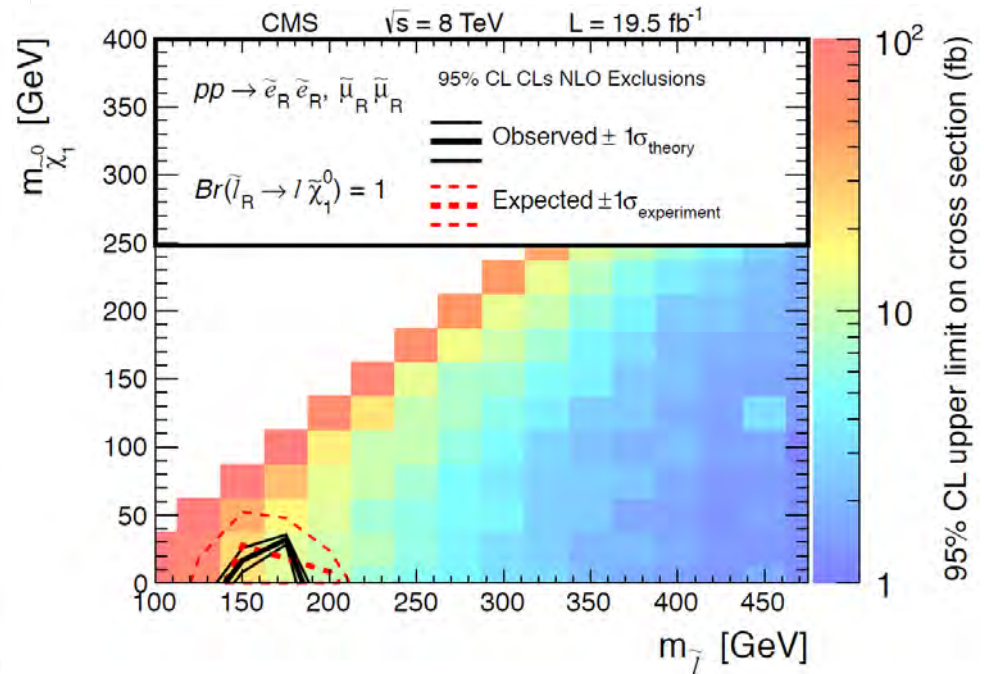


14 TeV prospects studied in [1408.2841](#) (Eckel, Ramsey-Musolf, Shepherd, Su)

\rightarrow re-interpreted



ATLAS (8TeV full) [[1403.5294](#)]



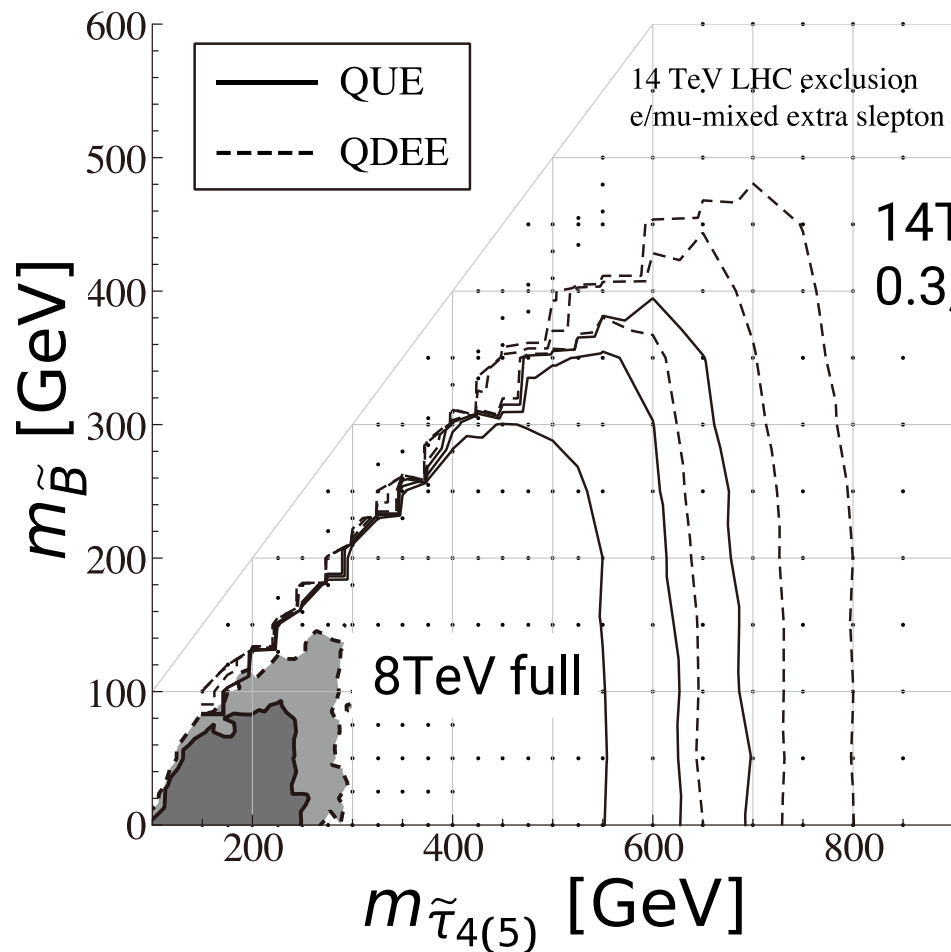
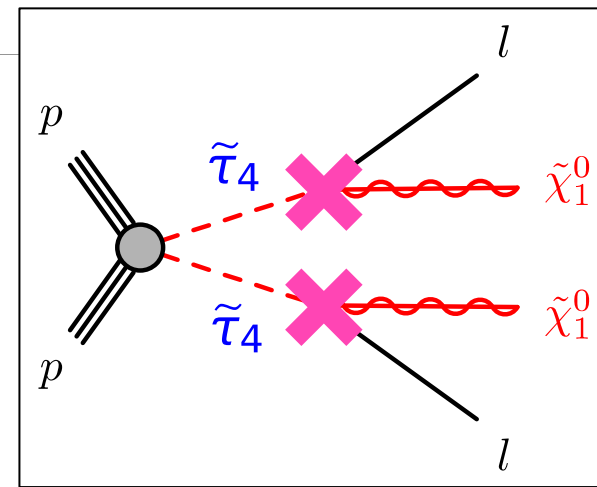
CMS (8TeV full) [[1405.7570](#)]

Collider prospects for extra slepton searches

$$pp \rightarrow \tilde{\tau}_{4(5)} \tilde{\tau}_{4(5)}^* \equiv pp \rightarrow \tilde{l}_R \tilde{l}_R^*$$

determined by mixing parameters

e/ μ -mixing \rightarrow slepton searches $\times 2$ (4)
 ($\tilde{e}_R, \tilde{\mu}_R$)



14TeV
 0.3, 1, 3/ab

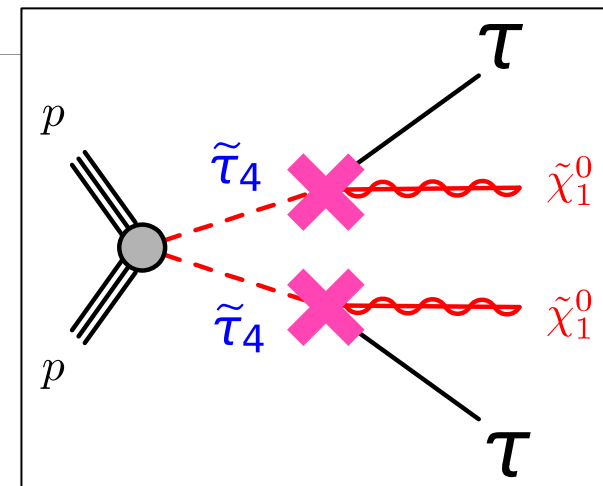
- 2 lepton + MET + mT2 + jet-veto
- BKG taken from 1408.2841
 - MG5-Pythia-Delphes (also for signal)
 - rescaled by NLO K-factor
 - di-boson dominates
- Signal events at LO level
- Uncertainties = stat. + 5% syst.

Collider prospects for extra slepton searches

$$pp \rightarrow \tilde{\tau}_{4,(5)} \tilde{\tau}_{4,(5)}^* \equiv pp \rightarrow \tilde{l}_R \tilde{l}_R^*$$

↑
determined by mixing parameters

τ -mixing \rightarrow stau searches $\times 2$ (4)

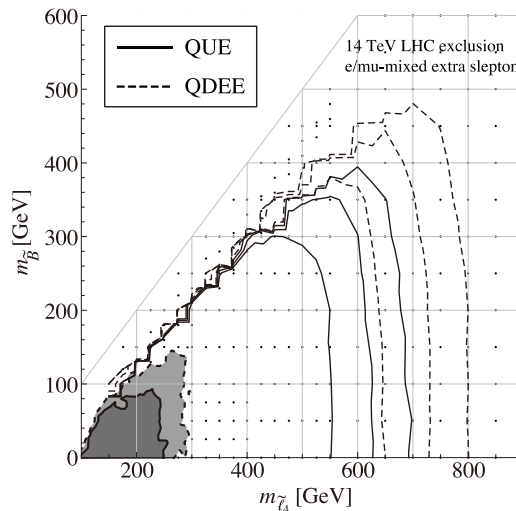
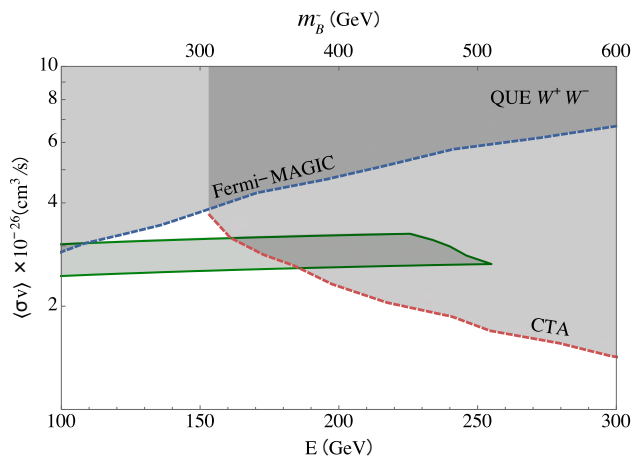


\rightarrow No constraint expected.

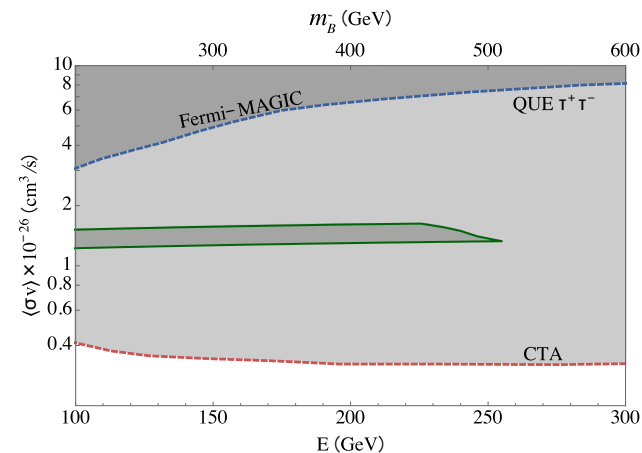
- LHC Run 1 provided no limit on MSSM stau mass.
- 14TeV, 3/ab LHC will not exclude MSSM4G parameter region.

| | e-mixing | μ -mixing | τ -mixing |
|------------------|---|---------------|----------------------|
| CTA 500hr | covers $m_{\tilde{B}} > 340-380$ GeV | | full coverage |
| HL-LHC (slepton) | covers $m_{\tilde{B}} < 400$ (480) GeV (but not “degenerate” region) | | — |
| HL-LHC (lepton) | | | |

e/ μ -mixing



τ/μ -mixing, QUE



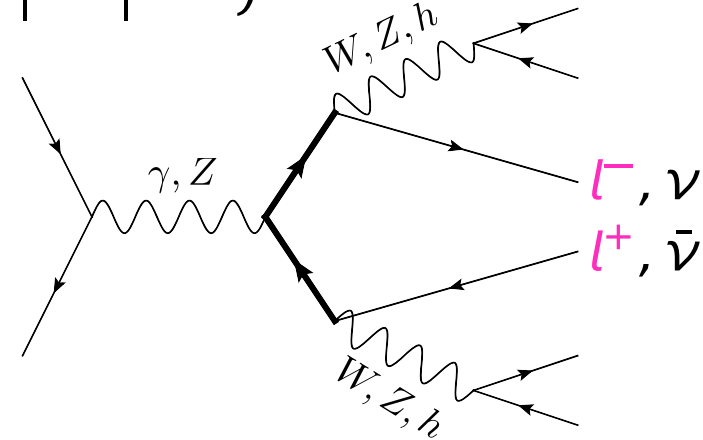
$$pp \rightarrow \tau_{4,(5)}^+ \tau_{4,(5)}^- \rightarrow (W\nu | hl | Zl)(W\nu | hl | hZ)$$

e/ μ -mixing case

“vectorlike lepton searches” by
multi- l^\pm signature (3–5 l^\pm)

[Cf. ATLAS collaboration, [1506.01291](#)]

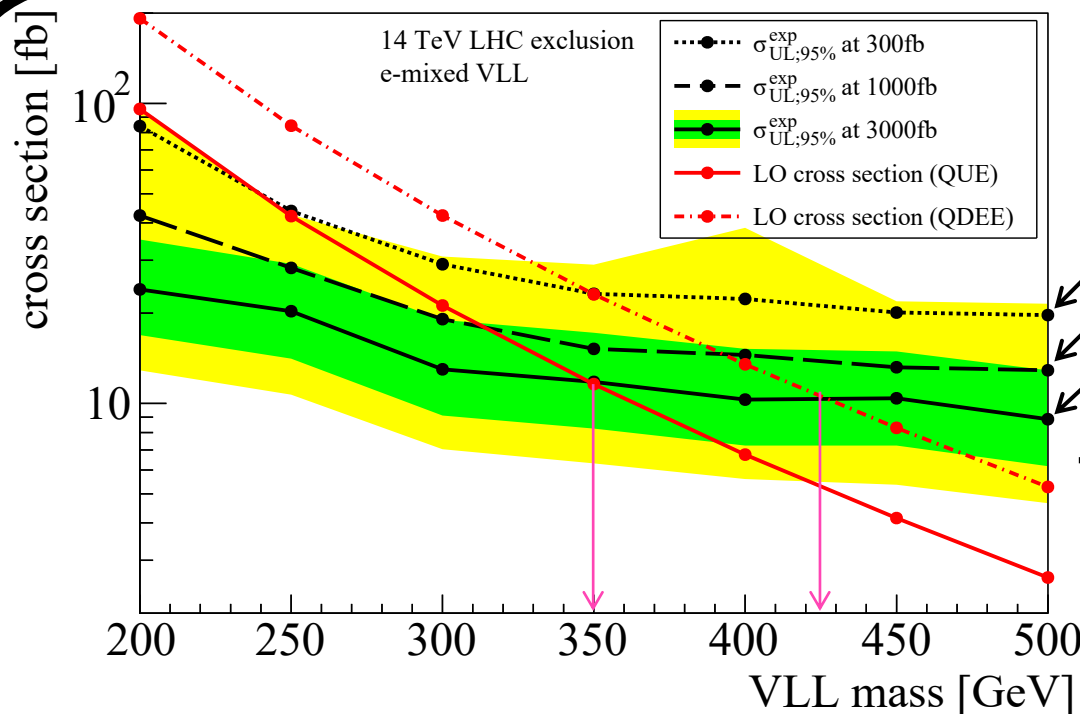
$$\left\{ \begin{array}{l} W\nu Zl \rightarrow 3l \text{ (1.3\%)} \\ W\nu hl \rightarrow 3l \text{ (0.6\%)} \\ hlZl \rightarrow 3l \text{ (0.8\%)} \\ hlhl \rightarrow 3l \text{ (0.8\%)} \end{array} \right. \quad \left\{ \begin{array}{l} W\nu Zl \rightarrow 4^+ l \text{ (0.4\%)} \\ hlZl \rightarrow 4^+ l \text{ (1.0\%)} \\ ZlZl \rightarrow 4^+ l \text{ (0.8\%)} \\ hlhl \rightarrow 4^+ l \text{ (0.2\%)} \end{array} \right.$$



→ Monte Carlo simulation

$$pp \rightarrow \tau_{4,(5)}^+ \tau_{4,(5)}^- \rightarrow (W\nu | hl | Zl)(W\nu | hl | hZ)$$

e/ μ -mixing case



\rightarrow 14TeV, 3/ab covers
 $m_{\tau_4} < 350$ (425) GeV
 QUE QDEE

- Snowmass BKG set is used.
 - MG5-Pythia-Delphes + NLO K -factor
 - di-boson + tt dominated
- SR dedicated for WZ / ZZ + leptons
 - 3L, 4L for WZ, and 4L, 5L for ZZ
 - tau-tag / b-tag not used (avoided)
- Signal by FR-MG5aMC-Pythia-Delphes (LO)
- Uncertainties = stat. + 20% syst.

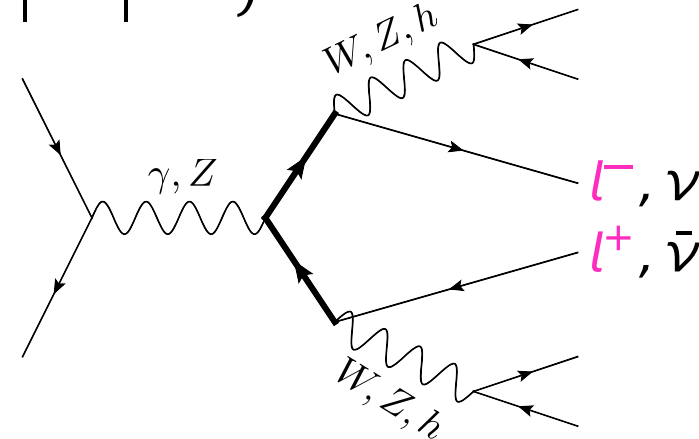
$$pp \rightarrow \tau_{4(5)}^+ \tau_{4(5)}^- \rightarrow (W\nu | hl | Zl)(W\nu | hl | hZ)$$

e/ μ -mixing case

“vectorlike lepton searches” by
multi- l^\pm signature ($3-5l^\pm$)

[Cf. ATLAS collaboration, [1506.01291](#)]

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→ 14TeV, 3/ab covers
 $m_{\tau_4} < 350 \text{ (425) GeV}$
QUE QDEE

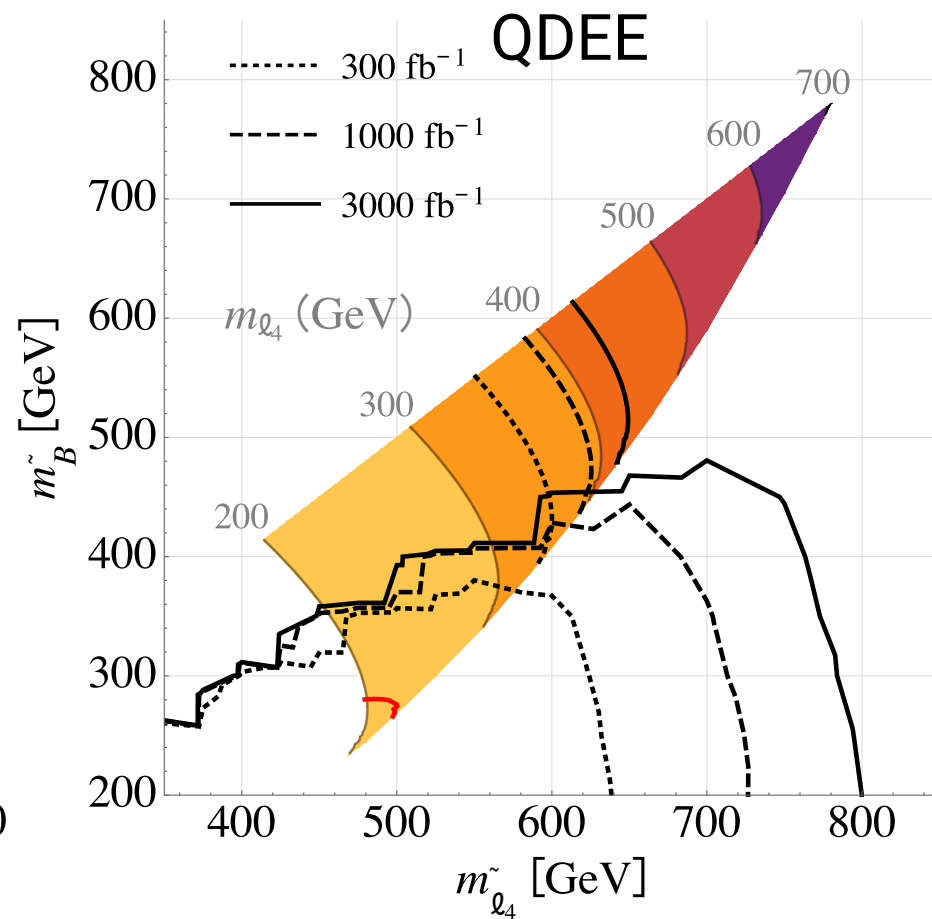
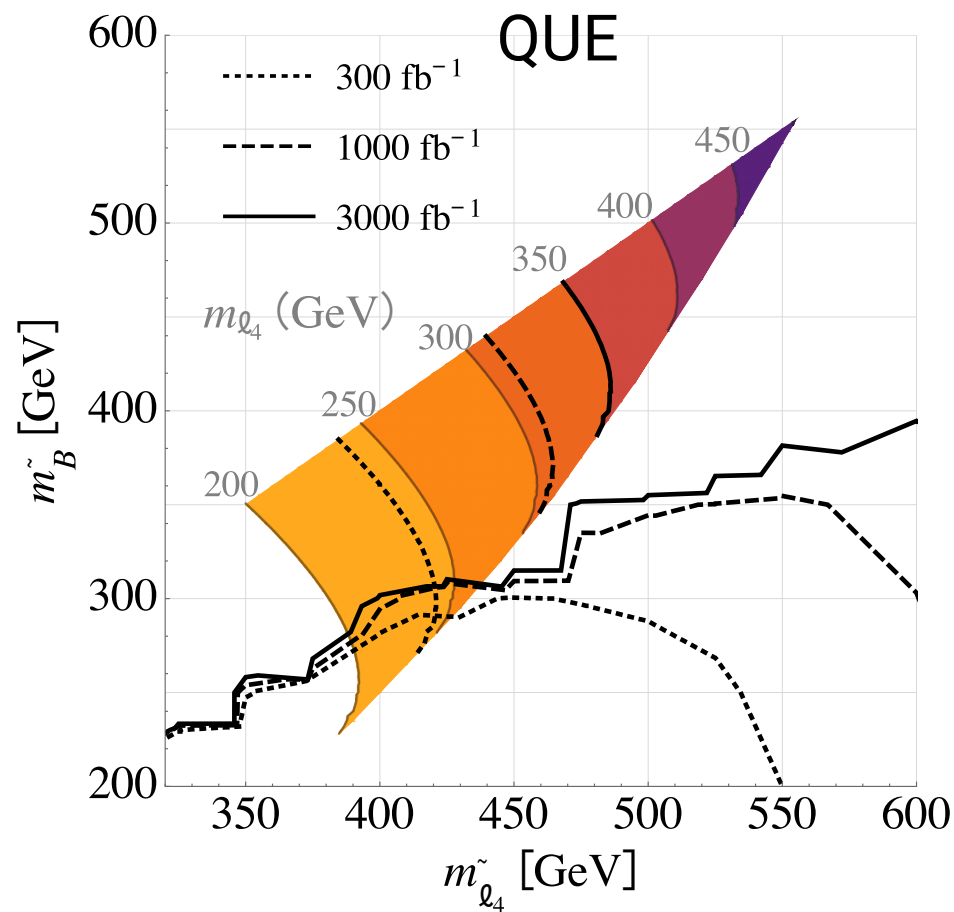
τ -mixing case

✓ [1510.03456](#) (Kumar and Matrin)

- SRs: 4(e, mu, had-tau)
- Signal and BKG by their MC (FR-MG5-Pythia-Delphes)
- no prospects for exclusion if BKG syst. unc. > 10%

→ 13 TeV, 3/ab covers
 $m_{\tau_4} < 234 \text{ (264) GeV}$
with “a very optimistic BKG estimation”

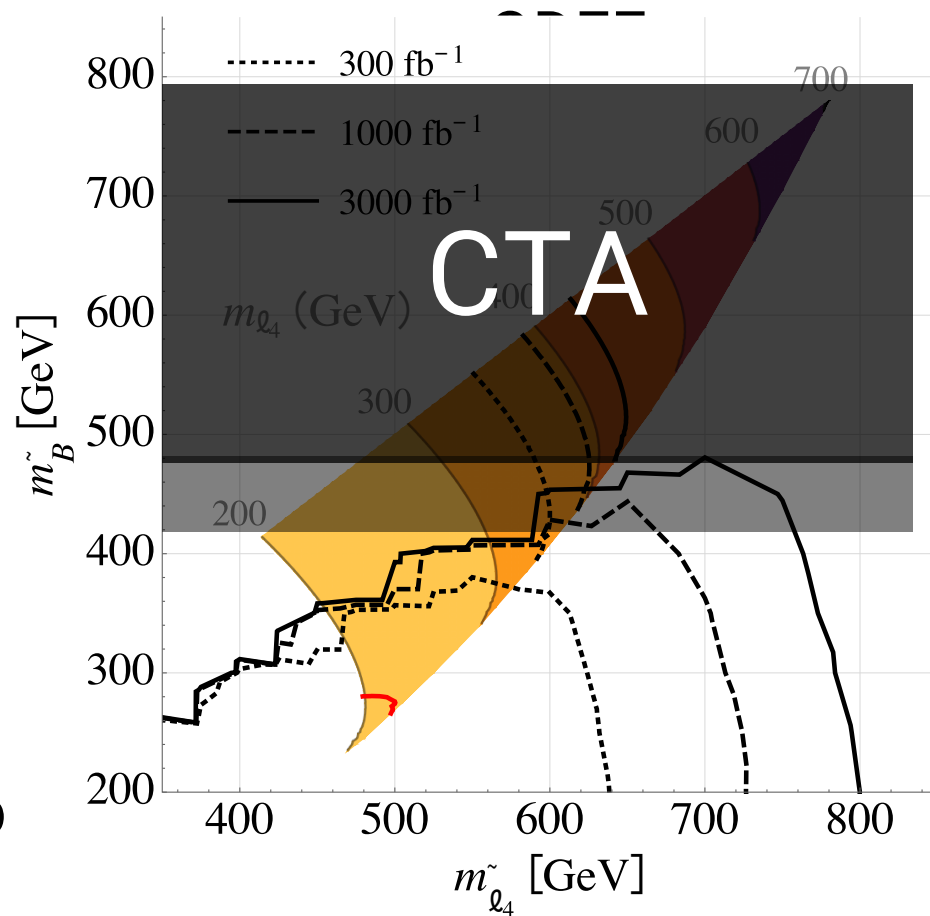
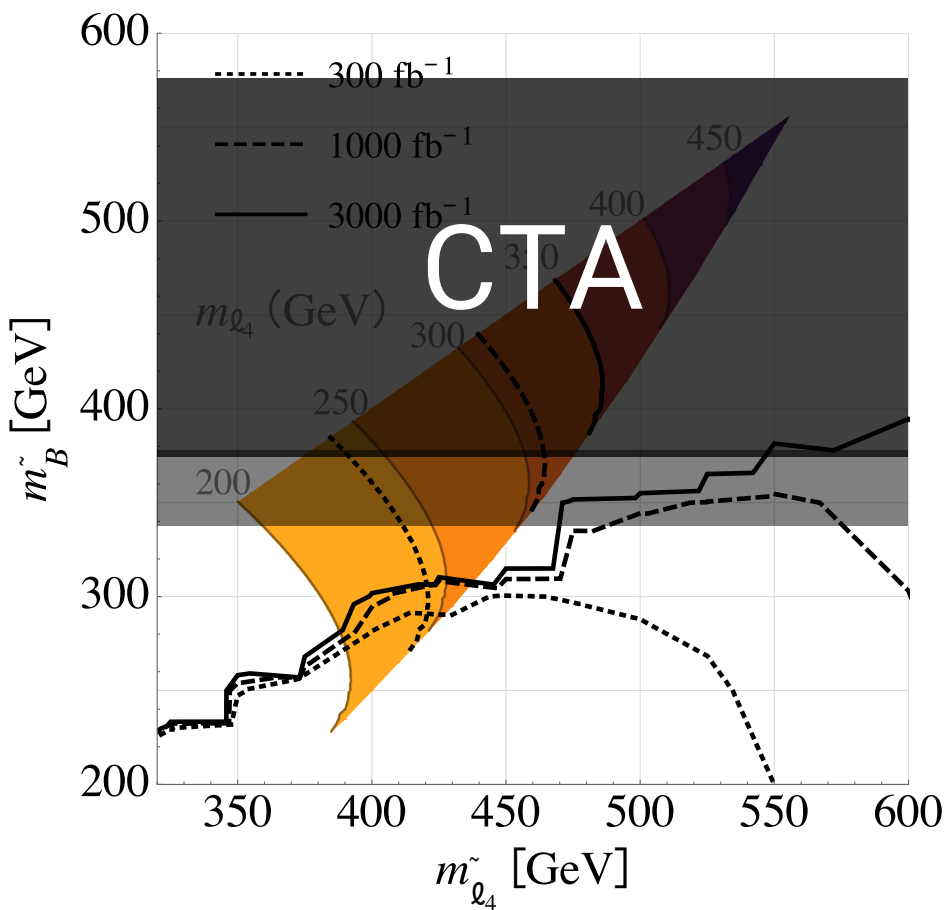
■ e/ μ -mixing cases



■ τ -mixing case

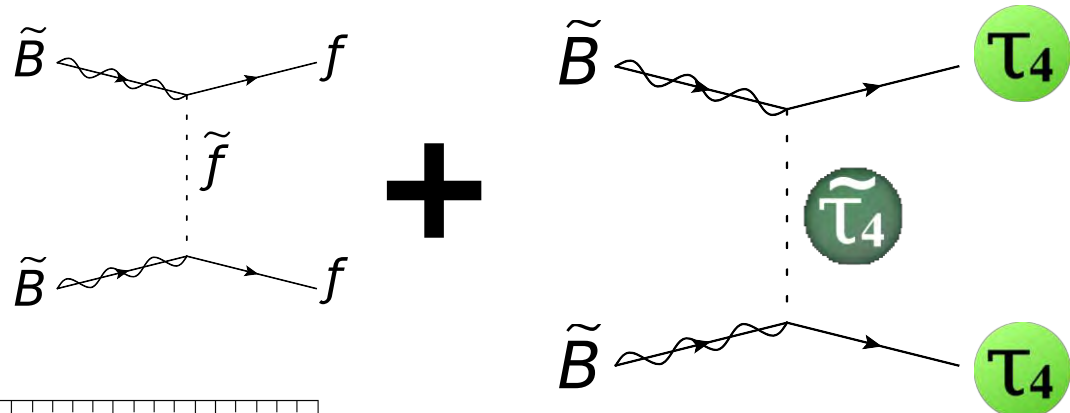
➤ LHC insensitive ... ($\tau \cdot \omega \cdot \tau$)

■ e/ μ -mixing cases



■ τ -mixing case

- LHC insensitive, but CTA covers full region



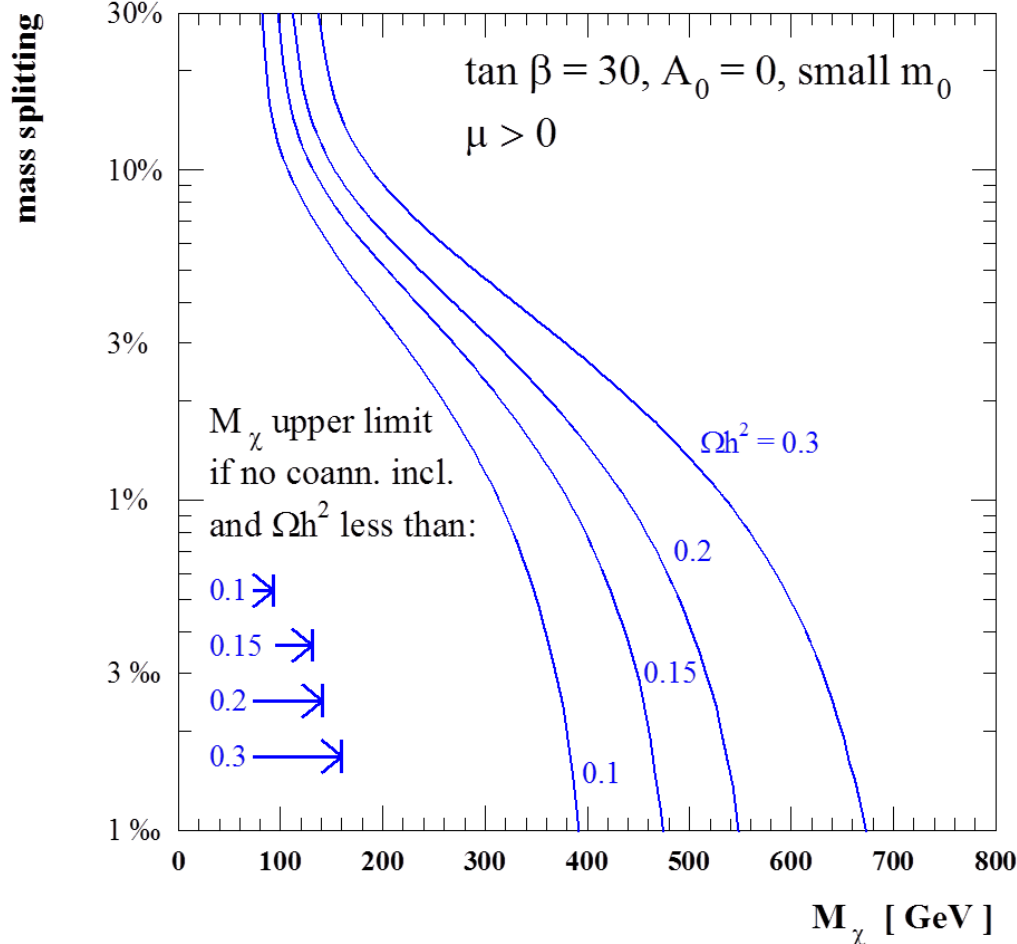
extra annihilation channel

→ larger Ωh^2
 → “proper” $\langle \sigma v \rangle$

if $\tilde{\tau}_4 \gtrsim \tilde{B} > \tau_4$

$\langle \sigma v \rangle \propto Y^4 \implies \text{MSSM} + E\bar{E}$

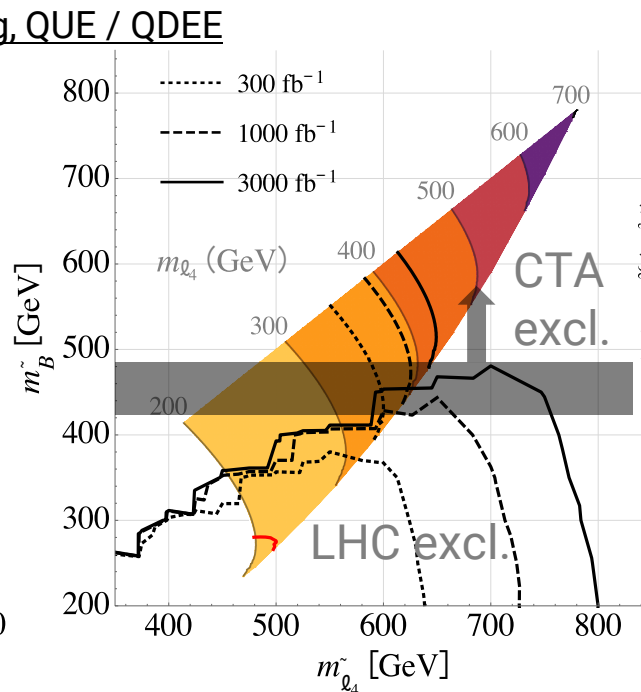
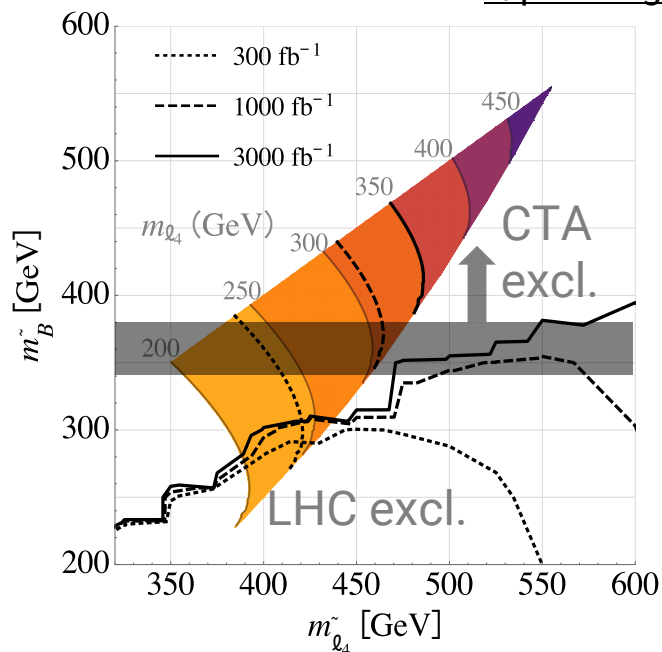
$$Y_u H_u Q \bar{U} + Y_d H_d Q \bar{D} + Y_e H_d L \bar{E} \\
 + M_{E_4} E_4 \bar{E}_4 + \epsilon_i H_d L_i \bar{E}_4$$



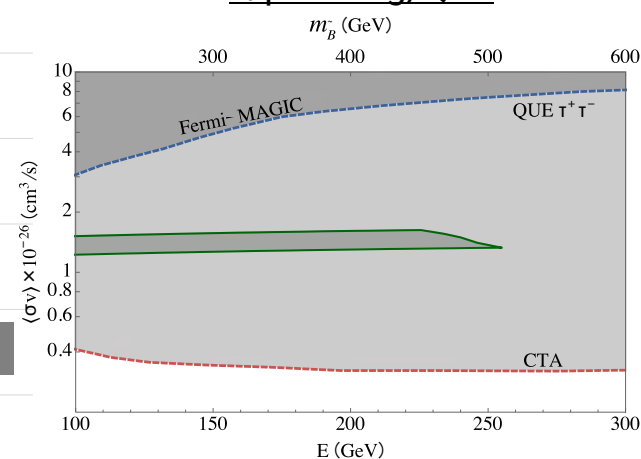
Summary : Future prospects

| | e-mixing | μ -mixing | τ -mixing |
|------------------|--|---------------|----------------------|
| CTA 500hr | covers $m_{\tilde{B}} > 340\text{--}380$ GeV | | full coverage |
| HL-LHC (slepton) | covers $m_{\tilde{B}} < 400$ (480) GeV (but not “degenerate” region) | | — |
| HL-LHC (lepton) | covers $m_{\tau_4} < 350$ (430) GeV equivalent to $m_{\tilde{B}} < 380$ (480) GeV | | — |

e/ μ -mixing, QUE / QDEE



τ / μ -mixing, QUE



Introduction: why overabundant?

Model: **MSSM4G**  solves overabundance.

Analysis:

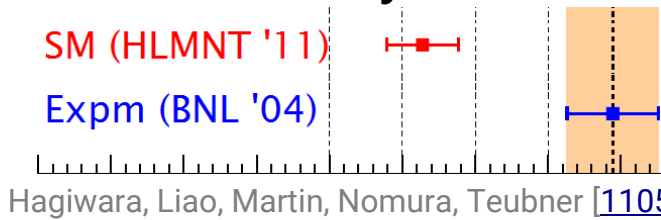
- cosmic rays (CTA, Fermi, MAGIC)
- colliders (LHC)
- direct detection (LUX)

Summary with discussion seeds

: “muon $g-2$ problem”

$$\left(a_\mu := \frac{g_\mu - 2}{2} \right)$$

■ $(g - 2)_\mu$ anomaly



$$a_\mu^{\text{SM}} = (116\,591\,828 \pm 49) \times 10^{-11}$$

$$a_\mu^{\text{exp}} = (116\,592\,089 \pm 63) \times 10^{-11}$$

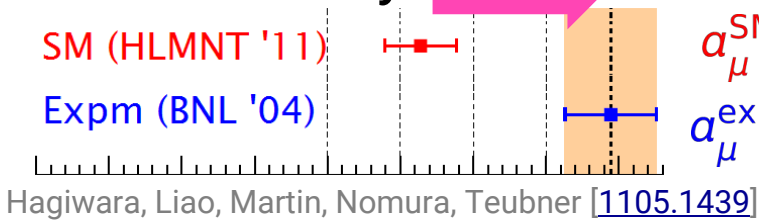
3.3 σ discrepancy

MSSM: extra contribution \rightarrow MSSM **may** explain this anomaly.

$$\left(a_\mu := \frac{g_\mu - 2}{2} \right)$$

■ $(g - 2)_\mu$ anomaly

PUSH UP



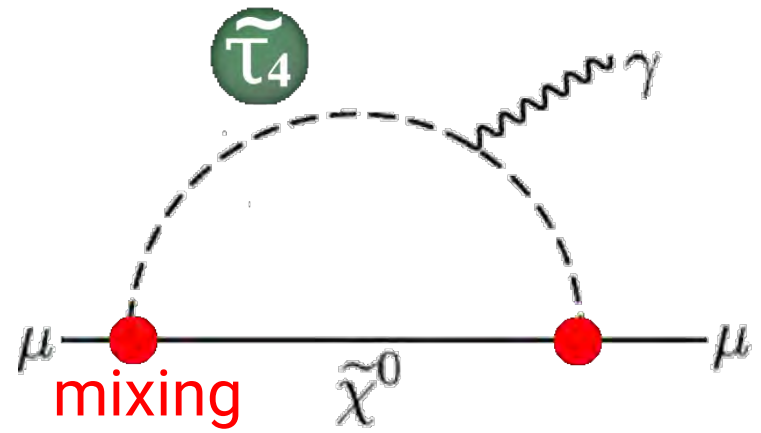
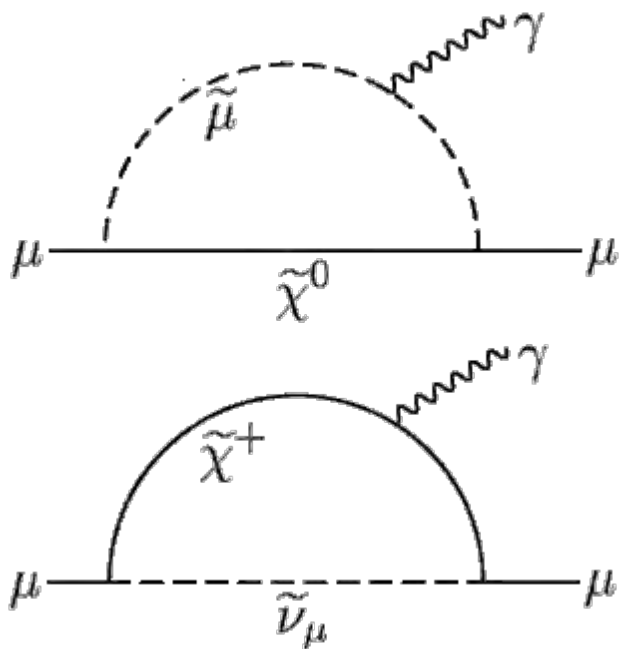
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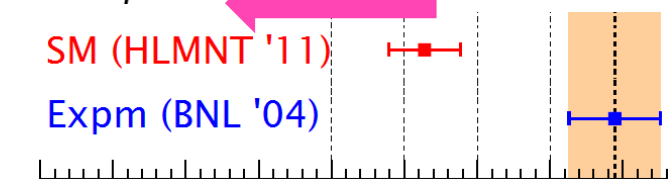
4G extra contribution?



$$\left(a_\mu := \frac{g_\mu - 2}{2} \right)$$

■ $(g - 2)_\mu$ anomaly

PUSH DOWN



$$a_\mu^{\text{SM}} = (116\,591\,828 \pm 49) \times 10^{-11}$$

$$a_\mu^{\text{exp}} = (116\,592\,089 \pm 63) \times 10^{-11}$$

Hagiwara, Liao, Martin, Nomura, Teubner [1105.1439]

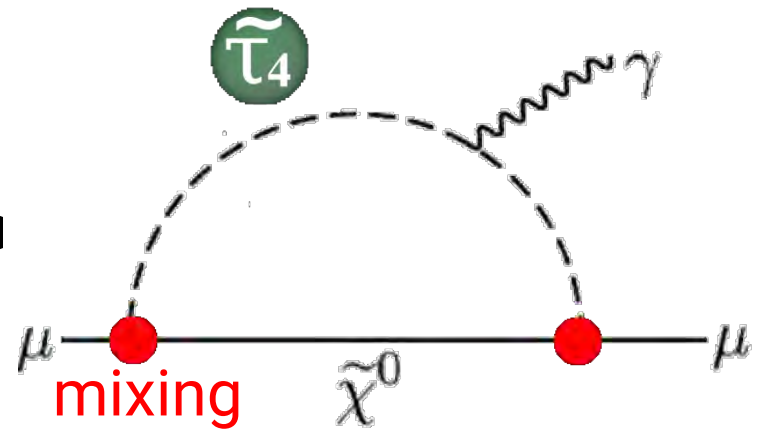
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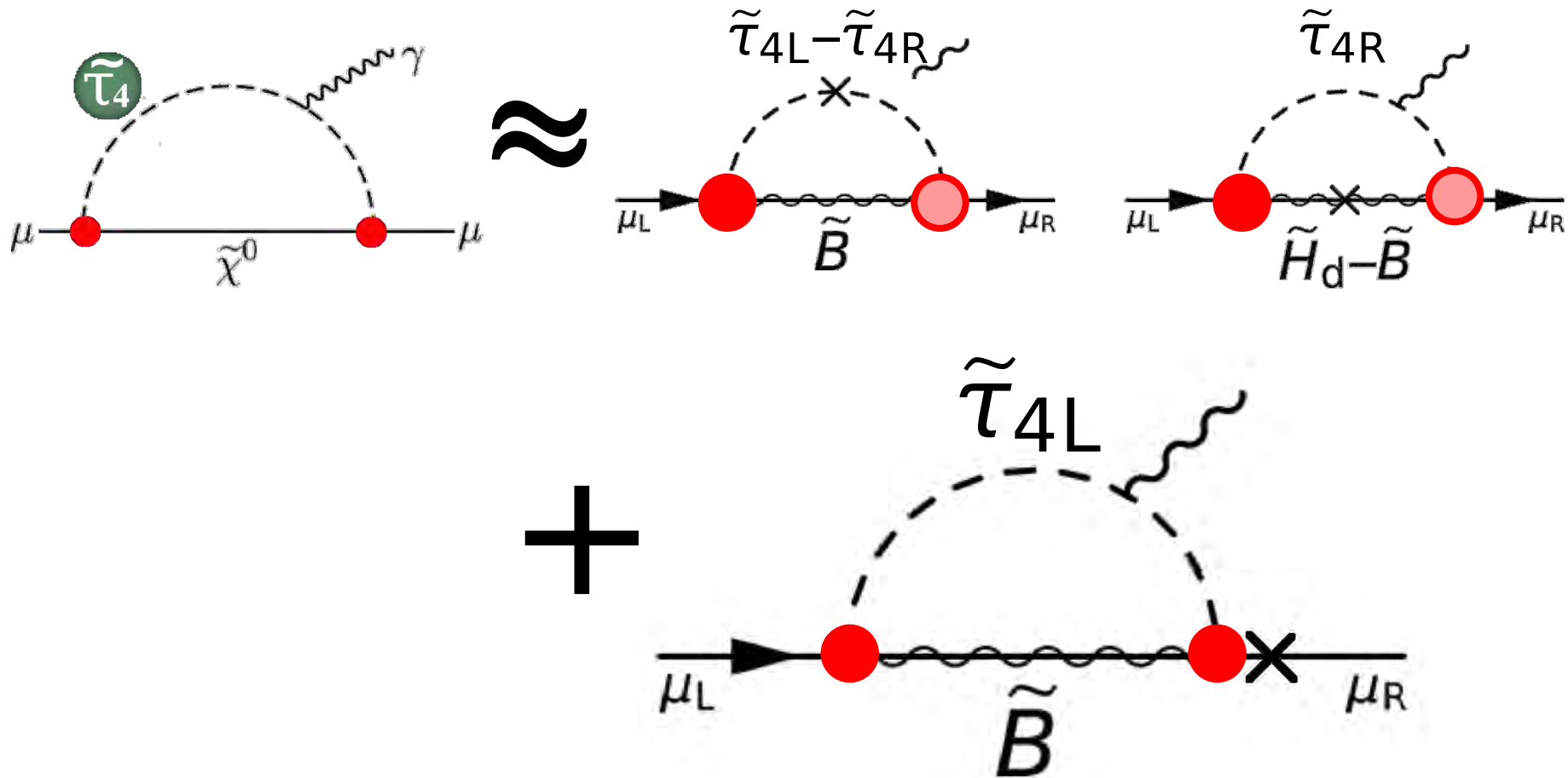
4G extra contribution?

0

\geq



■ Why always negative?

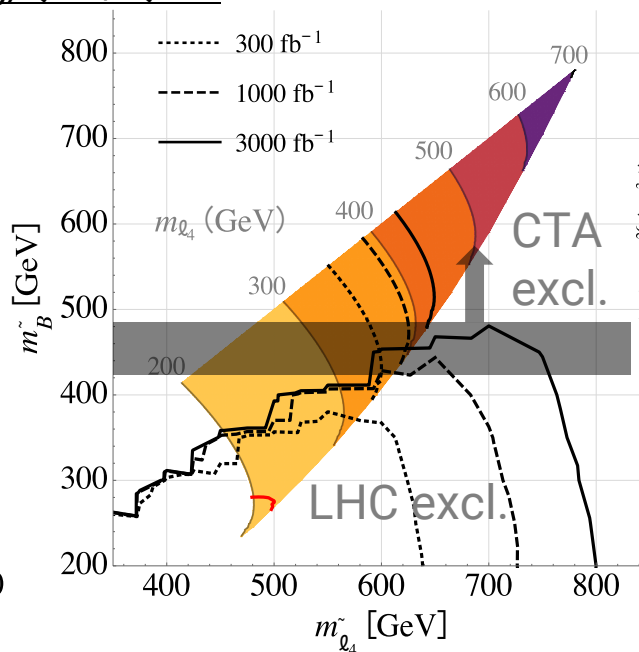
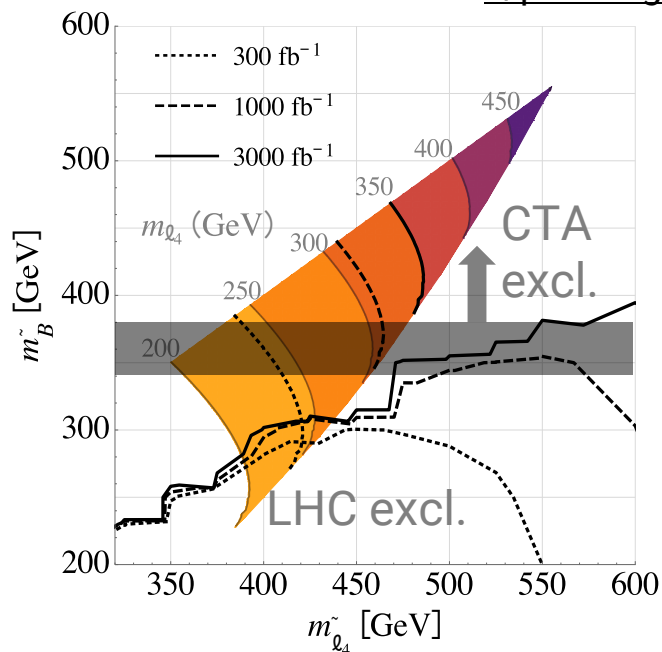


$$= -\frac{|\epsilon|^2}{16\pi^2} \frac{m_\mu^2}{6(|M_E|^2 + m_{\tilde{E}_c}^2)} N_1 \left(\frac{\mu^2}{|M_E|^2 + m_{\tilde{E}_c}^2} \right)$$

Summary : Future prospects

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|------------------|--|---------------|----------------------|
| CTA 500hr | covers $m_{\tilde{B}} > 340\text{--}380$ GeV | | full coverage |
| HL-LHC (slepton) | covers $m_{\tilde{B}} < 400$ (480) GeV (but not “degenerate” region) | | — |
| HL-LHC (lepton) | covers $m_{\tau_4} < 350$ (430) GeV equivalent to $m_{\tilde{B}} < 380$ (480) GeV | | — |

e/ μ -mixing, QUE / QDEE



τ / μ -mixing, QUE

